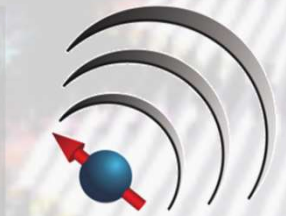


Magnetic Solitons in Spin-Orbitronics: novel science and applications in memory & non-conventional computing

M. Kläui

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www.klaeui-lab.de



- Introduction: **devices & chiral interactions**
- Topologically stabilized **Skyrmions**
- Fast dynamics: **Spin** and **Orbital Torques**
- Efficient dynamics: **thermal diffusion**
- **Non-conventional logic** with skyrmions

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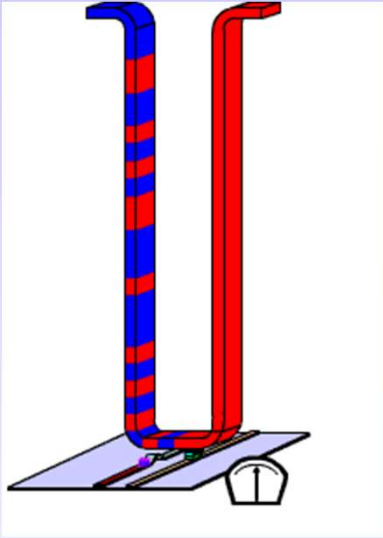
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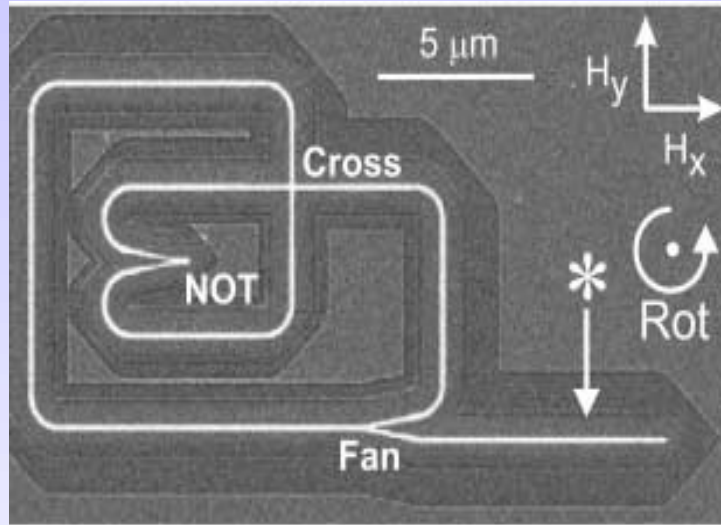
Devices based on Condensed Matter Solitons

Memory



Parkin et al., Science **320**, 190 ('08)
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Position & angle sensors



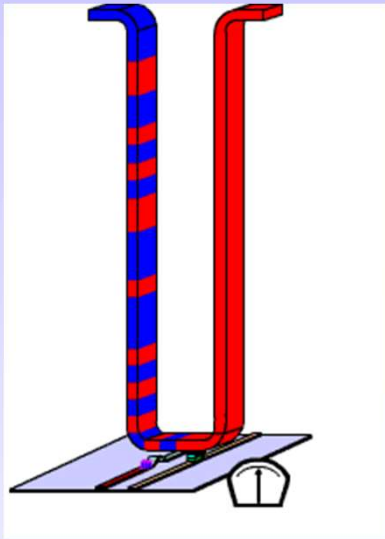
R. Mattheis et al., IEEE Trans. Magn. **45**, 3792 (2009)
A. Bisig et al., Nature Comm. **4**, 2328 (2013)

- Key low power IT devices based on magnetic spin structures include:
- Memory: non – volatile, no mechanically moving parts, one memory fits all
→ low power and simplified device architecture
- Logic: non – volatile, non – contact, no constant power source necessary:
→ low power + thermally excited diffusive dynamics → ultra-low power logic
- Sensing - Angle and position sensors: non – volatile, no constant power source necessary → low power, low maintenance



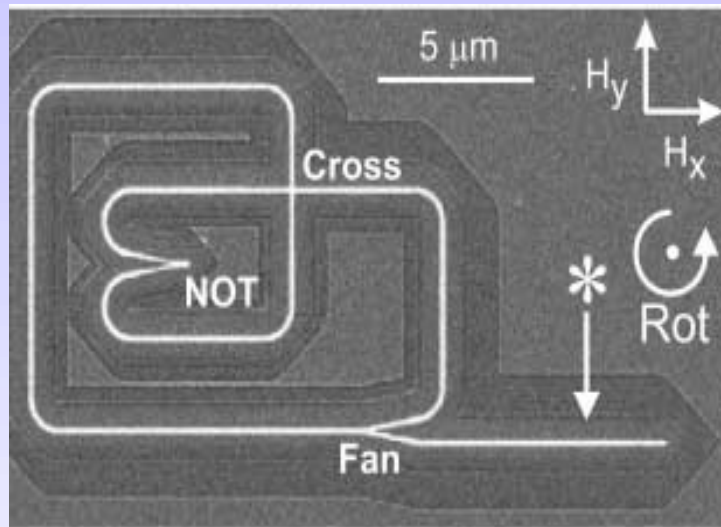
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Challenges for Spintronics Devices:

Statics: Stability – Long term information retention

→ Topological Spin Structures to the rescue

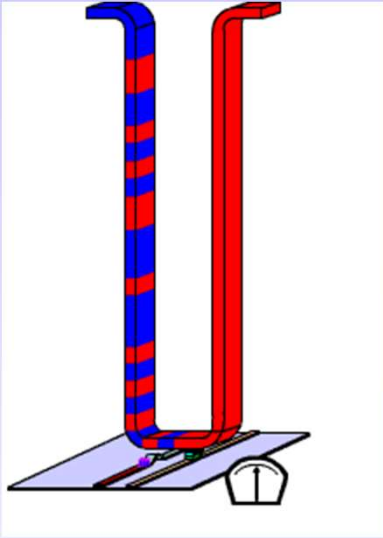
Dynamics: Manipulation – Efficiency and Speed

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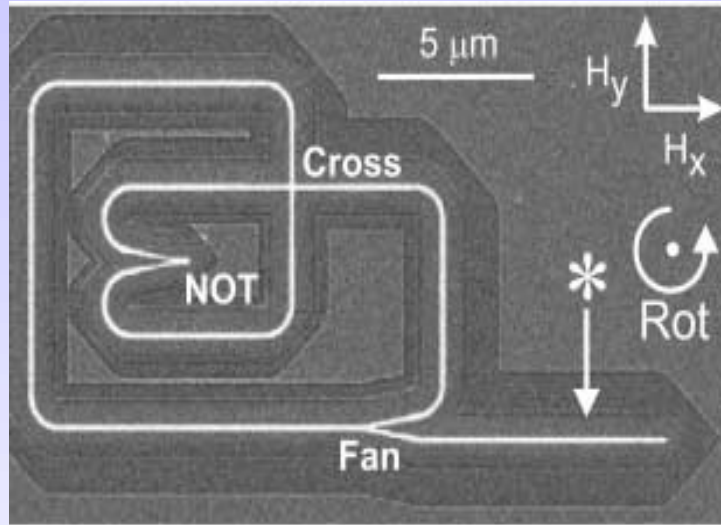
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Skyrmions in Spin-Orbitronics & Orbitronics: novel science and applications in memory & non-conventional computing

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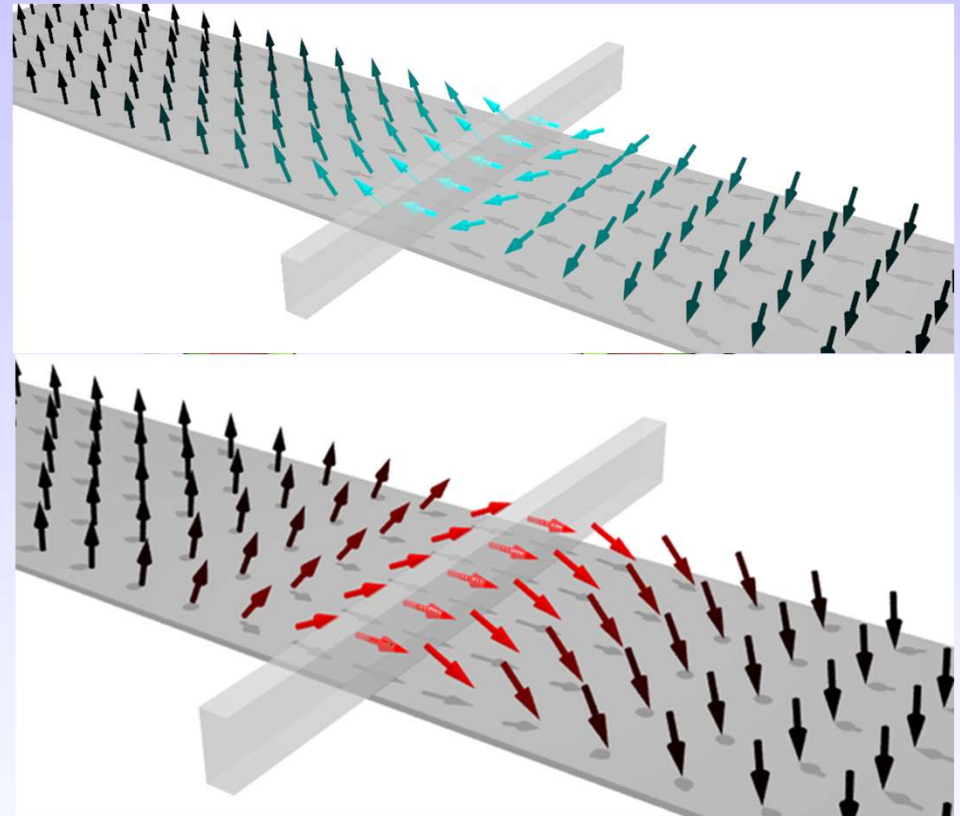


0. Magnetic coupling – Heisenberg exchange coupling

Conventional:

Spin-Spin Heisenberg
exchange interaction

➔ Stabilization of states with
**random topology and
random chirality**



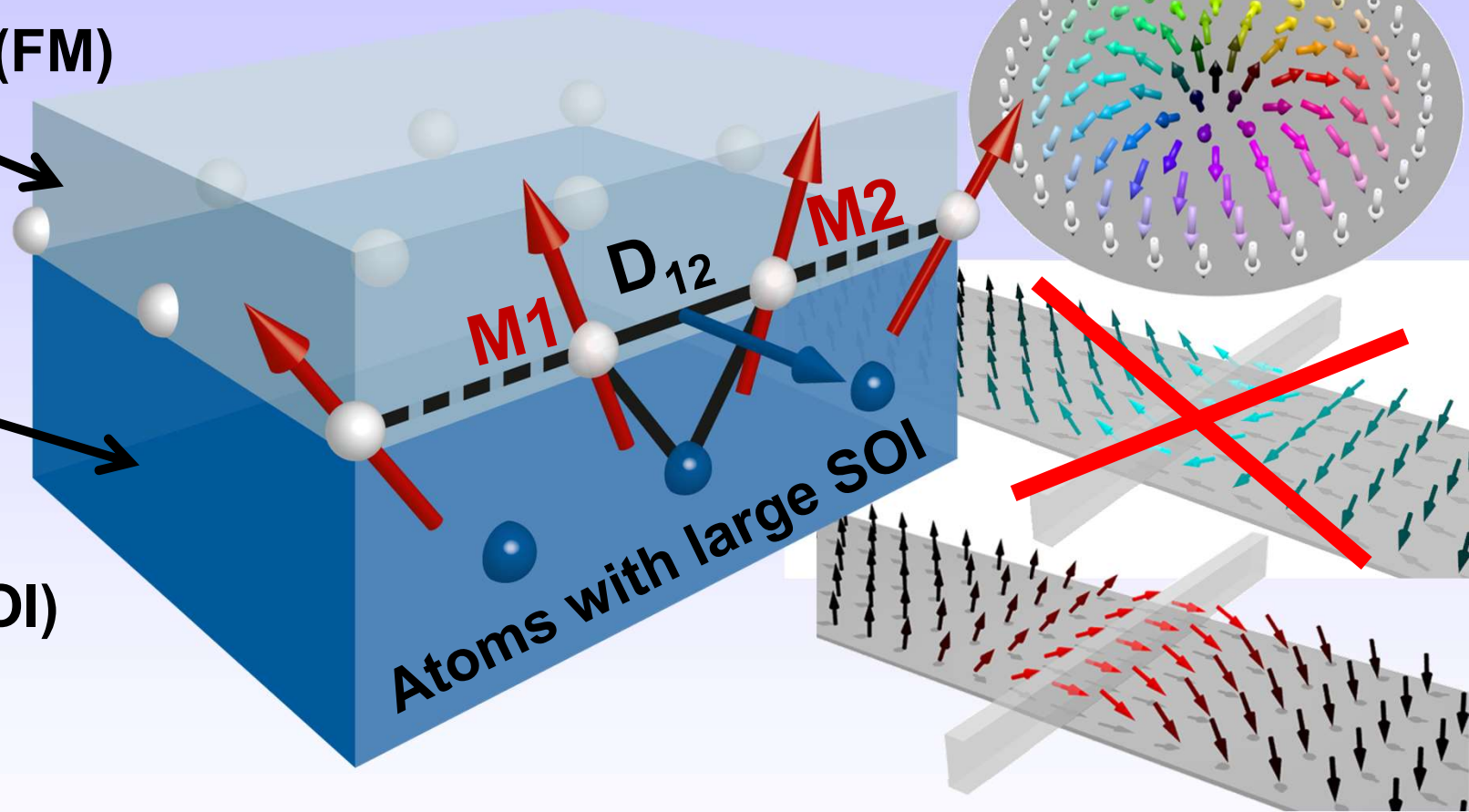
- Heisenberg exchange interaction sets the magnetic ordering.
- However many energetically degenerate spin structures can be stabilized → spin structures do not have a set chirality.

0. Chiral exchange coupling – Dzyaloshinskii-Moriya interaction

Chiral exchange coupling mediated by **Spin-Orbit** interaction

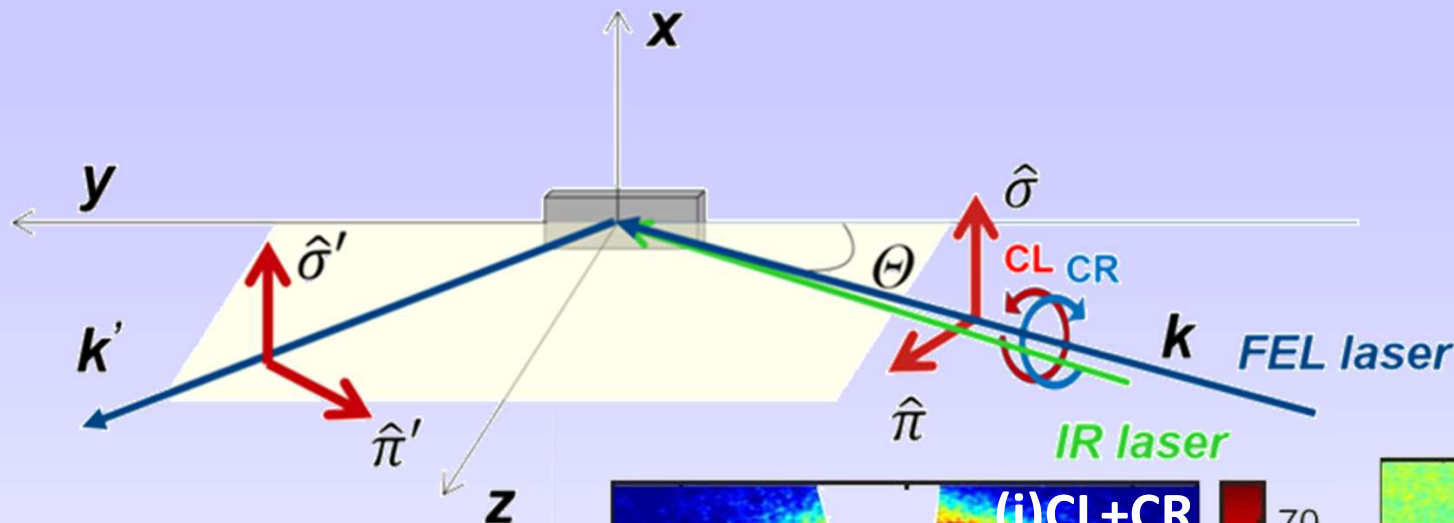
Ferromagnet (FM)

Heavy Metal Layer (HL) with large spin-orbit interaction (SOI)

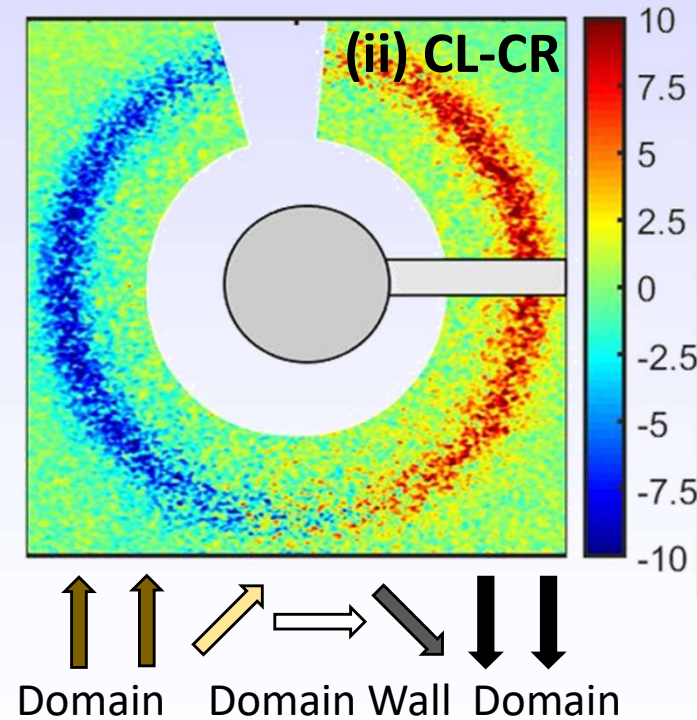
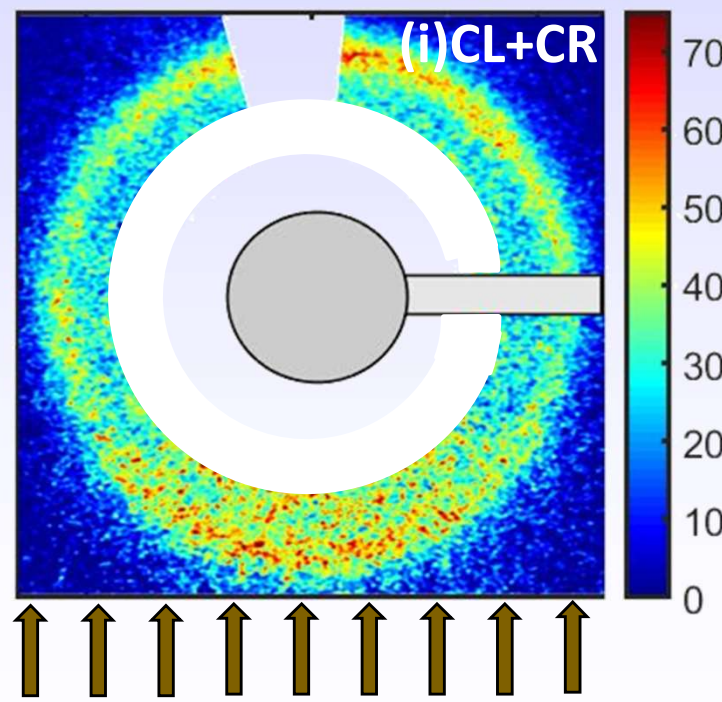
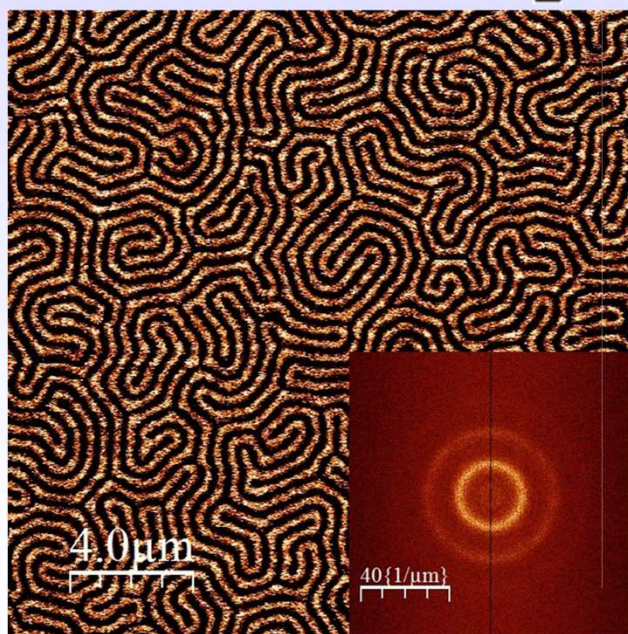


- Two spins in the ferromagnet are coupled via an atom with large SOI in a heavy metal layer $\rightarrow$ Dzyaloshinskii-Moriya interaction (DMI)
- Favours a spin canting with defined chirality $\rightarrow$ Chiral Domain Walls!

0. Chiral exchange coupling – ultra-fast spin-orbitronics



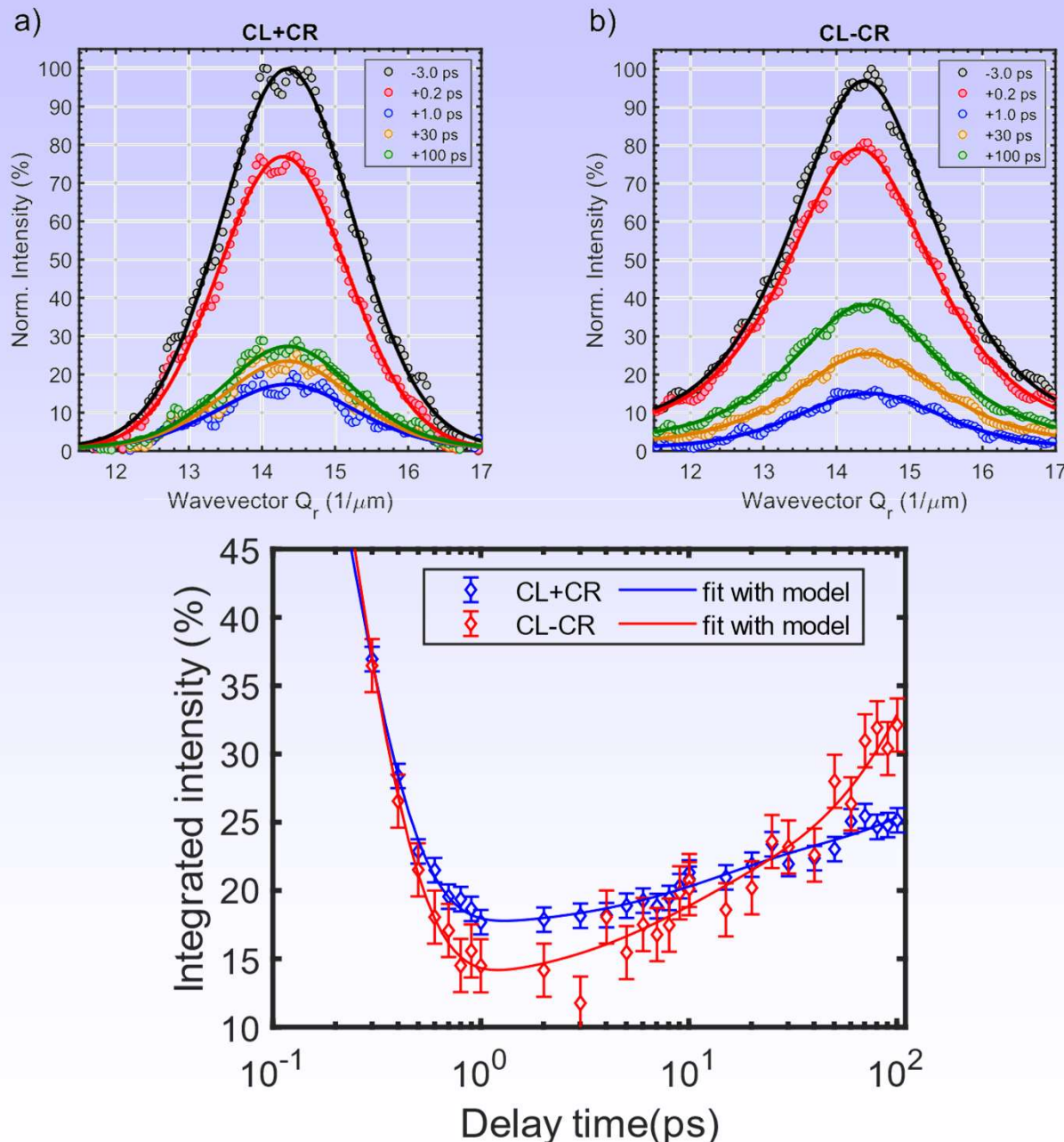
fs-time-resolved
small angle
x-ray scattering
@FERMI Free
Electron Laser



Domain Domain Wall Domain

- Time evolution of (i) collinear order in domains and (ii) chiral order in DWs

0. Chiral exchange coupling – ultra-fast spin-orbitronics

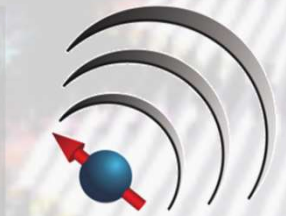


- “Dechiralisation” of chiral domain walls: **same timescale** as “demagnetization” of the collinear domains.
- **Faster** recovery of **chiral** magnetic order than collinear magnetic order
- → Chiral magnetic order more robust!
→ enhanced stability of chiral spin structures !

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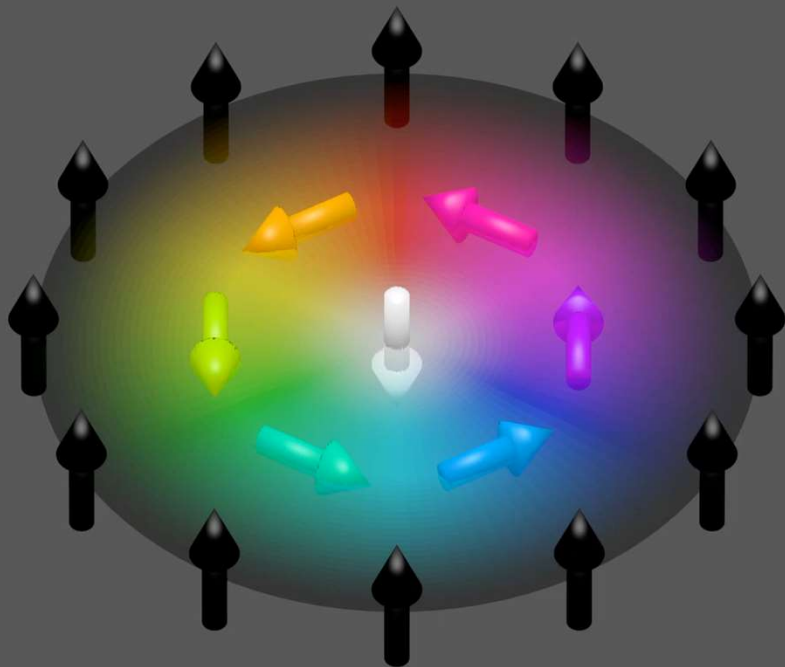
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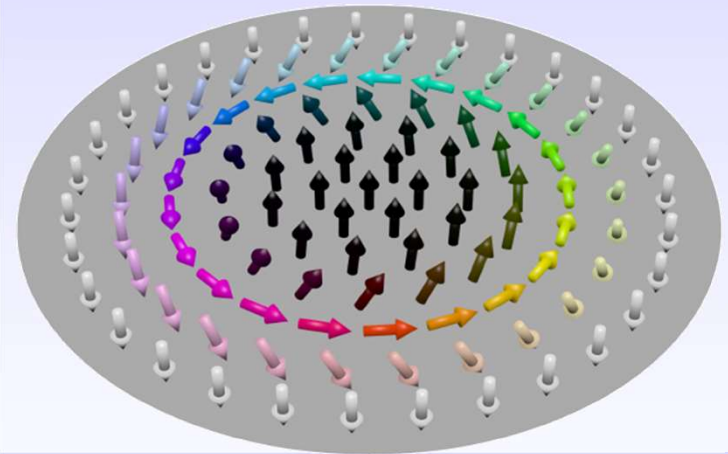
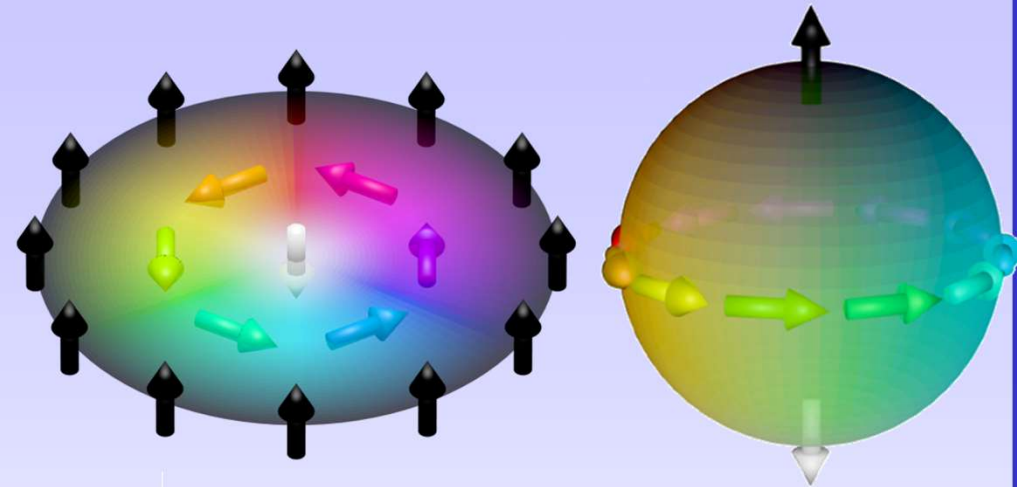


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1. Topological Skyrmion Spin Structures in high-anisotropy materials



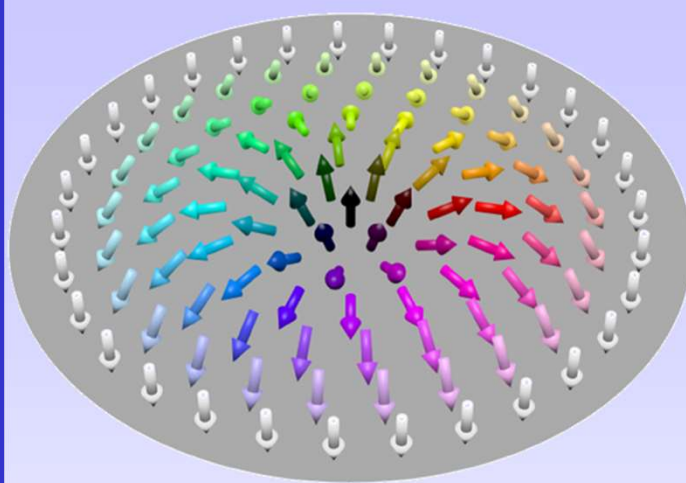
F. Büttner



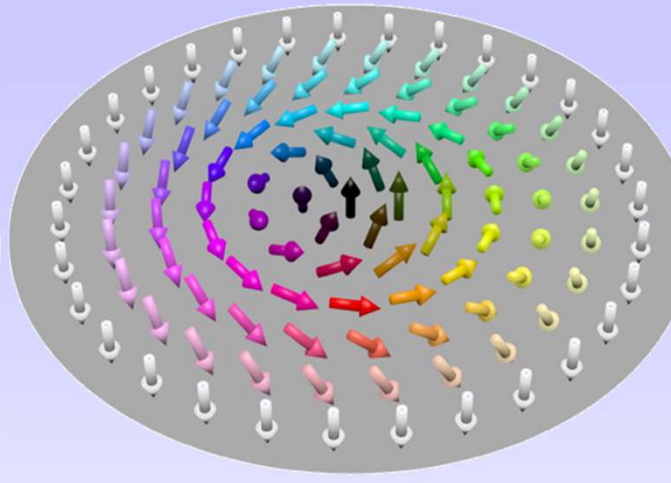
- Skyrmions are vector fields that can be continuously deformed into a sphere.
- For appropriately designed DMI, exchange, anisotropy, saturation magnetization, skyrmion spin structures can be stabilized as metastable states or ground states.

U. Rößler et al., *Nature* **442**, 797 (2006); S. Mühlbauer *et al.* *Science* **323**, 915–919 (2009); X. Yu, *et al.* *Nature* **465**, 901 (2010); S. Seki et al., *Science* **336**, 198 (2012); A. Nayak et al., *Nature* **561**, 548 (2017); Heinze *et al.*, *Nat. Phys.* **7**, 713 (2011); N. Romming et al., *Science* **341**, 636 (2013); A. Malozemoff et al., *Magnetic DWs in Bubble Materials*, Ac. Press (1979)

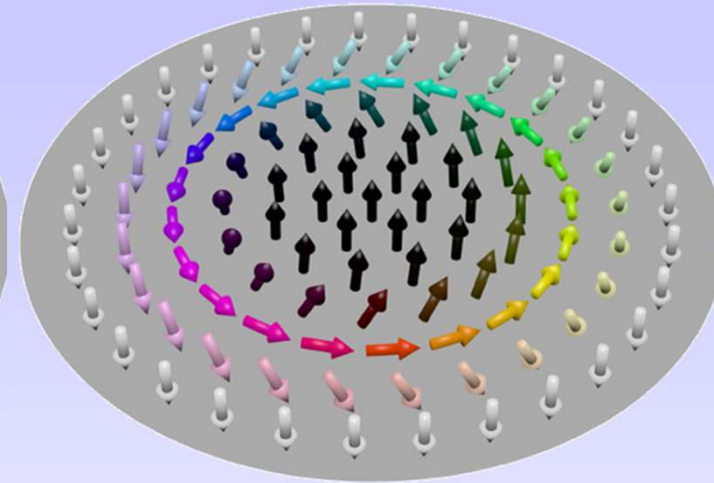
1. Spin Structures stabilized by the chiral DMI



Hedgehog skyrmion (N=1)



Chiral skyrmion (N=1)



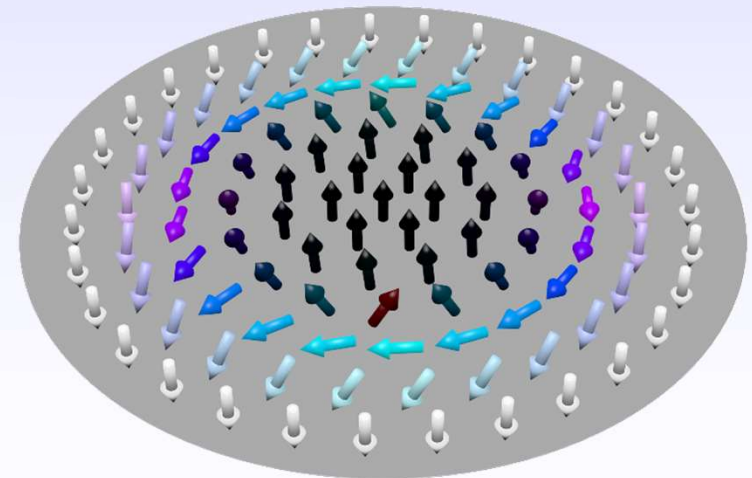
Bubble skyrmion (N=1)

- Hedgehog skyrmion is not stable without DMI with in-plane $\mathbf{D}_{12}$.
- Topology of an object is characterized by its winding number¹:

$$N = (8\pi)^{-1} \int dx dy n$$

With the topological density n :

$$n = \epsilon_{\mu\nu} (\partial_\mu \mathbf{m} \times \partial_\nu \mathbf{m}) \cdot \mathbf{m}.$$

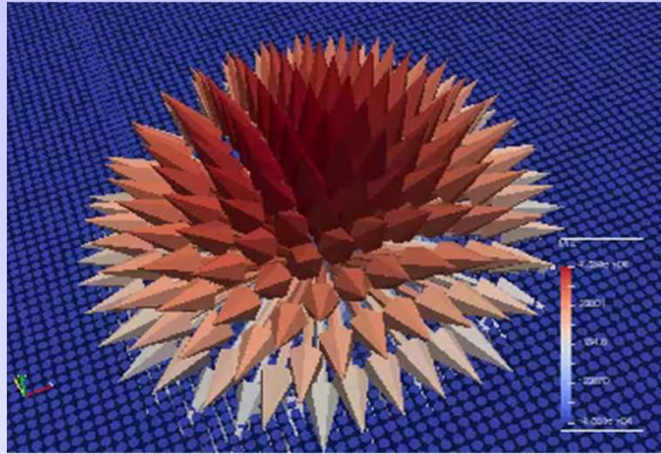


Bubble Skyrmion (N=0)

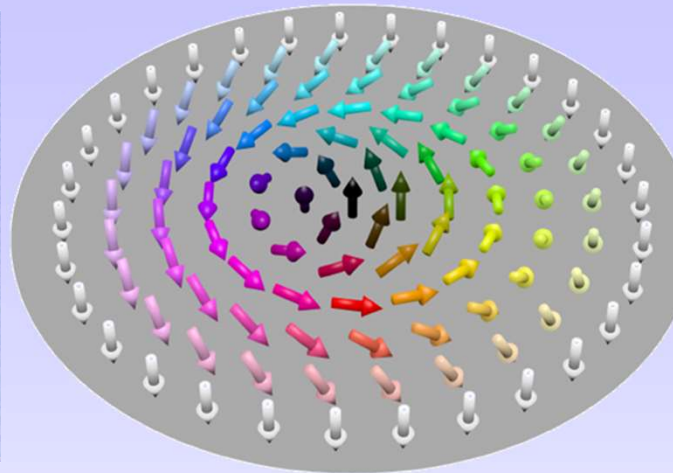


¹N. Papanicolaou et al., Nuclear Physics B 360, 425–462 (1991)
F. Büttner, MK et al., Nature Phys. **11**, 225 (2015)

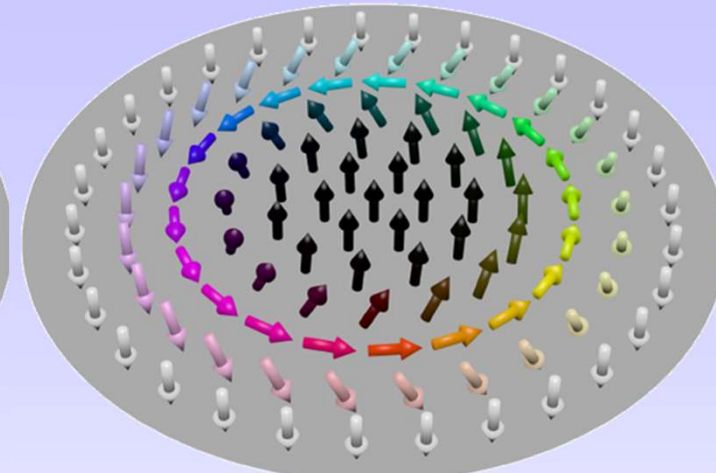
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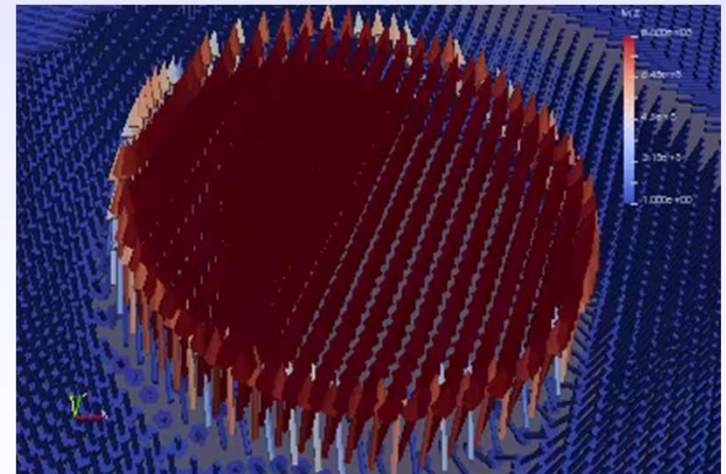
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- Skyrmion with $N=0$ (topology of uniform state) is less stable than $N=1$.



Bubble Skyrmion (N=0)

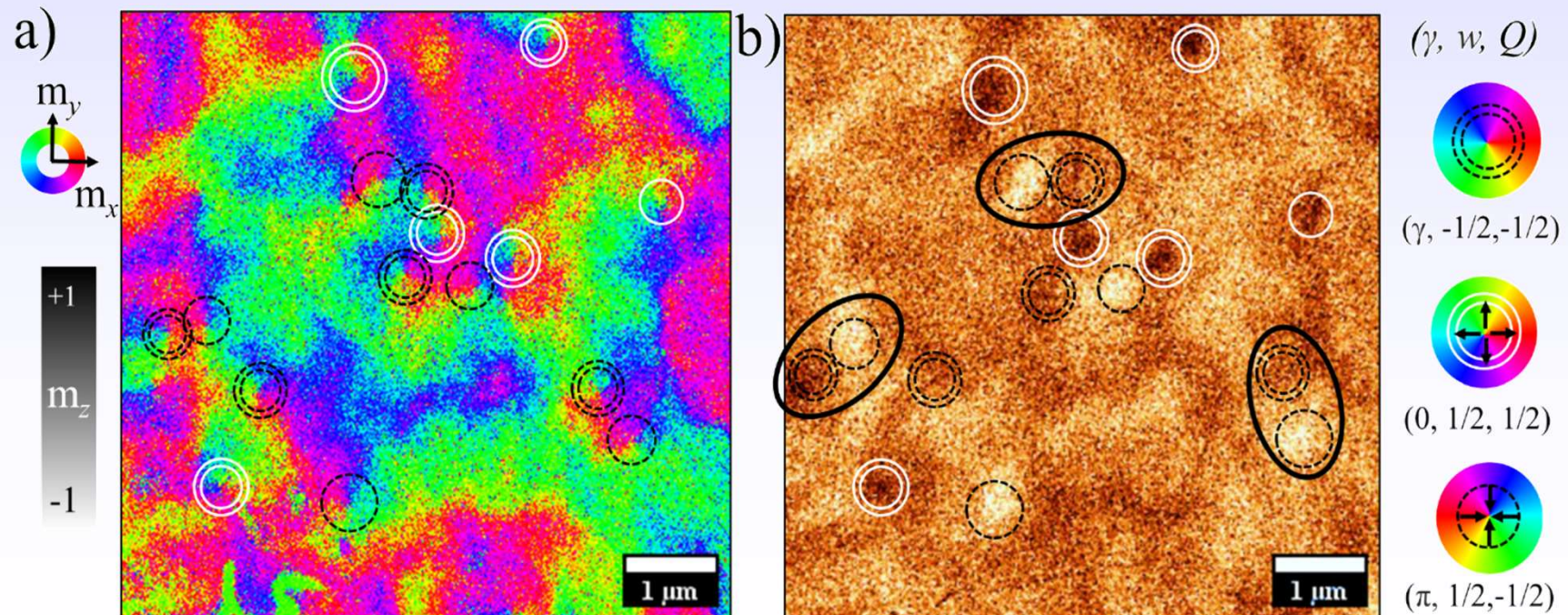
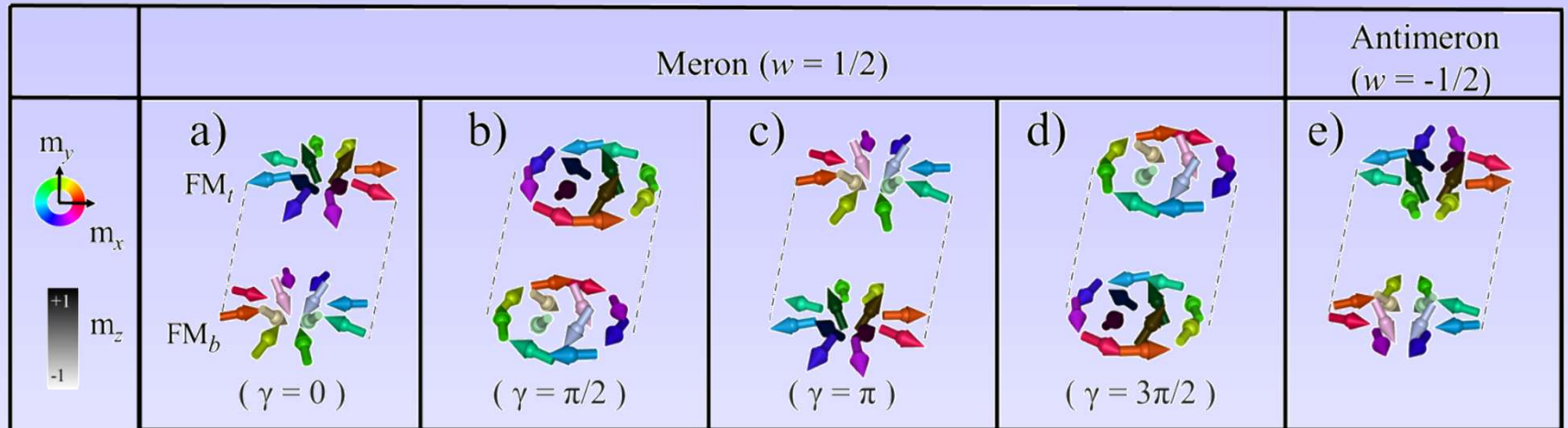


¹N. Papanicolaou et al., Nuclear Physics B 360, 425–462 (1991)
F. Büttner, MK et al., Nature Phys. **11**, 225 (2015)

2. Bimerons in synthetic antiferromagnets

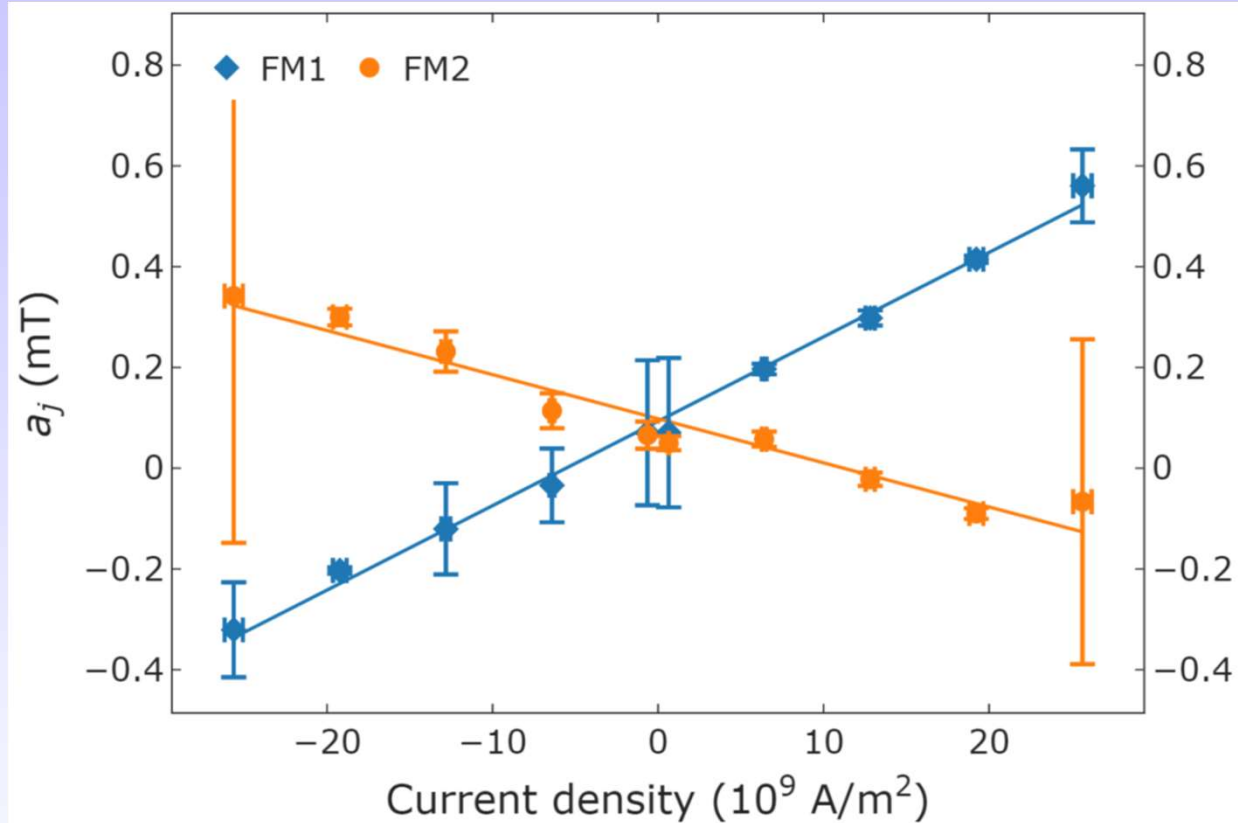
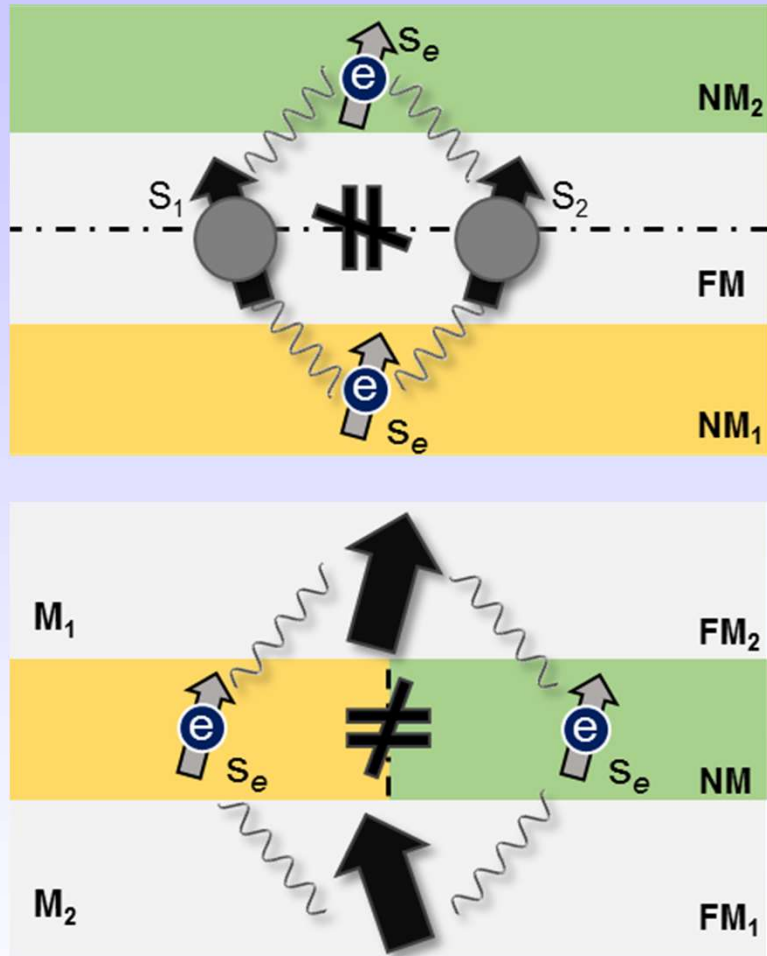
- In multi-layers: Different merons can be stabilized

- Observation using combine: SEMPA + MFM¹



¹ M. Bhukta, MK et al., arxiv:2303:14853

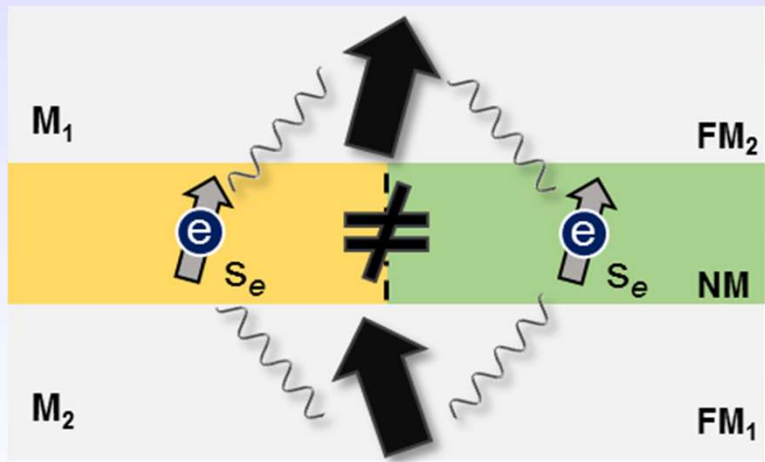
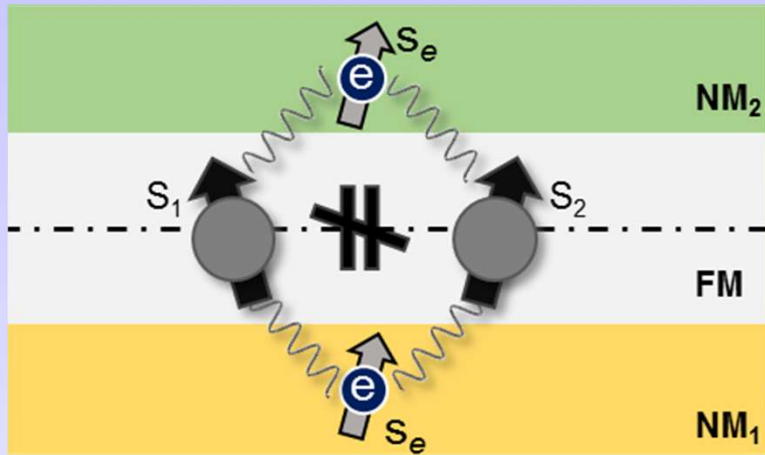
2. Chiral interlayer exchange coupling



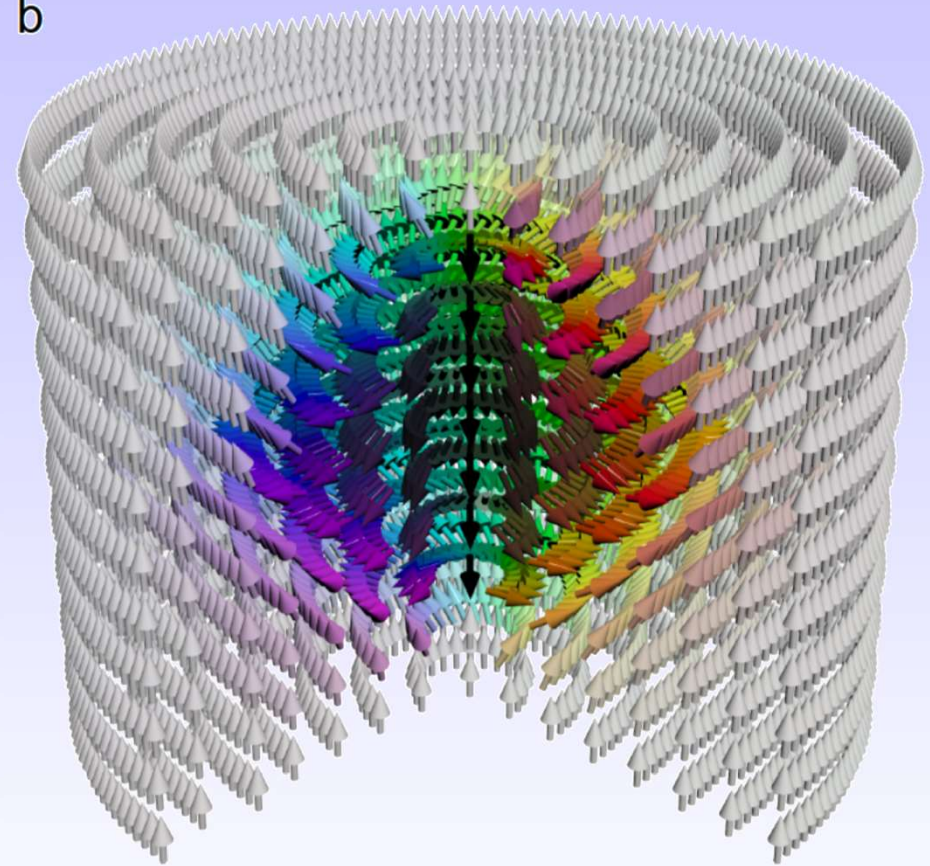
- Two spins in 2 magnetic layers are coupled by interlayer RKKY
- Chiral antisymmetric interlayer exchange coupling $\rightarrow$ RKKY-DMI¹
- Strength of RKKY-DMI can be tuned by currents on-the-fly!²

¹D. Han, MK et al., Nat. Mat. **18**, 703 (2019); ²F. Kammerbauer, MK et al., arxiv:2209.01450 (Nano Lett. 2023)

2. Chiral **interlayer** exchange coupling – 3D skyrmion structures



b

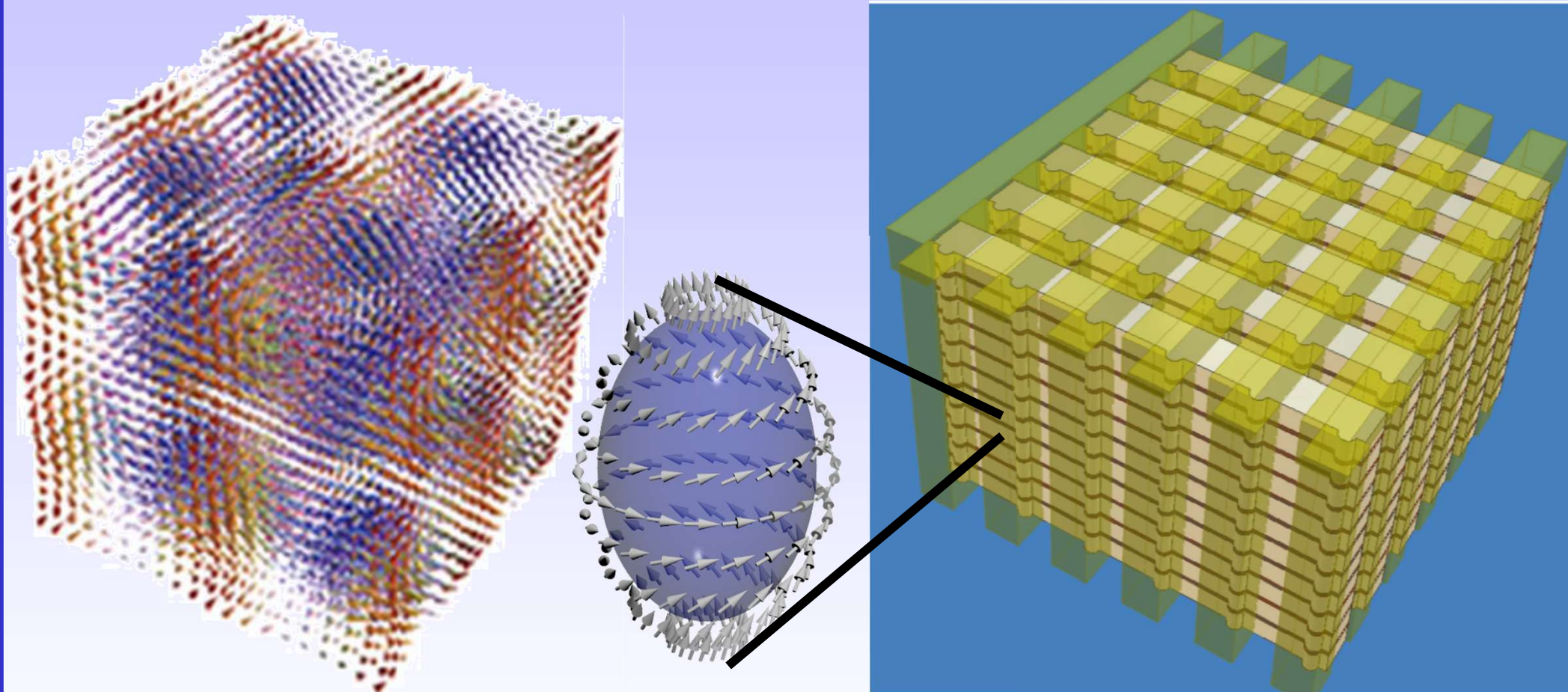


Courtesy N. Kiselev

- Two spins in 2 magnetic layers are coupled by interlayer RKKY
- Recently we found a chiral antisymmetric interlayer exchange coupling:
→ RKKY-DMI¹ stabilizes three-dimensional spin structures!

¹D. Han, MK et al., Nat. Mat. **18**, 703 (2019); see also A. Fernandez-Pacheco et al., Nat. Mat. **18**, 679 (2019)

2. 3D skyrmion structures – interconnectivity in 3D space



¹T. Tanigaki et al., Nano Lett. 15, 5438 (2015)

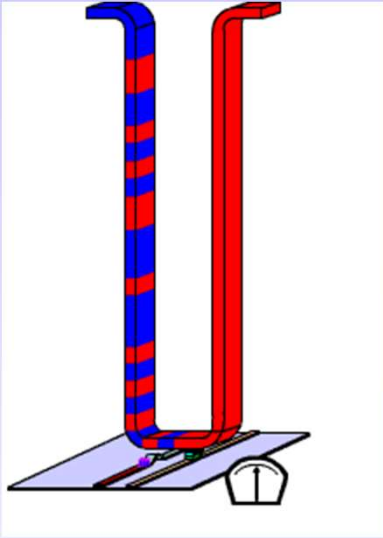
Courtesy R. Cowburn

- Claimed observation of a 3D lattice of 3D skyrmions¹
- Possible 3D interconnects → move 3D particles in all directions in space → realize (potentially) the huge interconnectivity of neurons in 3D!²

²D. Han, MK et al., Nature Materials **18**, 703 (2019)

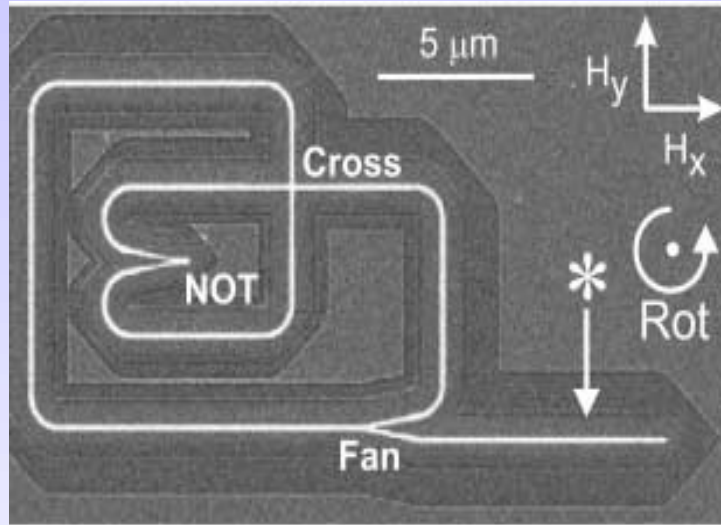
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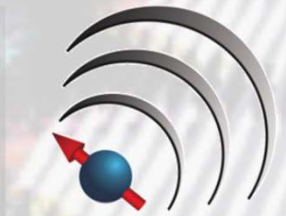
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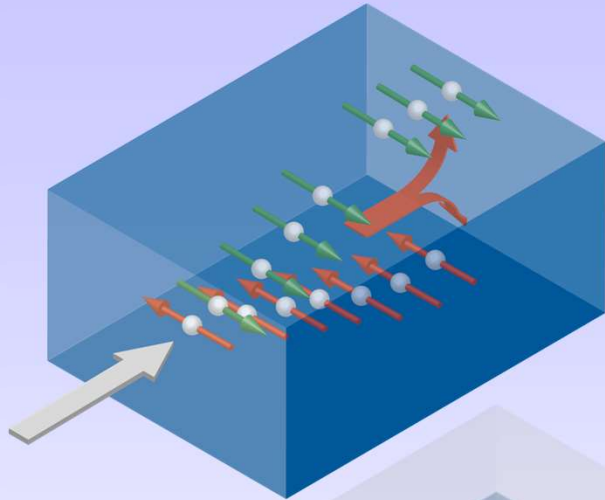
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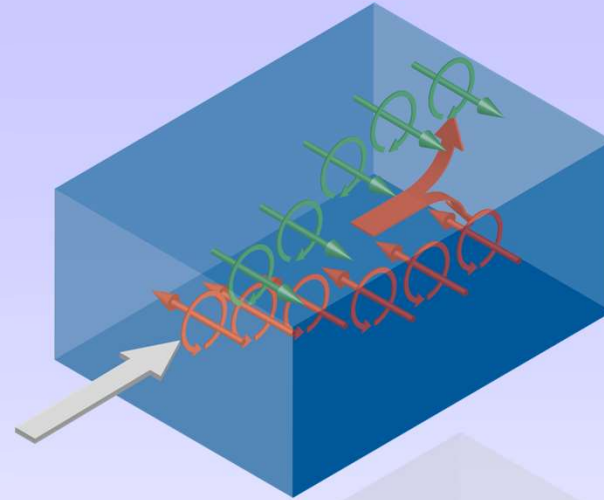
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3. Spin-, Orbit- and Spin-Orbit Torques



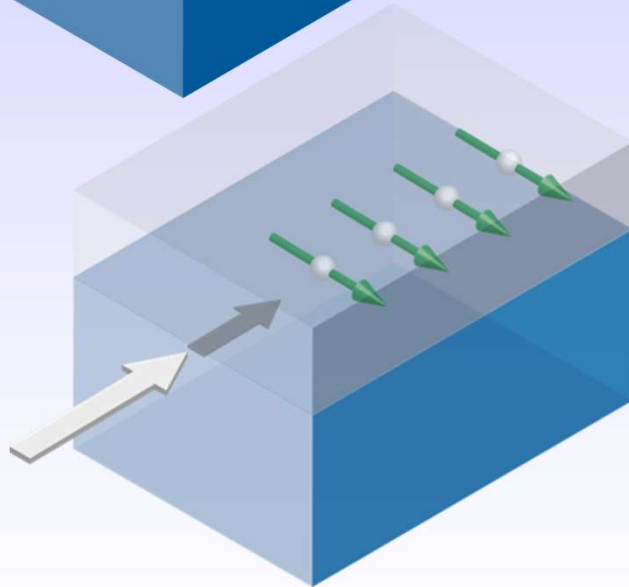
Spin Hall Effect

Rev. Mod. Phys. **87**, 1213 (2015)



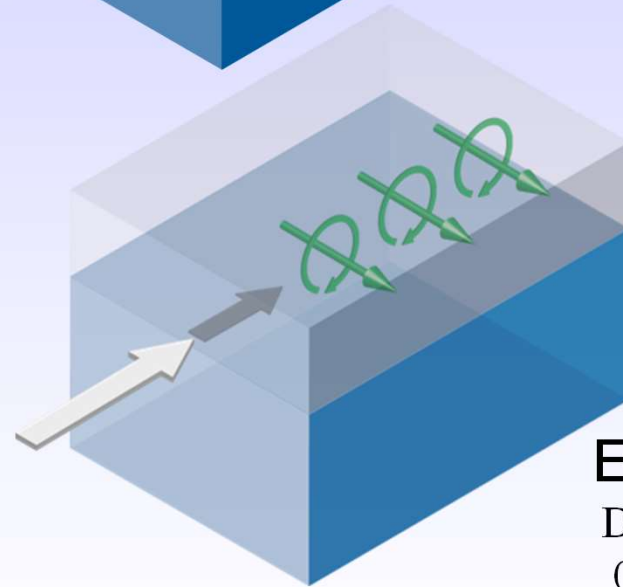
Orbital Hall Effect

H. Kontani et al., PRL **102**, 016601 (2009)



Inverse Spin Galvanic Effect / Rashba Edelstein Effect

PRL **112**, 096601 (2014)

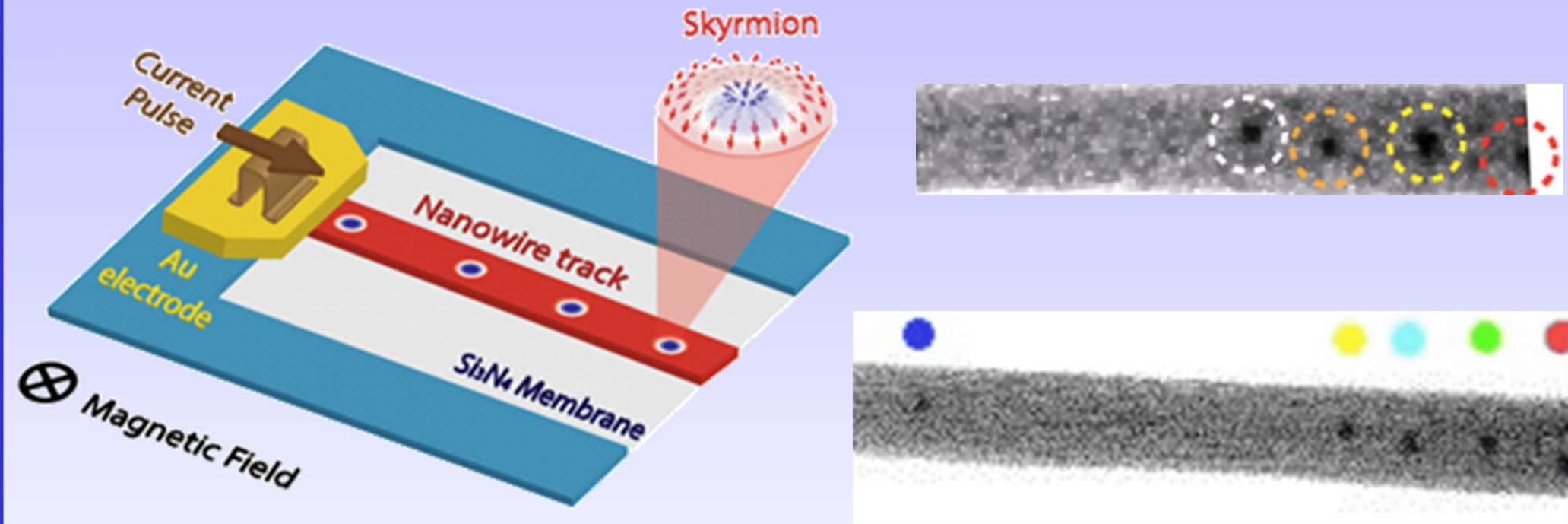


Orbital Rashba Edelstein Effect

D. Go et al., PRL **121**, 086602 (2018)

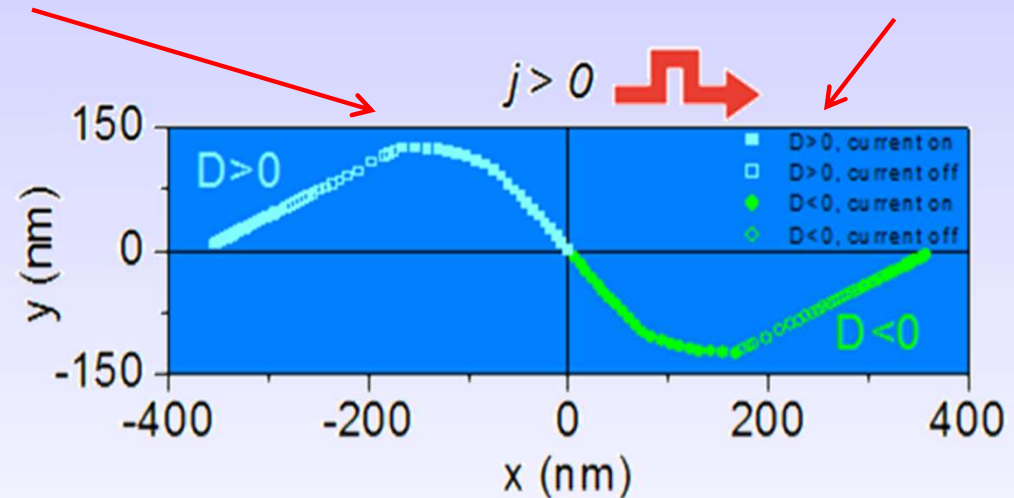
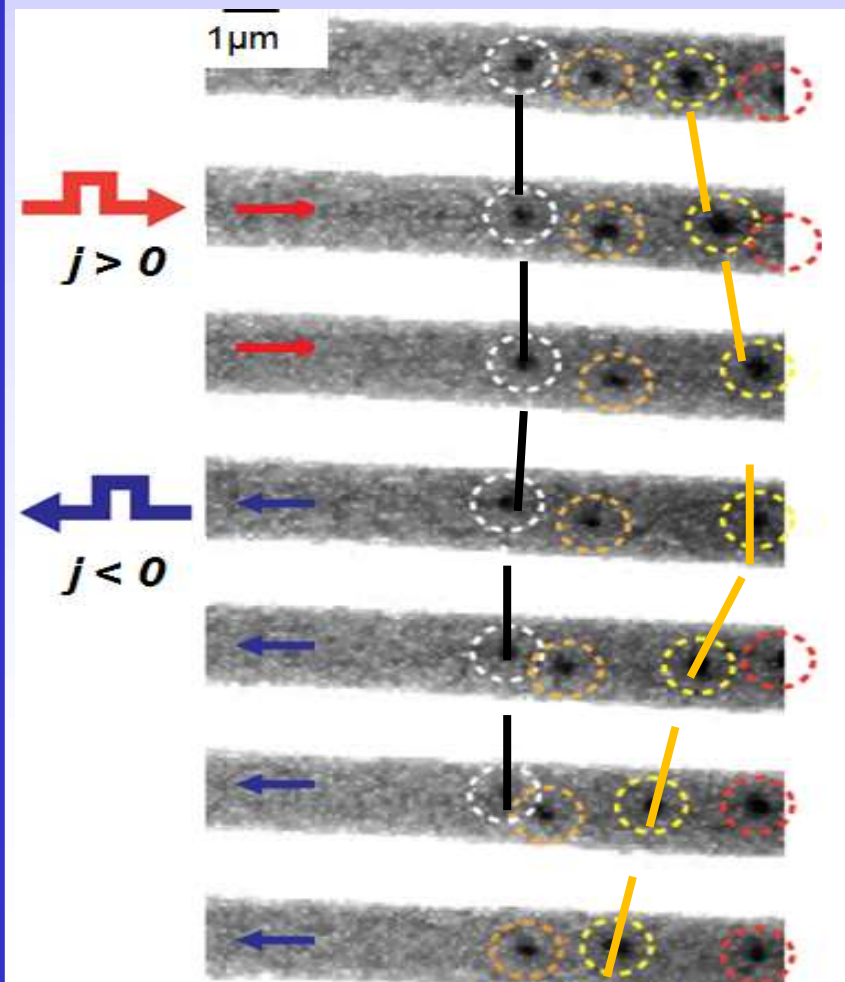
- Dynamics induced by spin-orbit torques due to SHE (a) and ISGE/REE (b),
- Additionally orbital angular momentum: Orbital Hall Effect (OHE) (c) [1] & Orbital Rashba Edelstein Effect (OREE) (d) [2].

3. Skyrmion Racetrack



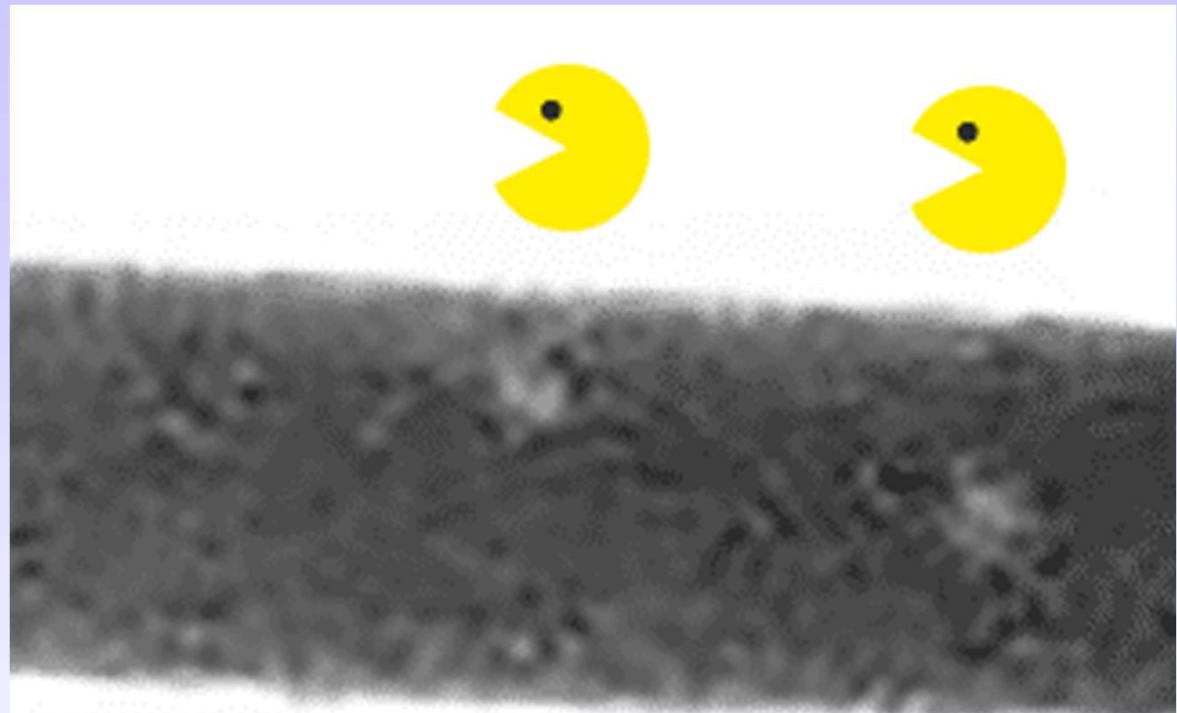
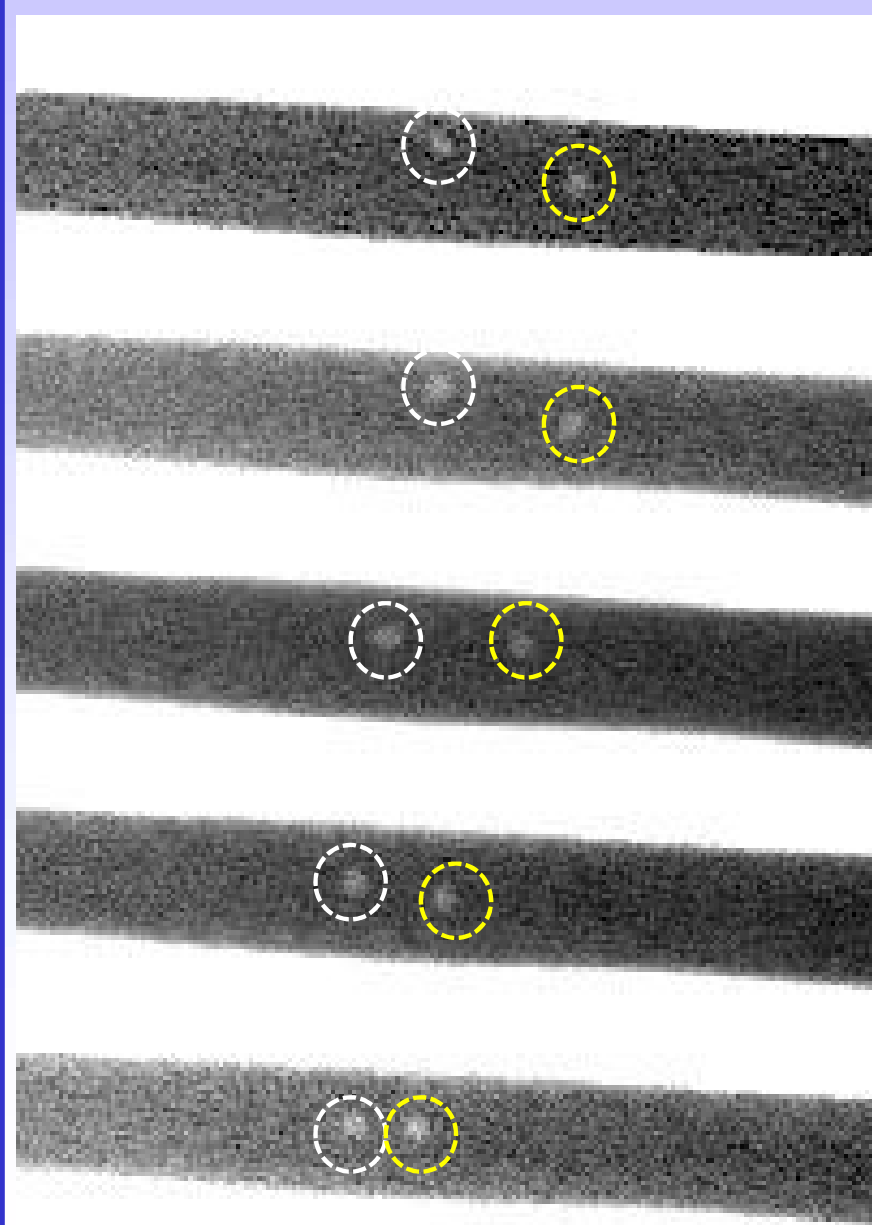
- Skyrmion racetrack¹: advantages compared to a DW-based racetrack: total magnetization does not change with skyrmion motion
→ less susceptible to stray fields.
- Topological protection of skyrmions → more reliable motion?
- Nanowire is patterned out of Pt/Co/Ta (μm width)²
- Single skyrmions can be moved by spin orbit torques on the nano-track³

3. Skyrmion Racetrack



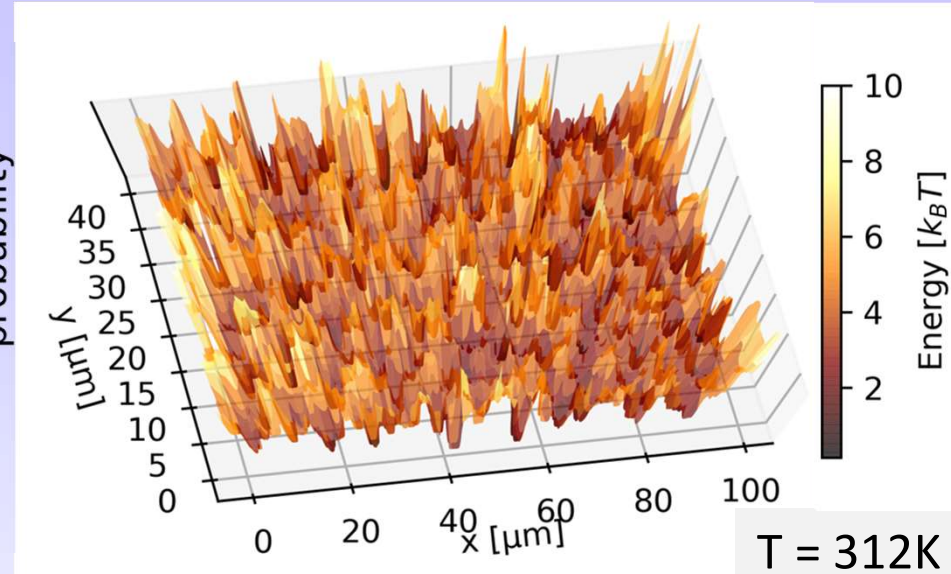
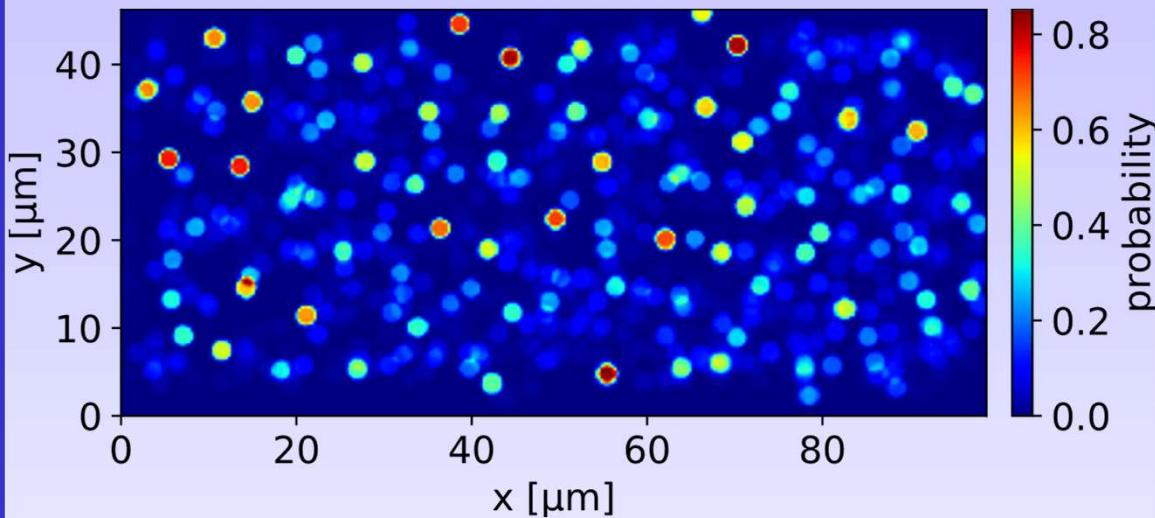
- Simulations show that skyrmions move synchronously on a complex trajectory.
- DMI and current set the motion direction.
- In the experiment skyrmions move at different velocities and can be pinned.

3. Skyrmion Racetrack - Stability



- Simulations show that skyrmions move synchronously on a complex trajectory.
- DMI and current set the motion direction.
- In the experiment skyrmions move at different velocities and can be pinned.
- Only pinned skyrmions can be annihilated!

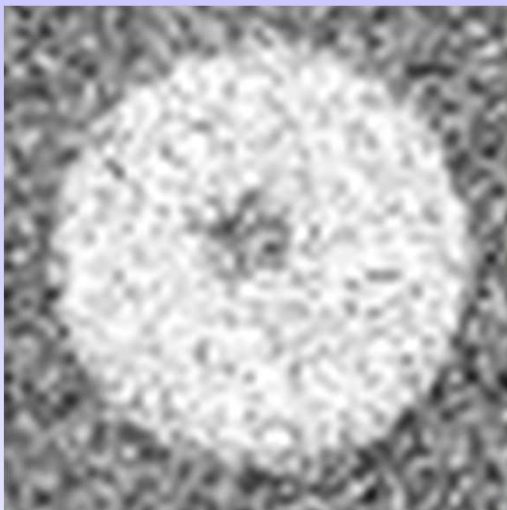
3. Origin of pinning



- Measure pinning and depinning of skyrmions
 - Determine probability of finding skyrmions at a certain position
- Variations due to non-flat energy landscape (pinning sites present)

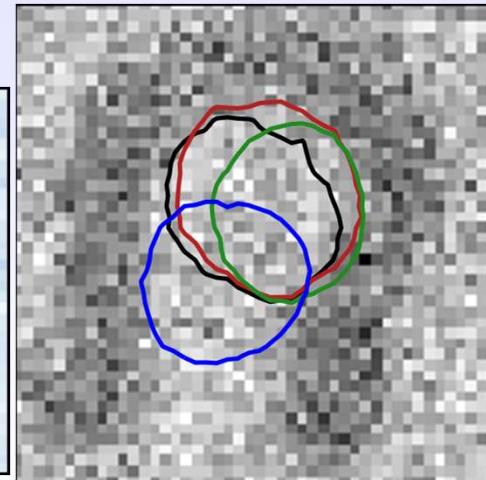
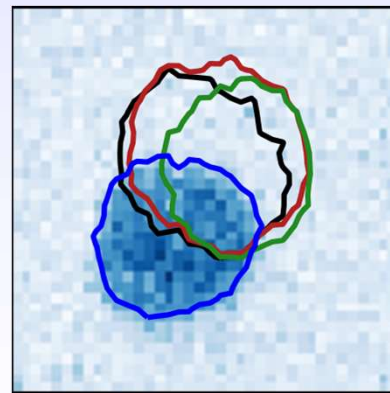
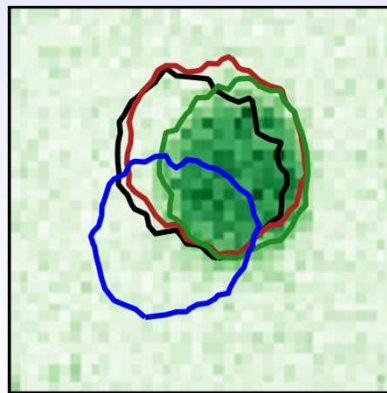
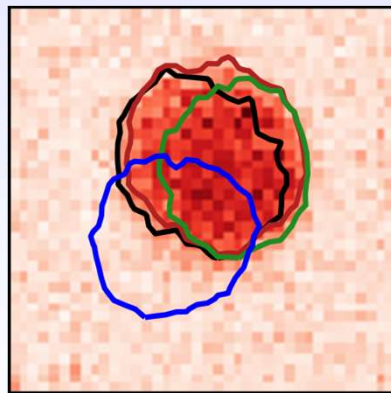
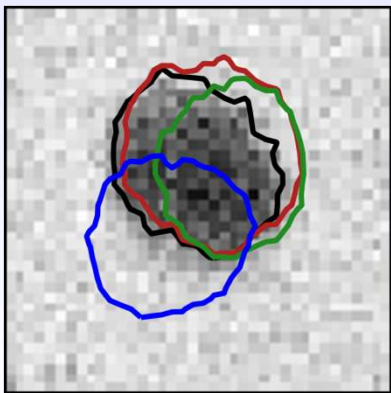
- Use probability density to calculate energy landscape
- Pinning and thermal energy on same scale
- Look at specific pinning site to understand origin:
→ grain boundaries

3. Origin of pinning



10 μm

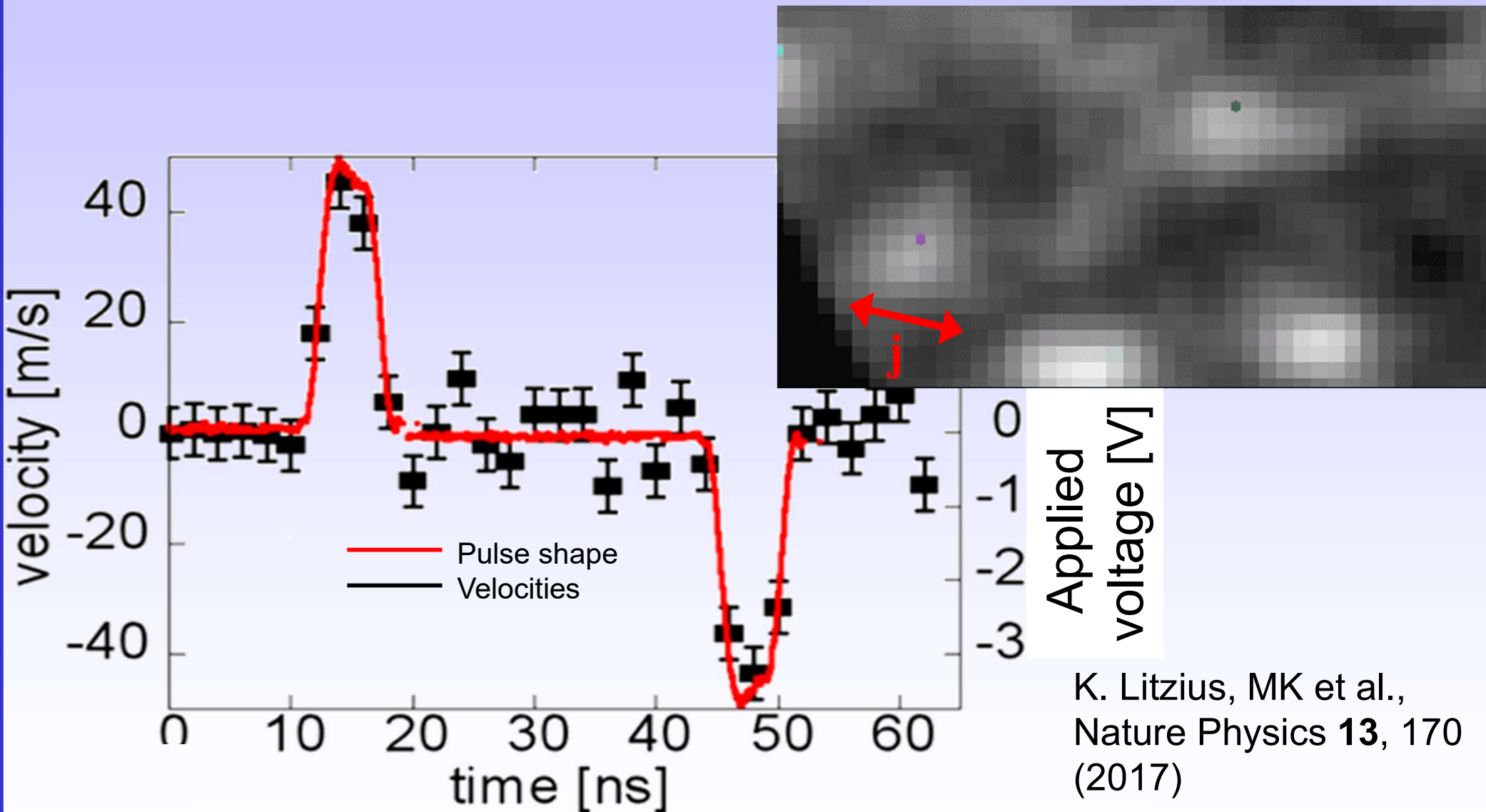
- Single skyrmion moving in confined geometry
- Skyrmion moves between distinct positions
→ obtain statistics to investigate pinning effects
→ Skyrmions are found in characteristic configurations of the domain wall.



5 μm

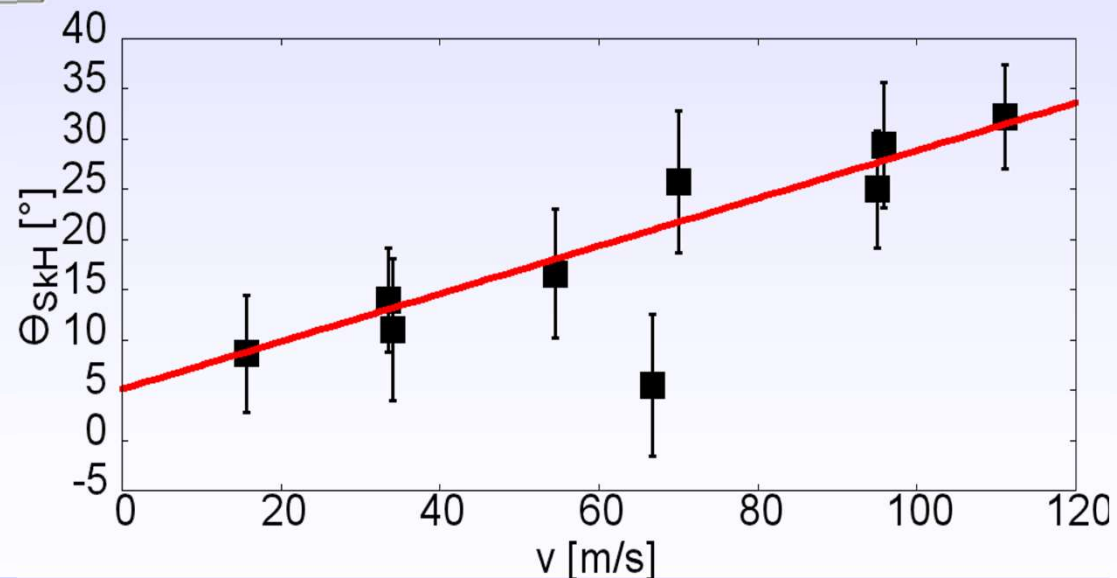
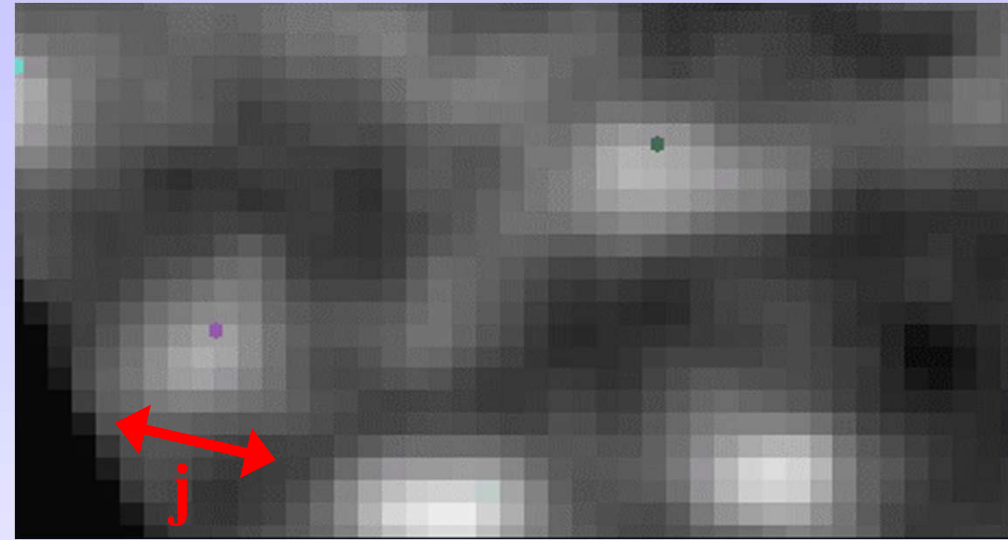
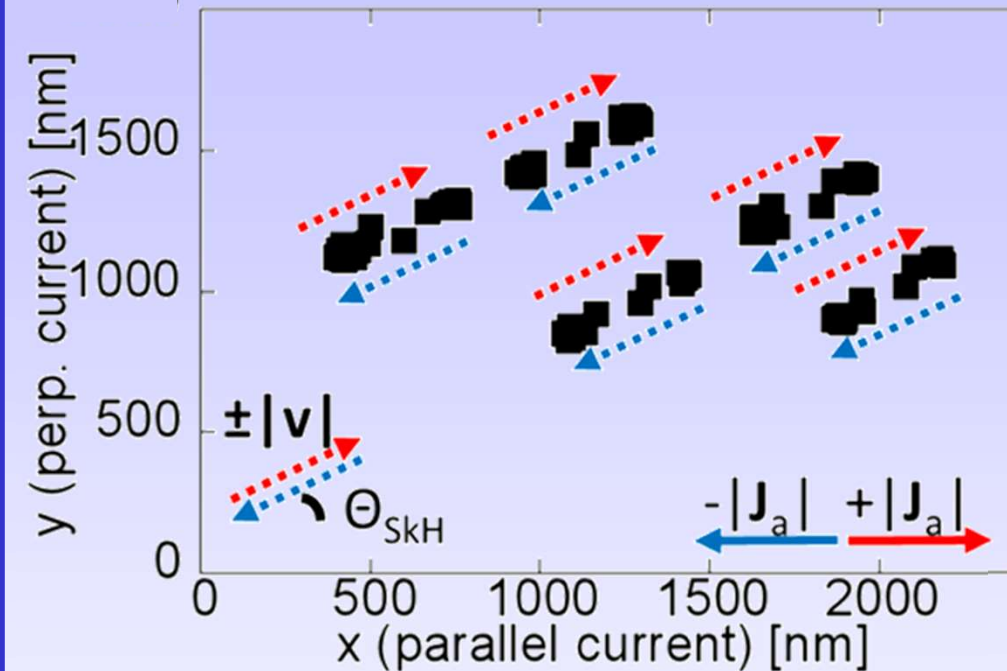
- Pinning of the skyrmion boundary domain wall: confirmed by stripe domain pinning

3. Real time magnetic imaging of spin-orbit torque induced dynamics



- Dynamic imaging enabled by low pinning Pt/CoFeB/MgO → reliability $>10^{10}$ cycles!
- Skyrmions move synchronously at an angle with current flow → skyrmion Hall effect.

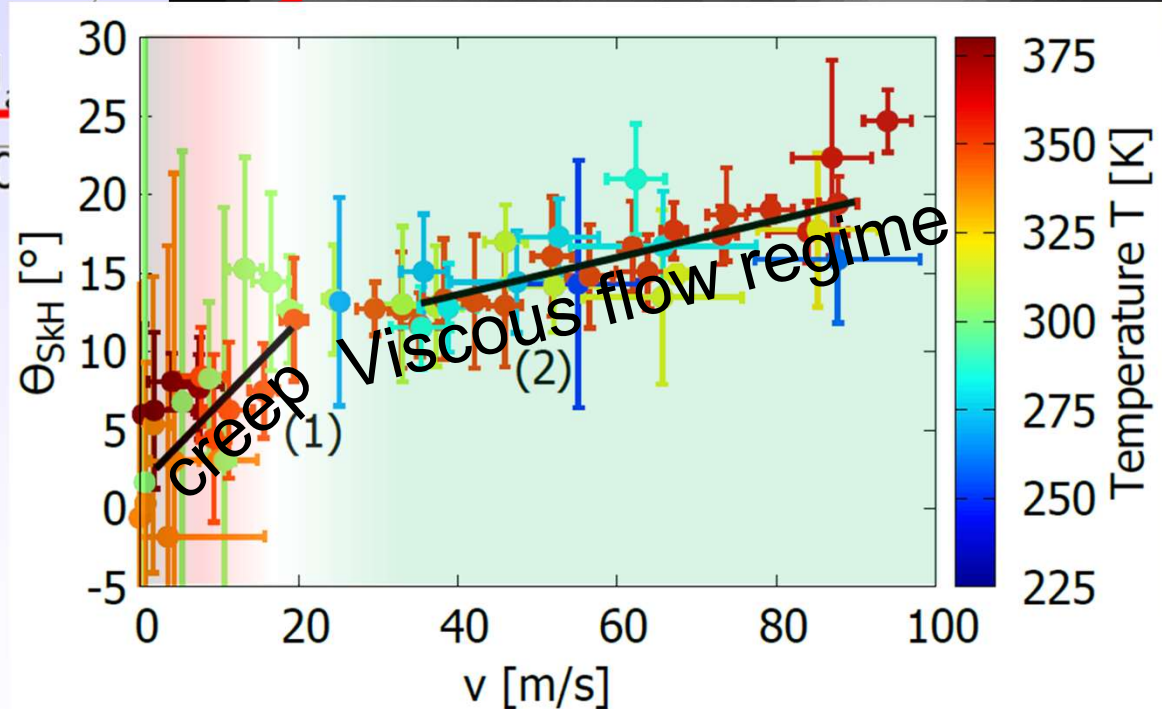
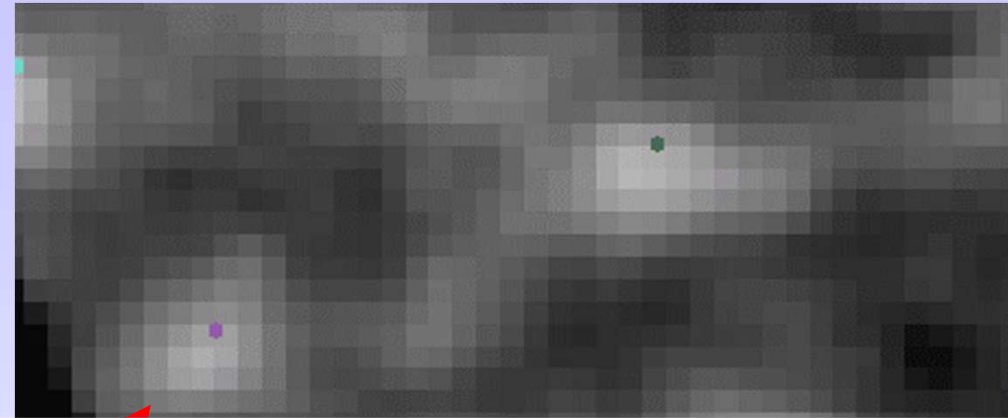
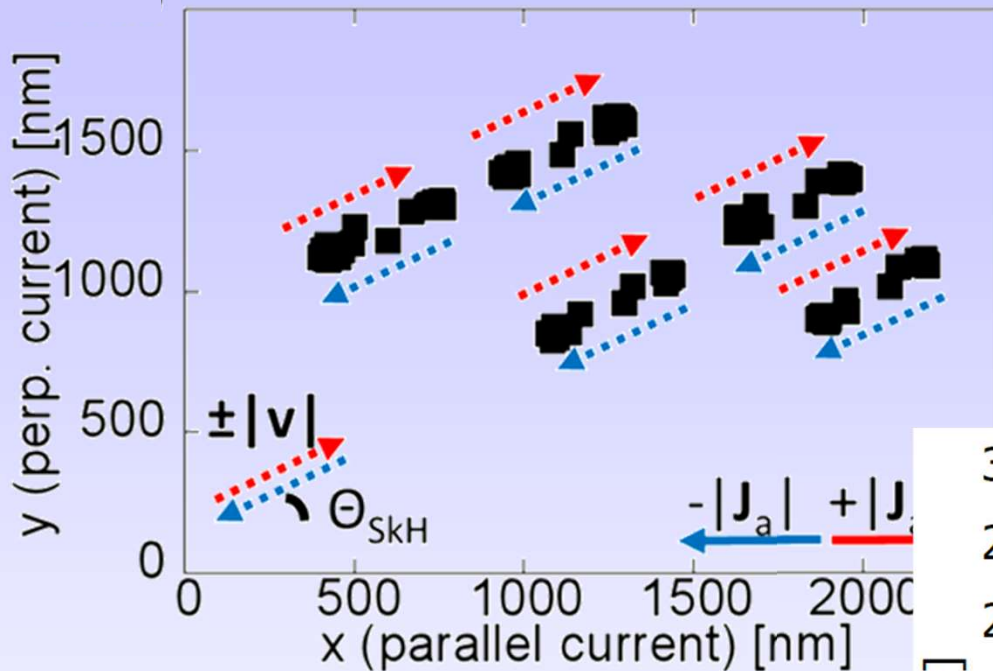
3. Real time magnetic imaging of spin-orbit torque induced dynamics



K. Litzius, MK et al.,
Nature Physics **13**, 170 (2017)
W. Jiang et al.,
Nature Physics **13**, 162 (2017)

- Skyrmion Hall angle (Θ_{SkH} between j and skyrmion direction) scales with velocity
→ Conventional rigid skyrmion model incomplete! → new theory needed!

3. Skyrmion Hall Angle



K. Litzius et al., Nat. Electron. **3**, 30 (2020)

K. Litzius et al., Nat. Phys. **13**, 170 (2017)

W. Jiang et al., Nat. Phys. **13**, 162 (2017)

K. Zeissler et al., Nat. Com. **11**, 428 (2020)

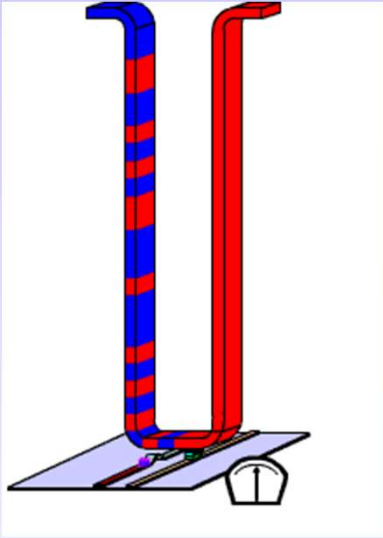
R. Juge et al., PR Appl. **12**, 044007 (2019)

C. Reichhardt et al., Nat. Com. **11**, 738 (2020)

- Skyrmion Hall angle (Θ_{SkH} between j and skyrmion direction) scales with velocity
 → Two different slopes in creep and viscous flow regime → different origins!

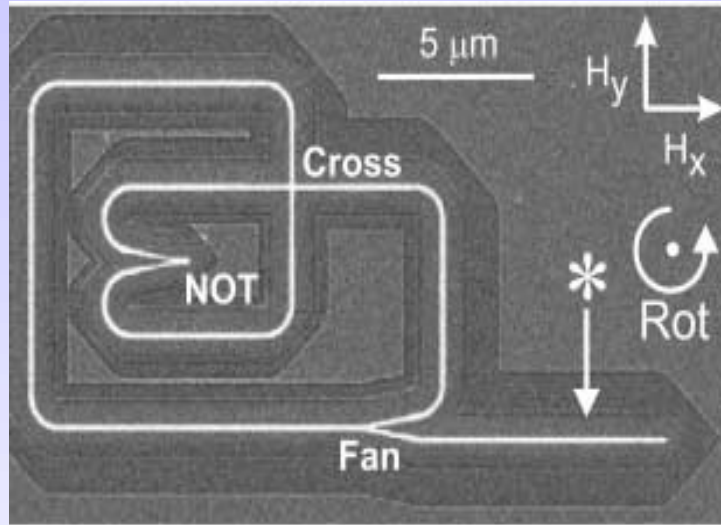
Devices based on Domain Walls and Skyrmions

Memory



Parkin et al, Science **320**, 190 ('08)
Fert et al., Nature Nano **8**, 152 ('13)

Magnetic Logic



D. A. Allwood et al., Science **309**, 1688 (2005)
J. Grollier et al., Nature Electron. **3**, 360 (2020)

Position & angle sensors



R. Mattheis et al., IEEE Trans. Magn. **45**, 3792 (2009)
A. Bisig et al., Nature Comm. **4**, 2328 (2013)

Challenges for Spintronics Devices:

Statics: Stability – Long term information retention

→ Topological Spin Structures to the rescue

Dynamics: Manipulation – **Efficiency** and Speed

→ Topological Spin Structures to the rescue



Skyrmions in Spin-Orbitronics & Orbitronics: novel science and applications in memory & non-conventional computing

M. Kläui

Institut für Physik & Materials Science in Mainz
Johannes Gutenberg-Universität Mainz
Centre for Quantum Spintronics, NTNU Trondheim



- Introduction: devices & chiral interactions
- Topologically stabilized Skyrmions
- Fast dynamics: Spin and Orbital Torques
- Efficient dynamics: **thermal diffusion**
- Non-conventional logic with skyrmions

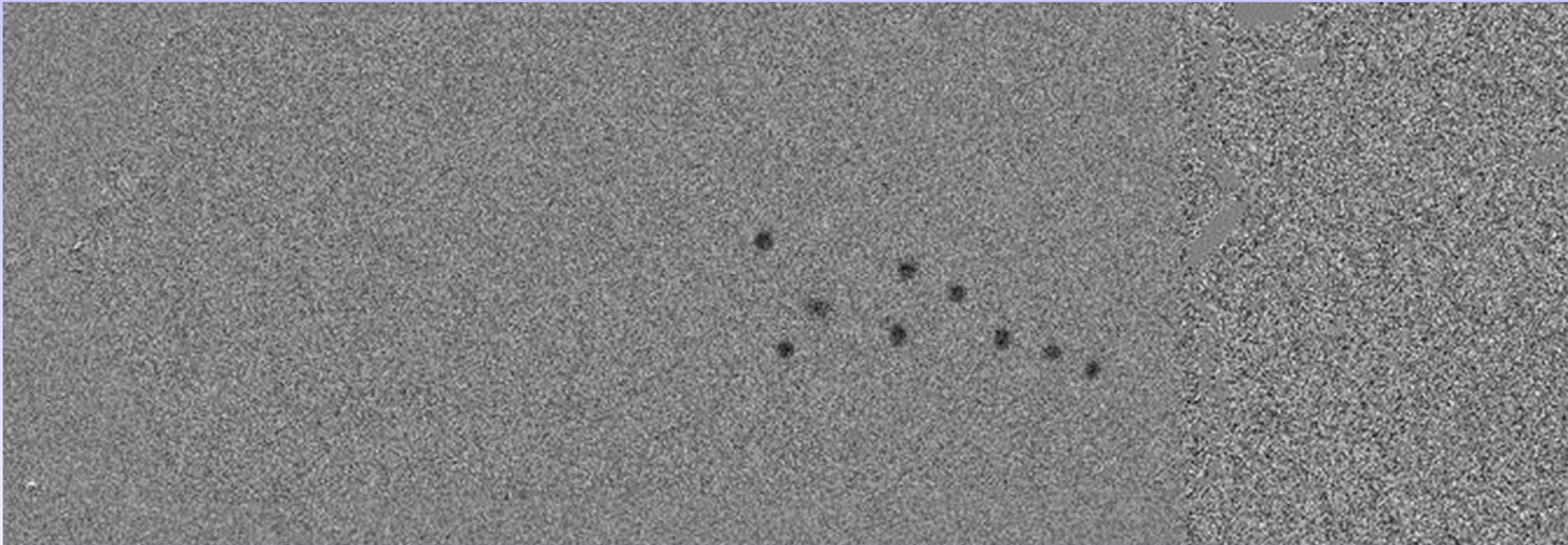
JOHANNES GUTENBERG
UNIVERSITÄT MAINZ

MATERIALS
IN
MAINZ SCIENCE

Qu.
Spin



4. Skyrmion Writing and Skyrmion Motion in low pinning materials



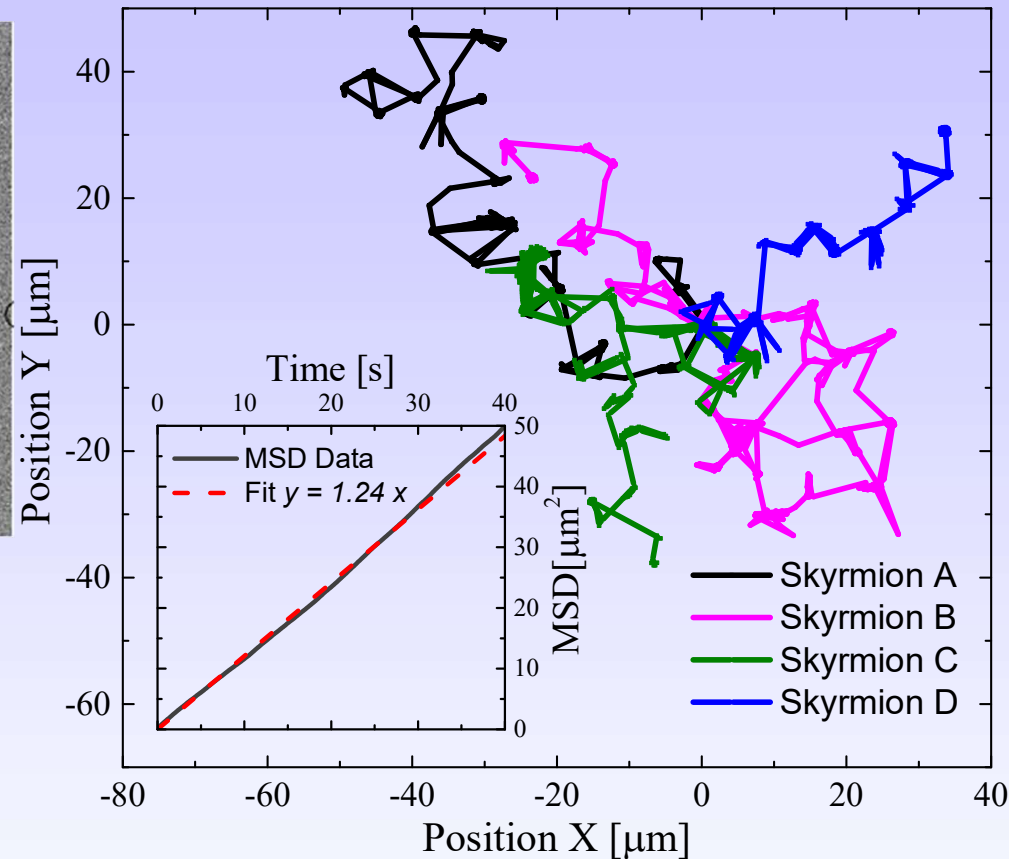
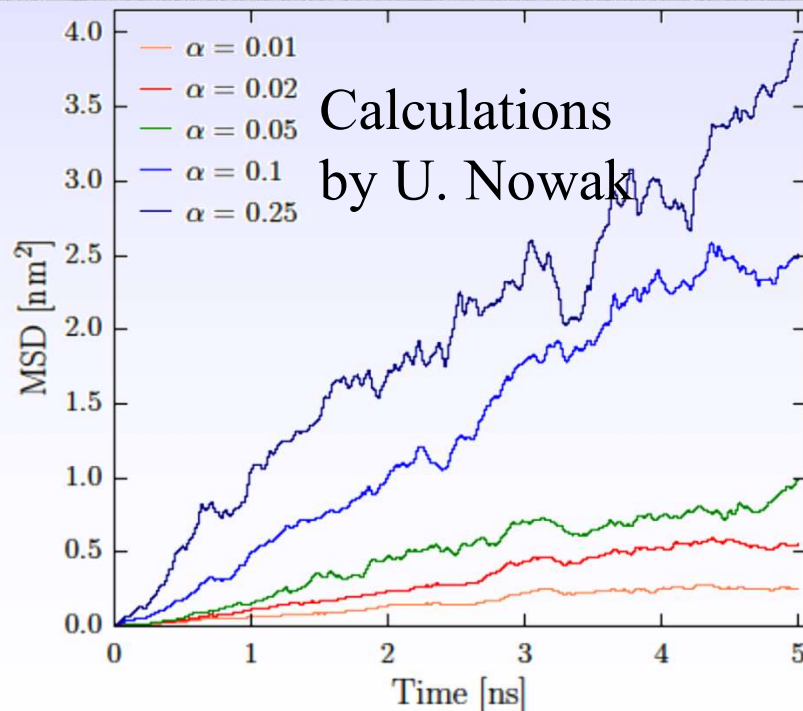
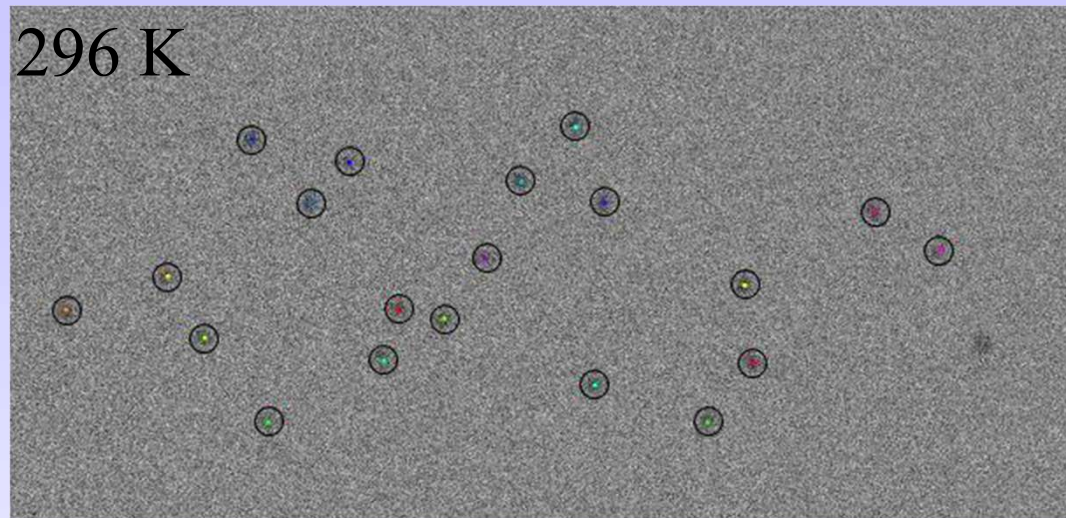
- Ultra-low pinning stack: Ta(5)/CoFeB(1)/Ta(0.08)/MgO(2)/Ta(5)¹
 - Using spin-orbit torques, skyrmions can be produced by pulses „on-demand“²
 - Synchronous displacement along current flow → chiral skyrmions
- In addition to deterministic „writing“ and „shifting“, we see thermally induced dynamics leading to random motion → diffusion? Predicted to be suppressed³

¹G. Yu et al., Nano Lett **16**, 1981 (2016); J. Zazvorka, K. Everschor-Sitte, U. Nowak et al., Nature Nano. **14**, 658 (2019)

²K. Everschor-Sitte et al., NJP **19**, 92001 (2017); M. Stier et al., PRL **118**, 267203 (2017); Z. Wang et al., Nat. El. **3**, 672 (2020)

³C. Schütte et al., Phys. Rev. B **90**, 174434 (2014)

4. Skyrmion Diffusion

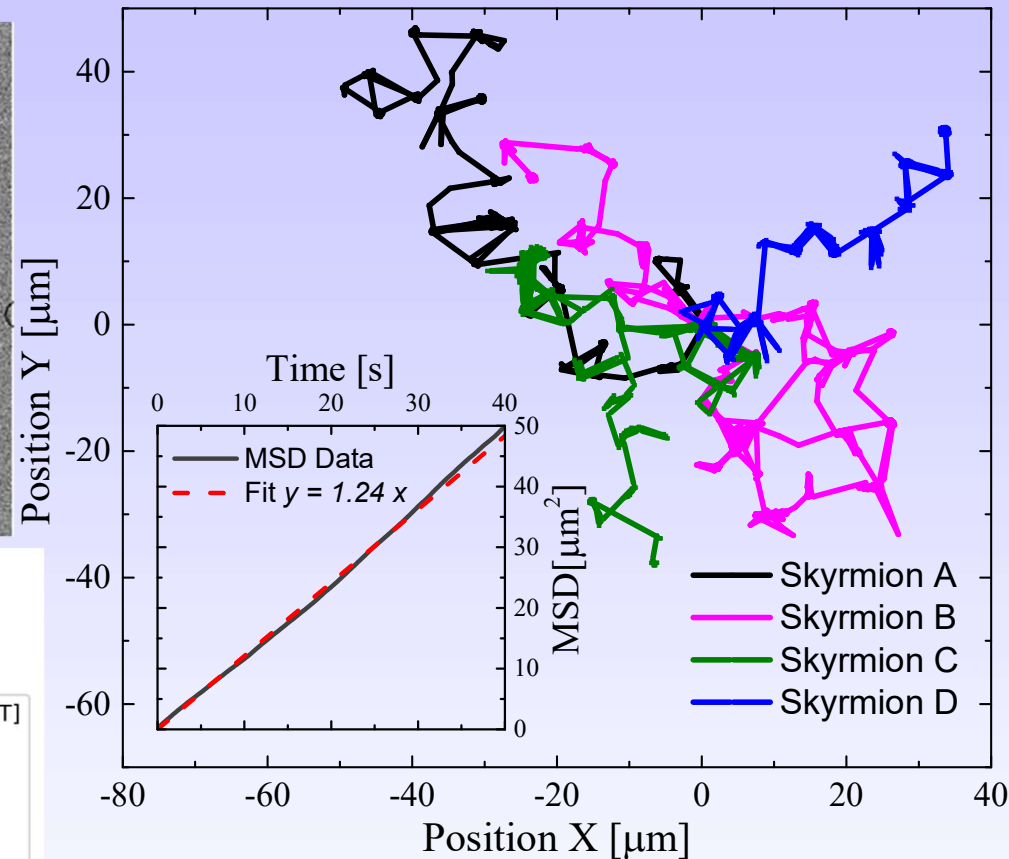
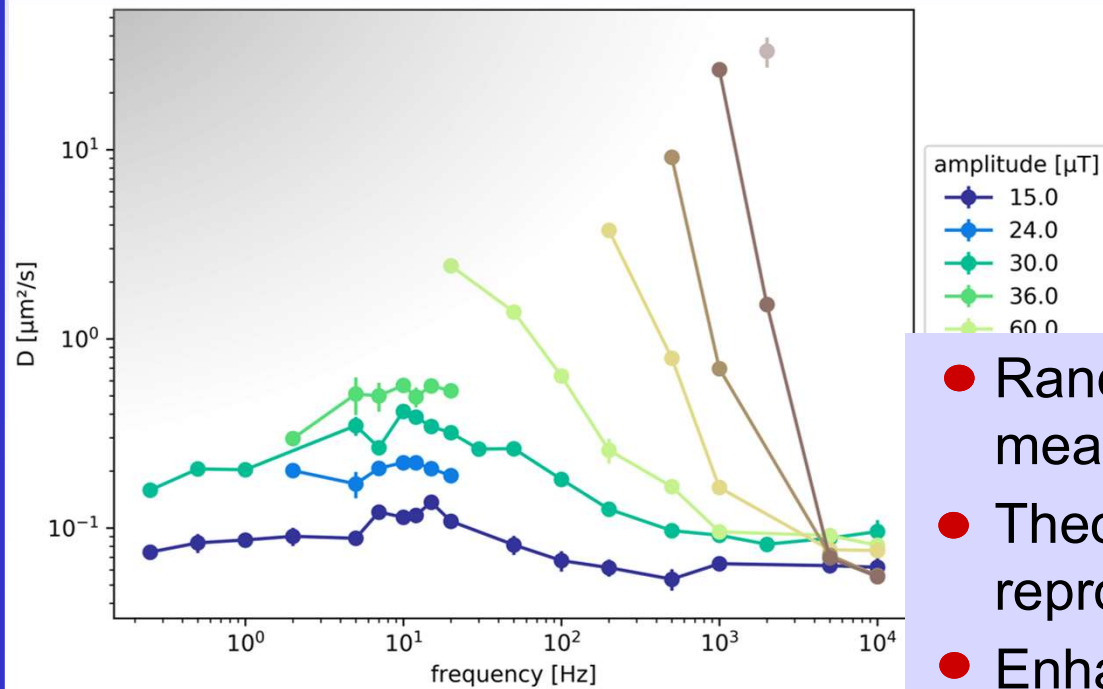
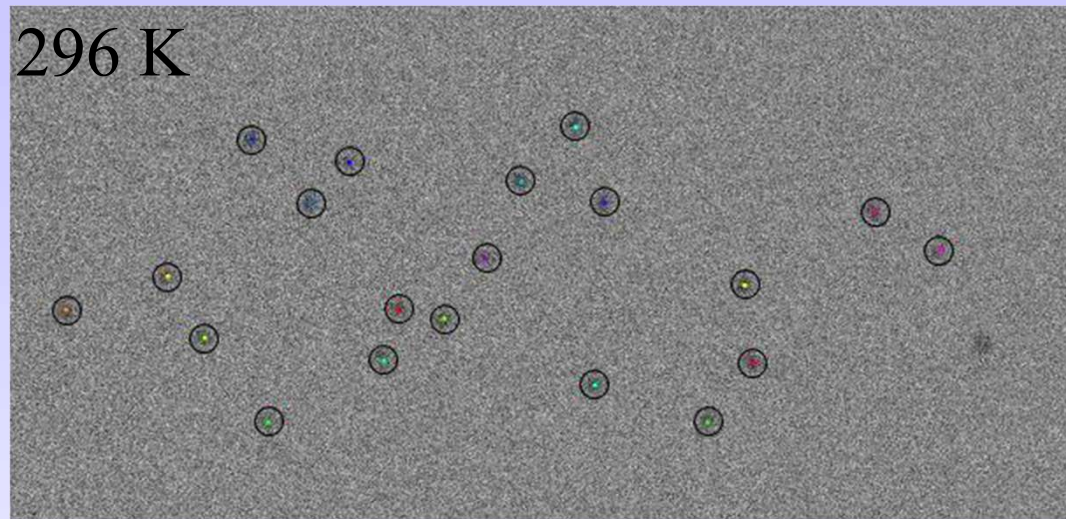


- Random motion exhibits linear scaling for mean square displacement $\rightarrow$ diffusion!
- Theoretical numerical spin simulations reproduce diffusion
- Use in unconventional computing?^{1,2}

¹J. Zazvorka, MK et al., Nature Nano. **14**, 658 (2019)
cf. L. Zhao et al., PRL **125**, 027206 (2020)

²D. Pinna et al., PRAppl. **9**, 064018 ('18); PRAppl. **9**, 014034 ('18)

4. Skyrmion Diffusion

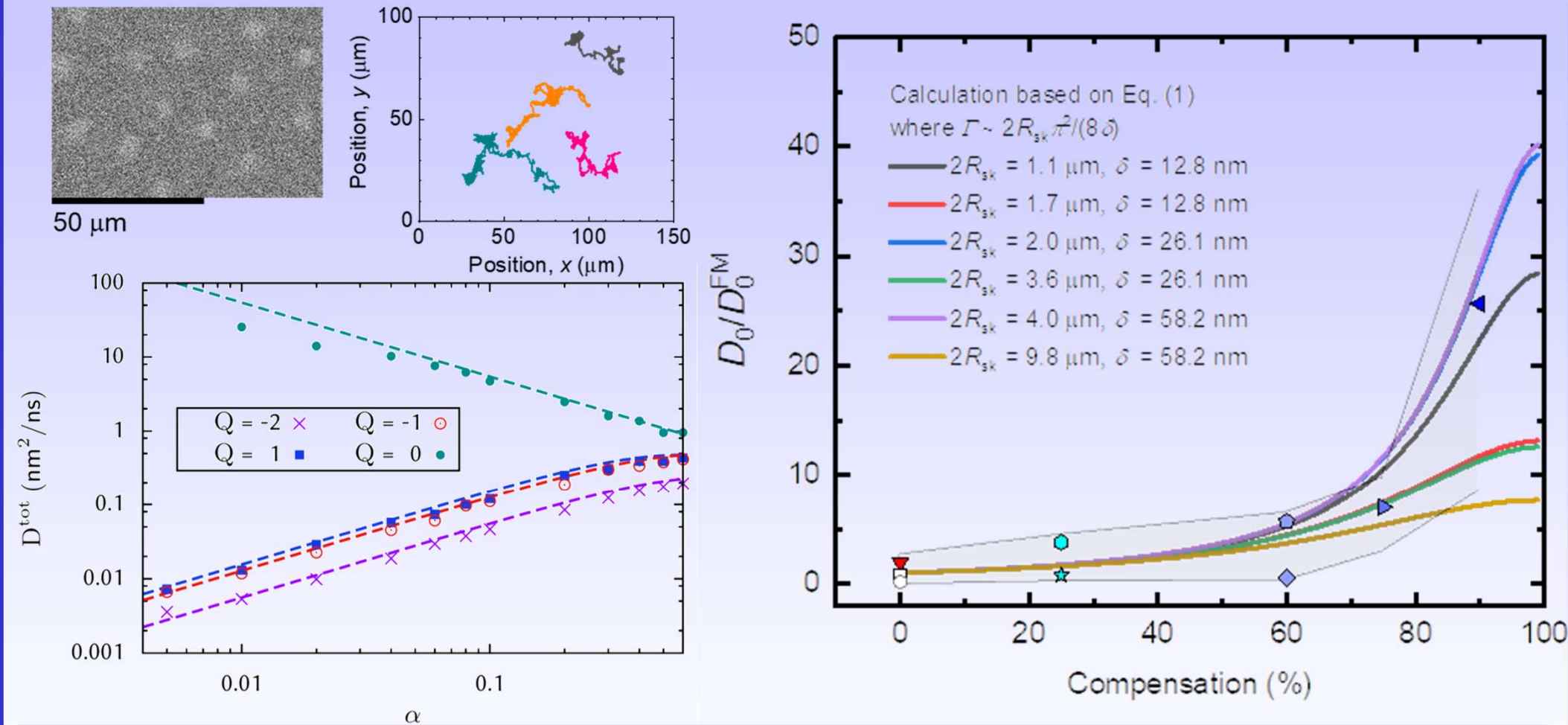


- Random motion exhibits linear scaling for mean square displacement $\rightarrow$ diffusion!
- Theoretical numerical spin simulations reproduce diffusion
- Enhanced diffusion by AC excitations²

¹J. Zazvorka, MK et al., Nature Nano. **14**, 658 (2019)
cf. L. Zhao et al., PRL **125**, 027206 (2020)

²R. Gruber, MK et al., Adv. Mater. 2208922 (2023)

4. Ultimately fast Skyrmion Diffusion in (synthetic) antiferromagnets



- Synthetic antiferromagnets: topological charge tuned by compensation ratio!
- Developed synthetic antiferromagnets SAFs with tailored compensation ratio¹
- Thermal dynamics: predicted to be suppressed by finite topological charge²
- Diffusion enhanced >20 times for maximally compensated (fully AFM) SAFs³

¹D. Han et al., Nat. Mat. **18**, 905 (2019); ²M. Weissenhofer et al., NJP **22**, 103059 (2020); ³T. Dohi et al., arxiv:2206.00791

Skyrmions in Spin-Orbitronics & Orbitronics: novel science and applications in memory & non-conventional computing

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- Fast dynamics: Spin and Orbital Torques
- Efficient dynamics: thermal diffusion
- **Non-conventional logic** with skyrmions

JOHANNES GUTENBERG
UNIVERSITÄT MAINZ

MATERIALS
IN
MAINZ SCIENCE

Qu.
Spin



Non-conventional low power computing using skyrmions: (I) Stochastic computing

5. Stochastic Computing

- Stochastic computing
- Non-arithmetic way of calculation using random bit streams
- Only approximation of result - “progressive precision”
- Simple way of multiplying numbers using only AND-gates (and some other functions such as scaled addition, etc.)
- Problem in stochastic computing is the creation of unbiased, uncorrelated bit streams

5. Stochastic Computing

- Stochastic computing – information representation

X



Coin

$$P\{X=1\} = 0.50 \text{ "Heads"}$$

Bitstream X: 0 1 0 0 1 1 1 1 0 1 0 1 1 0 0...
50% = 1 "Heads" and 50% = 0 "Tails"

Y



Cards

$$P\{Y=1\} = 0.25 \text{ "Ace"}$$

Bitstream Y: 0 0 0 0 1 0 0 0 0 0 1 1 0 0 0...
25% = 1 "Ace" and 75% = 0 "other card"

Bernoulli experiments

5. Stochastic Computing

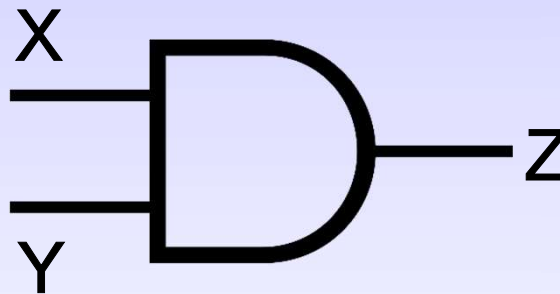
- Stochastic computing – implementing operations

Bitstream X: 010011110101100...

50% = 1 - “Heads” and 50% = 0 - “Tails”

Bitstream Y: 000010000011001...

25% = 1 - “Ace” and 75% = 0 - “other card”



AND - Gate

Bitstream X: 0 1 0 0 1 1 1 1 0 1 0 1 1 0 0...

Bitstream Y: 0 0 0 0 1 0 0 0 0 0 1 1 0 0 1...

Bitstream Z: 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0...

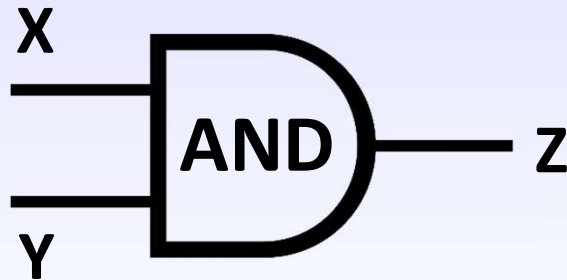
5. Stochastic Computing

- Stochastic computing – implementing multiplication

Bitstream X: 0 1 0 0 1 1 1 1 0 1 0 1 1 0 0... $\approx a = 0.50$

Bitstream Y: 0 0 0 0 1 0 0 0 0 0 1 1 0 0 1... $\approx b = 0.25$

Bitstream Z: 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0... $\approx c = \text{result}$



If X and Y are independent, then
 $(a) * (b) = P\{X=1 \text{ and } Y=1\} = c$

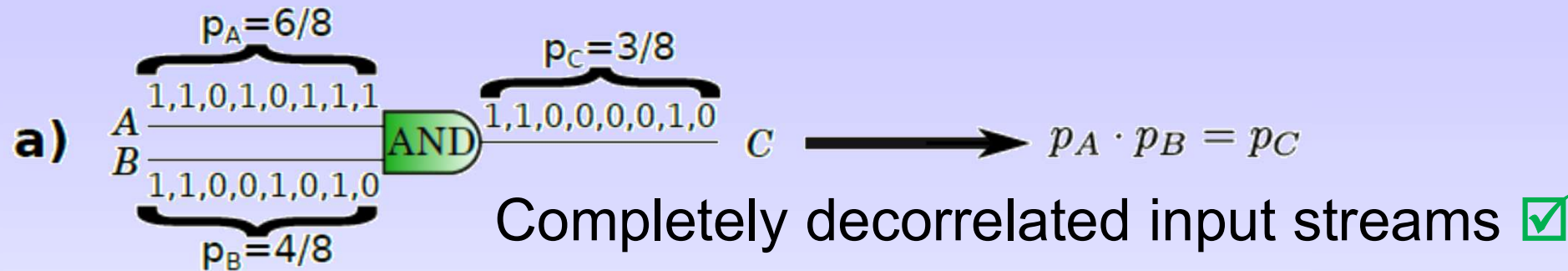
$$P\{Z=1\} = (0.5) (0.25) = 0.125 = c$$

$P\{Z=1\} = P\{X=1 \text{ and } Y=1\}$ Chance for “Heads” and “Ace”: 12.5% 

Result c is only correct if Bitstreams X and Y are uncorrelated

5. Skyrmion Diffusion for probabilistic computing

- Examples of stochastic computing :

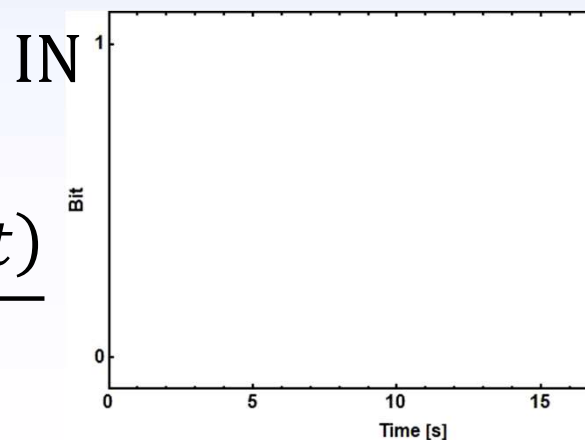
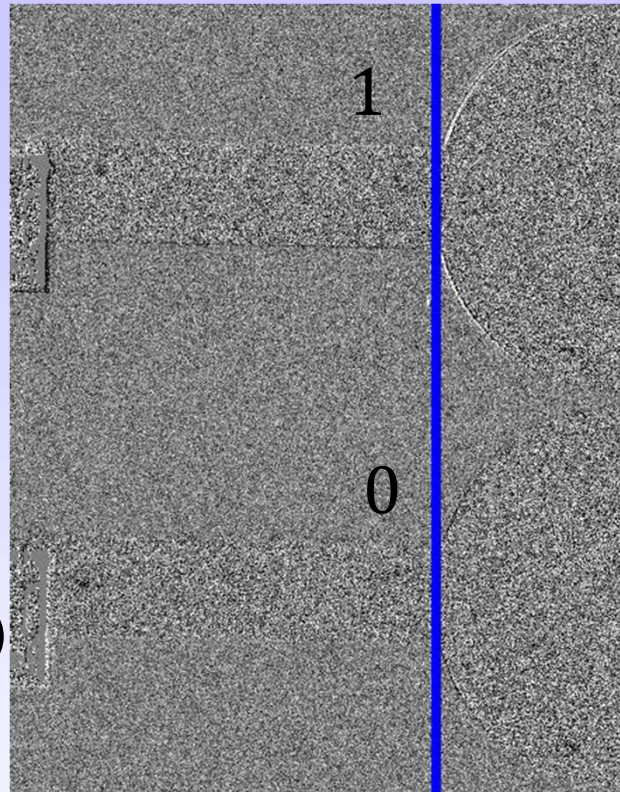


To obtain decorrelated input streams → reshuffler needed

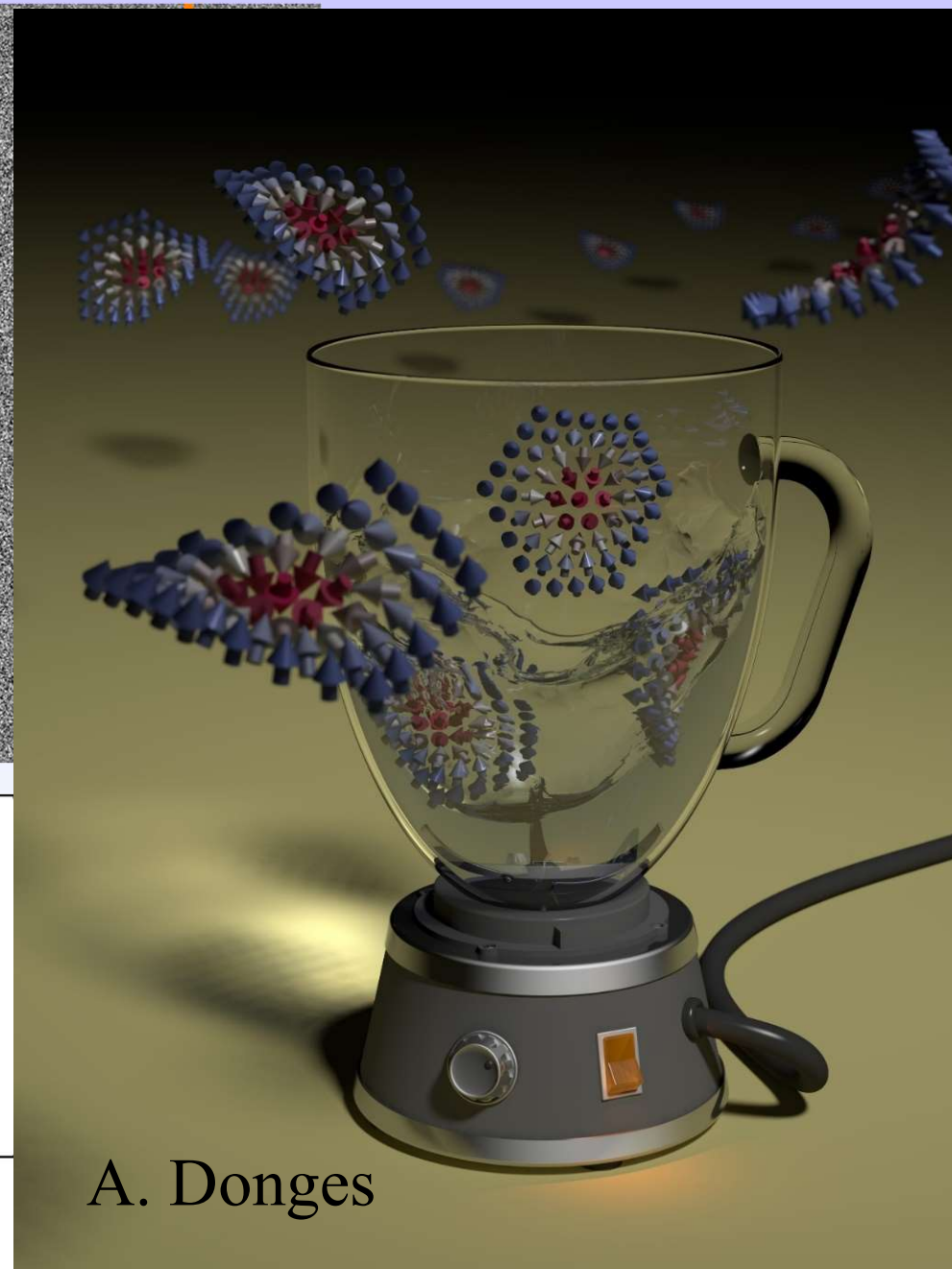
5. Skyrmion Reshuffler to create uncorrelated bitstreams

Realization:

- Skyrmion nucleation with pulses or DC.
- Readout with imaging.
- Skyrmions enter the chamber (blue line→input)
- Exiting chamber (orange) triggers corresponding bit → output signal



$$\rho = \frac{\text{cov}(in, out)}{\sigma_{in} \cdot \sigma_{out}}$$

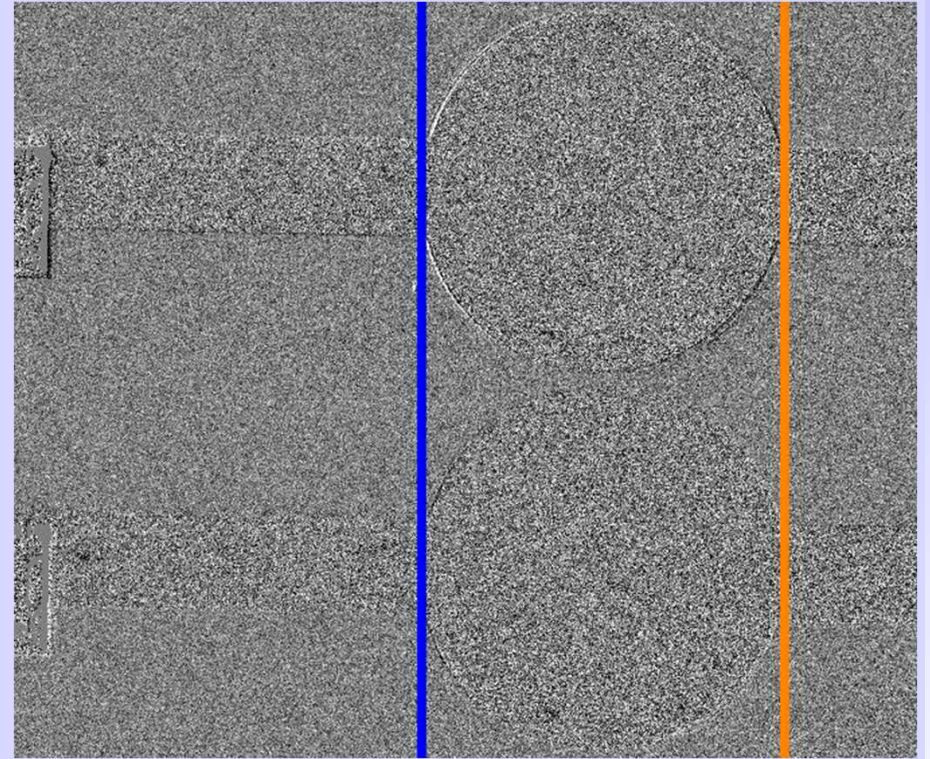


A. Donges

5. Logic using skyrmions

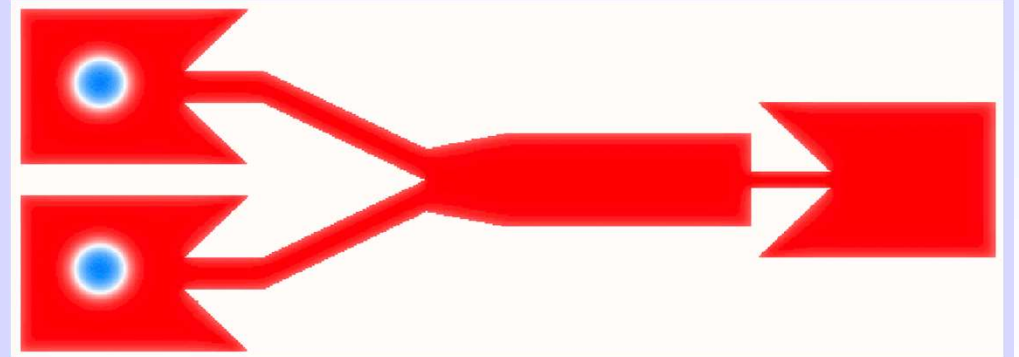
- Stochastic Logic can be realized with Skyrmions
- Combining:

1. Skyrmion Reshuffler



2. AND Gate

X. Zhang et al., Sci. Rep. 5, 9400 (2015)



→ Multiplication using probabilistic computing approach

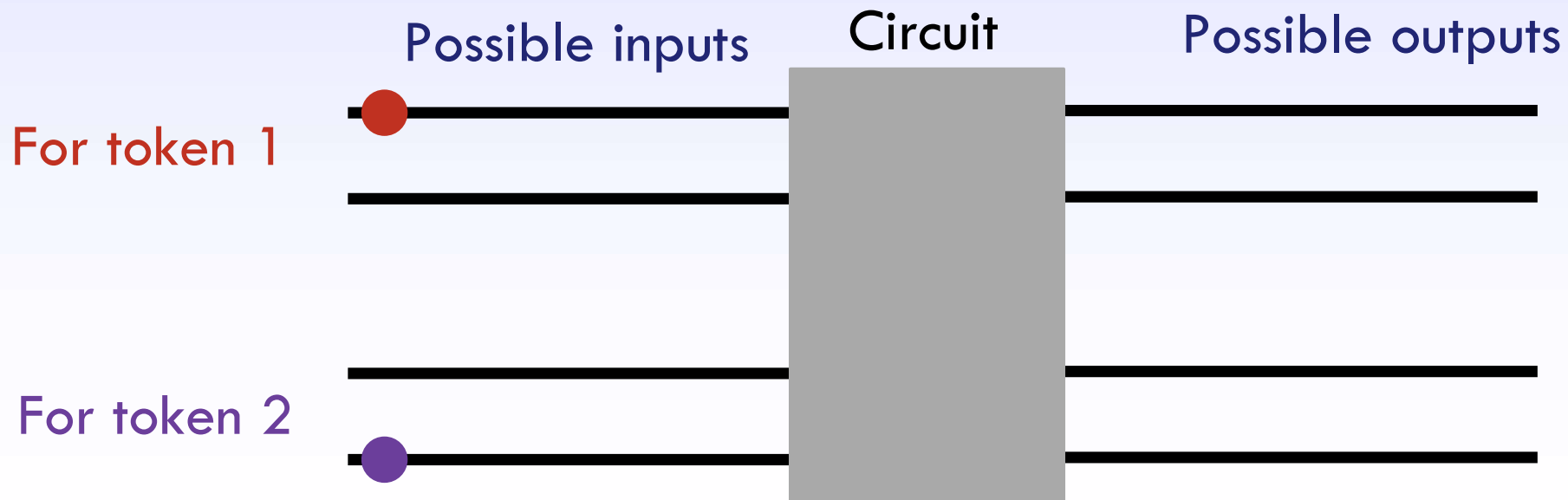
**Non-conventional
low power computing
using skyrmions:
(II) Token-based
Brownian Computing**

6. Token-based Brownian Computing - Basics

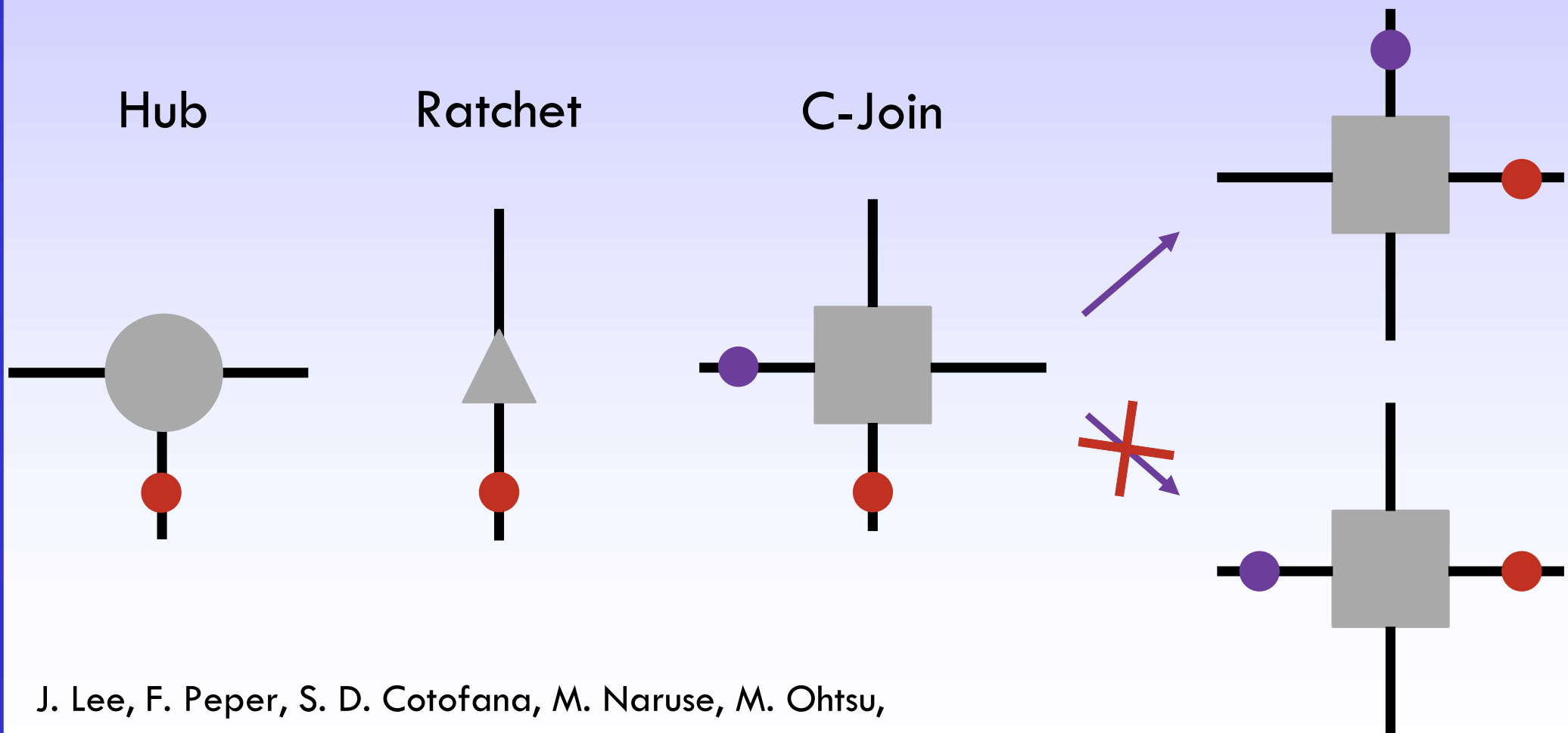
TOKEN-BASED COMPUTING FUNDAMENTALS

Token: Discrete signal carrier

Circuit: Network with special transition rules



6. Token-based Brownian Computing – Circuit Components



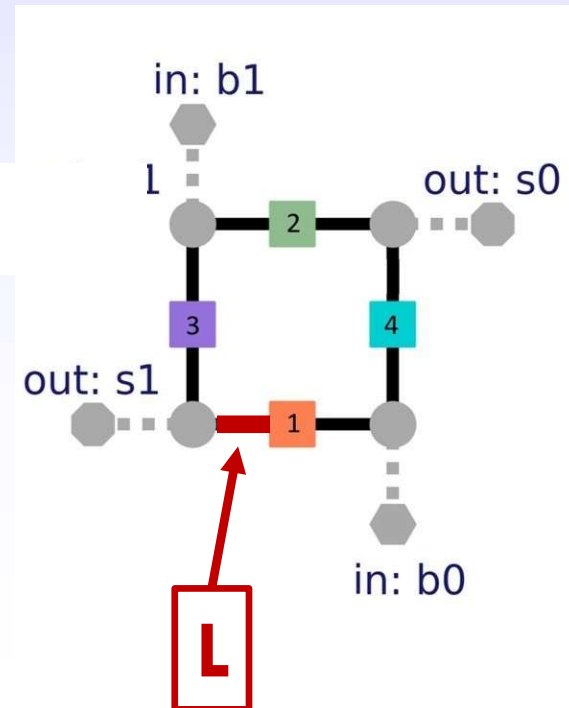
J. Lee, F. Peper, S. D. Cotozana, M. Naruse, M. Ohtsu,
T. Kawazoe, Y. Takahashi, T. Shimokawa, L. B. Kish, T. Kubota,
“**Brownian circuits: Designs**”, Int. J. Unconv. Comput. 12, 341-362 (2016)

6. Token-based Brownian Computing

COMPARISON IN REAL TIME

Layout	Condition	$L = 10 \mu\text{m}$	$L = 5 \mu\text{m}$
Crossing (thermal)	$T = 307.6 \text{ K}$	16 min	4 min

Using synthetic antiferromagnet: sub- μs operation!²



¹M. A. Brems, P. Virnau, M. Kläui,
**“Circuits and excitations to enable Brownian token-based
 computing with skyrmions”**, Appl. Phys. Lett. **119**, 132405 (2021)

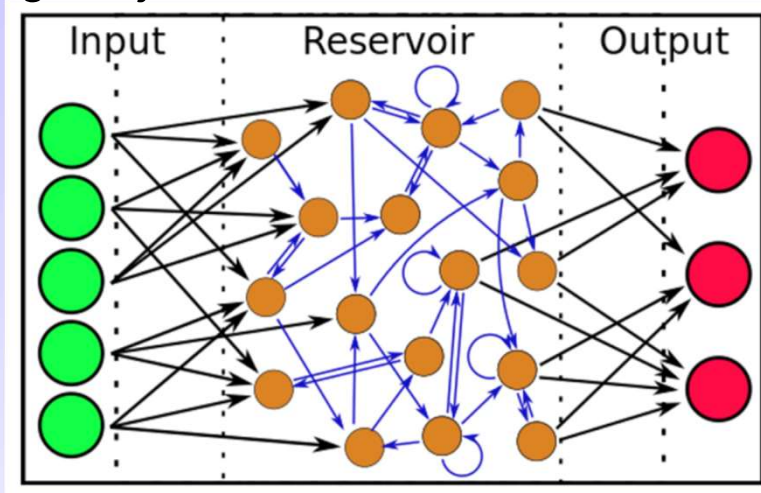
M. A. Brems, P. Virnau, M. Kläui,
“Information processing apparatus”,
European patent disclosure, EP21164676.5 (2021)

²T. Dohi, MK et al., arxiv:2206.00791 (under review 2022)

**Non-conventional
low power computing
using skyrmions:
(III) Reservoir Computing**

6. Reservoir Computing with Skyrmions

originally: artificial neural network with



recursive
neural network

feed forward
only

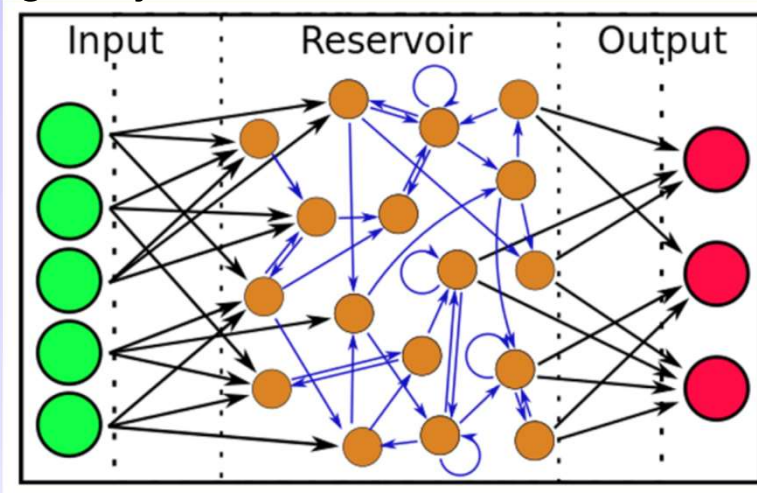
Goal: map a complex problem to a linearly solvable one

- **Network does not need tuning:** internal connections are fixed
- Only output connections are trained

**RC bypasses
training constraints**

6. Reservoir Computing with Skyrmions

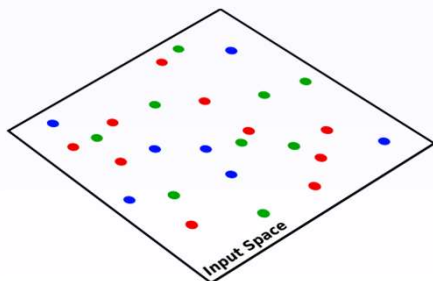
originally: artificial neural network with



Goal: map a complex problem to a linearly solvable one

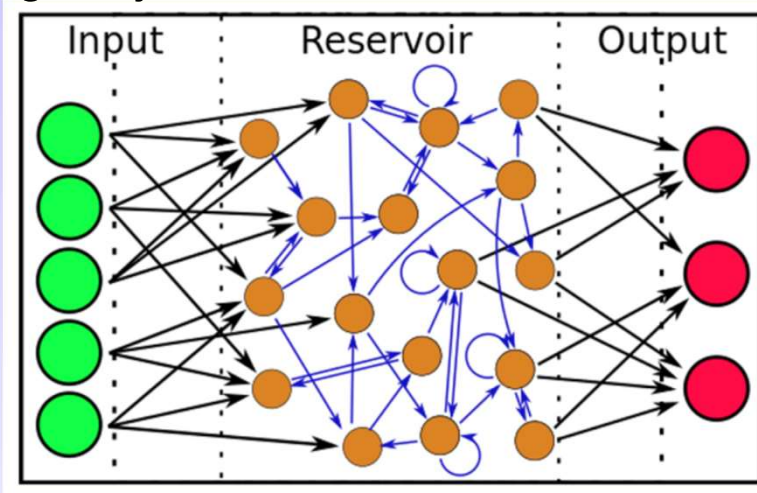
Functionality:

Reservoir projects different spatial-temporal events into a sparsely populated high dimensional space where they become easier to recognise and categorise



6. Reservoir Computing with Skyrmions

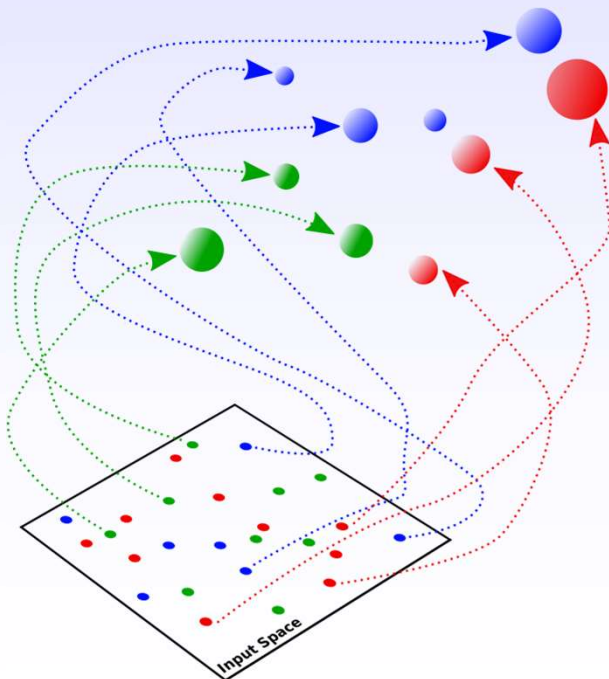
originally: artificial neural network with



Goal: map a complex problem to a linearly solvable one

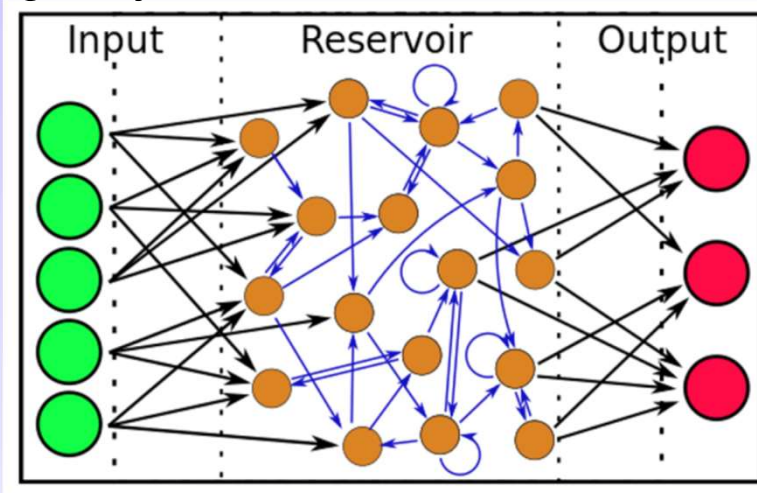
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6. Reservoir Computing with Skyrmions

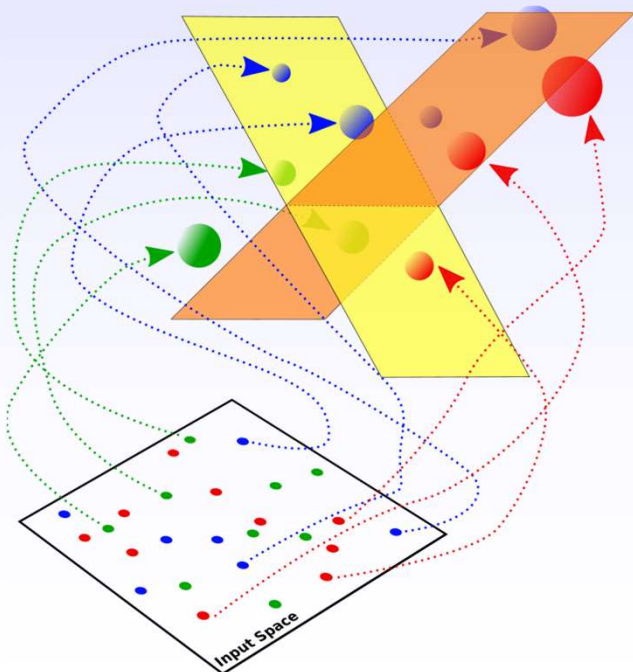
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Goal: map a complex problem to a linearly solvable one

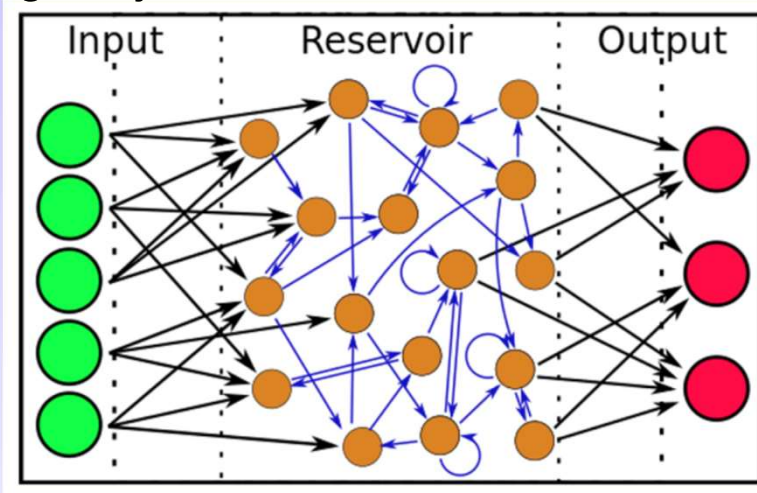
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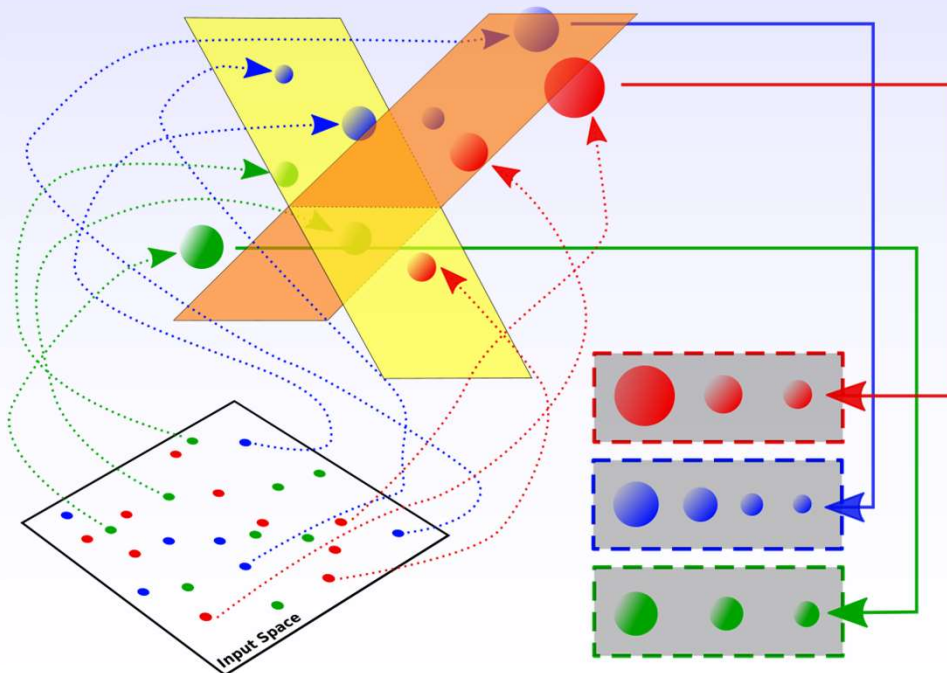
originally: artificial neural network with



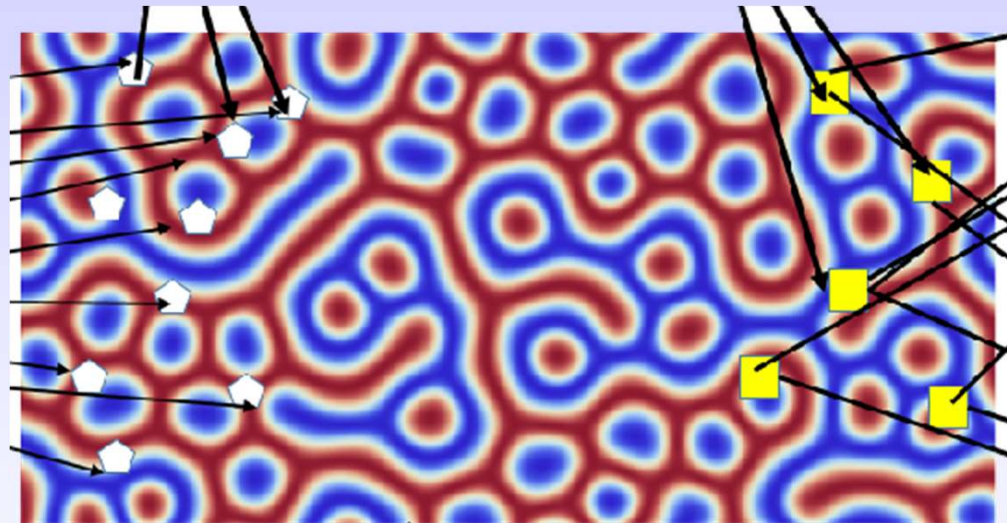
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6. Reservoir Computing using Skyrmions



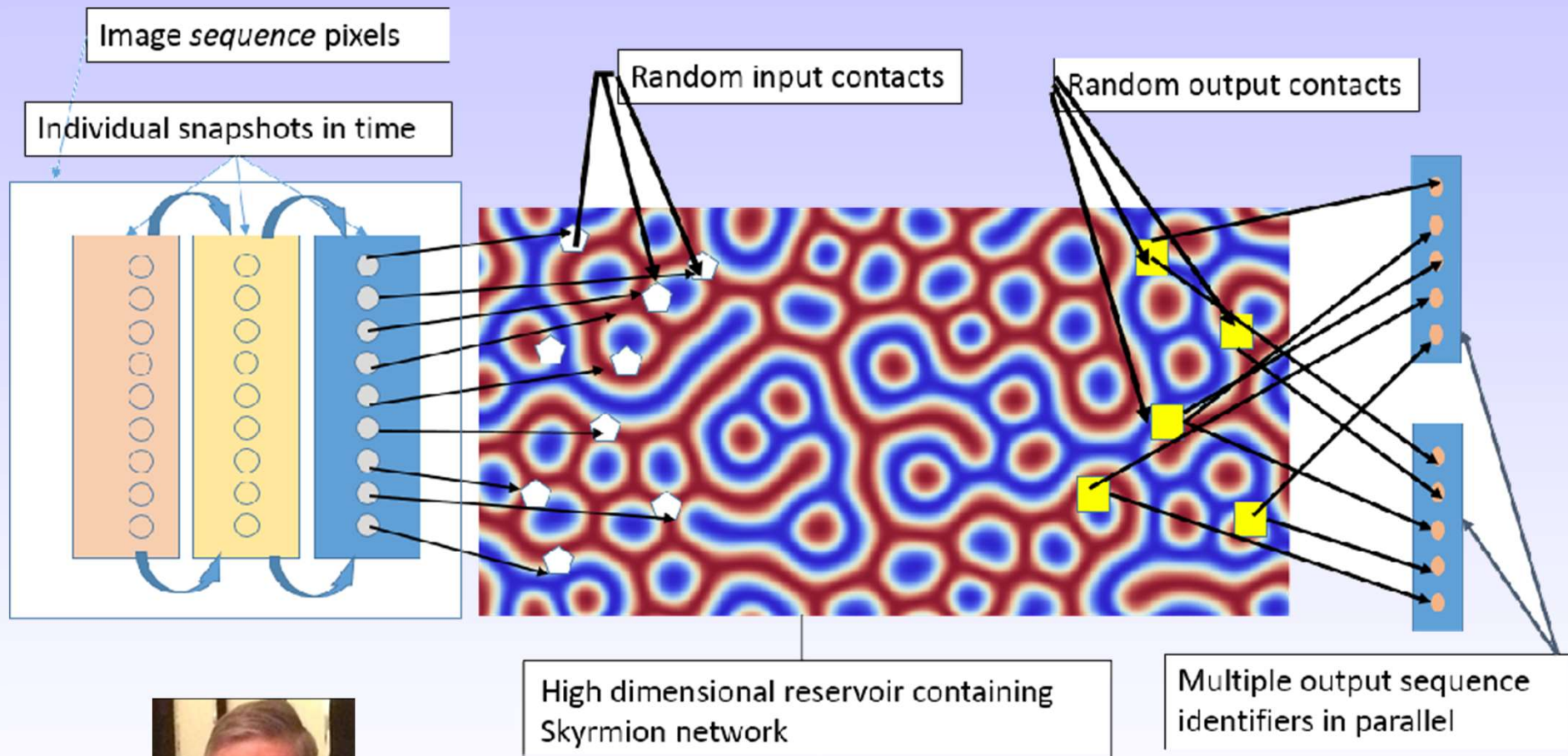
“skyrmion fabrics” as reservoir



George Bourianoff



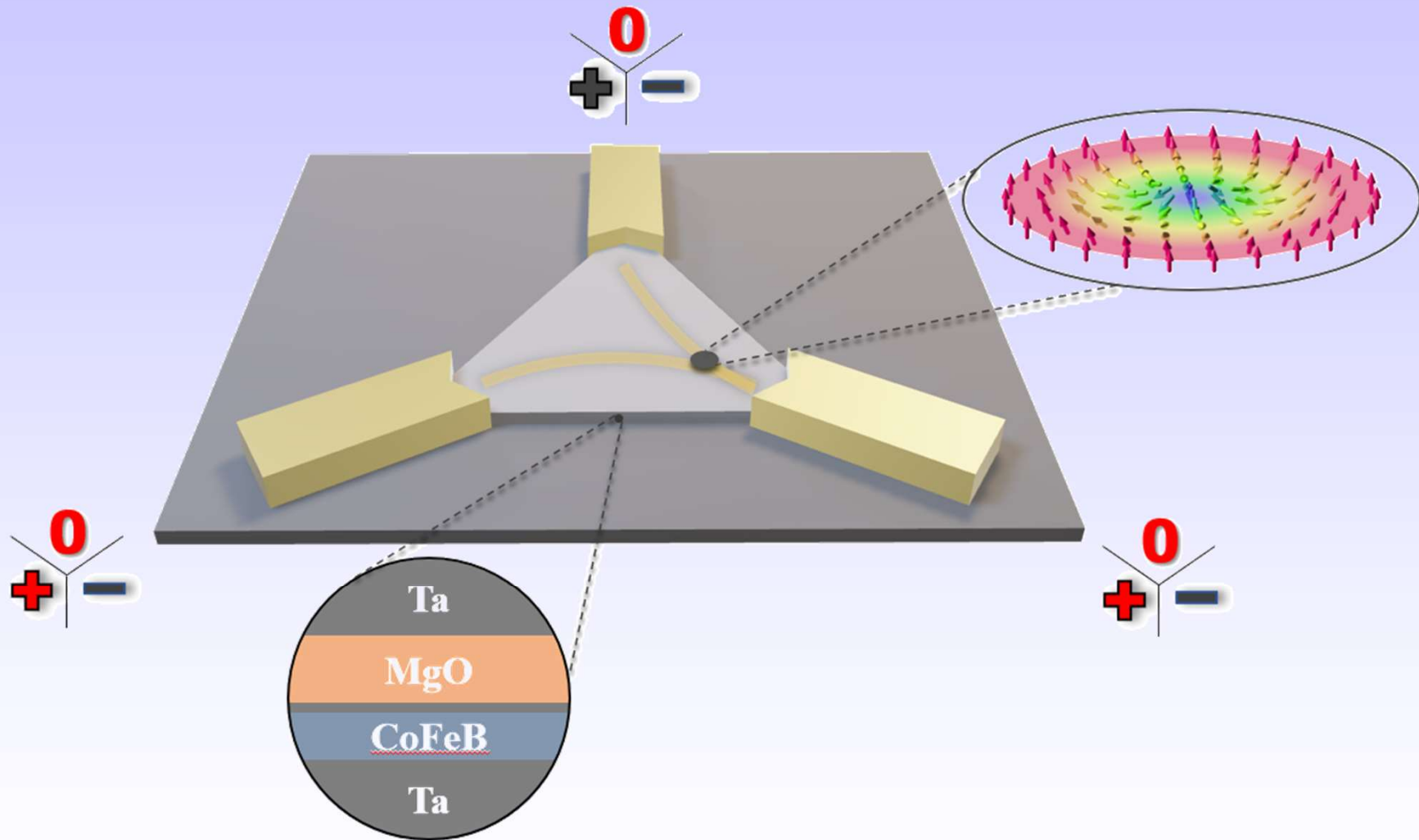
6. Reservoir Computing using Skyrmions



George Bourianoff



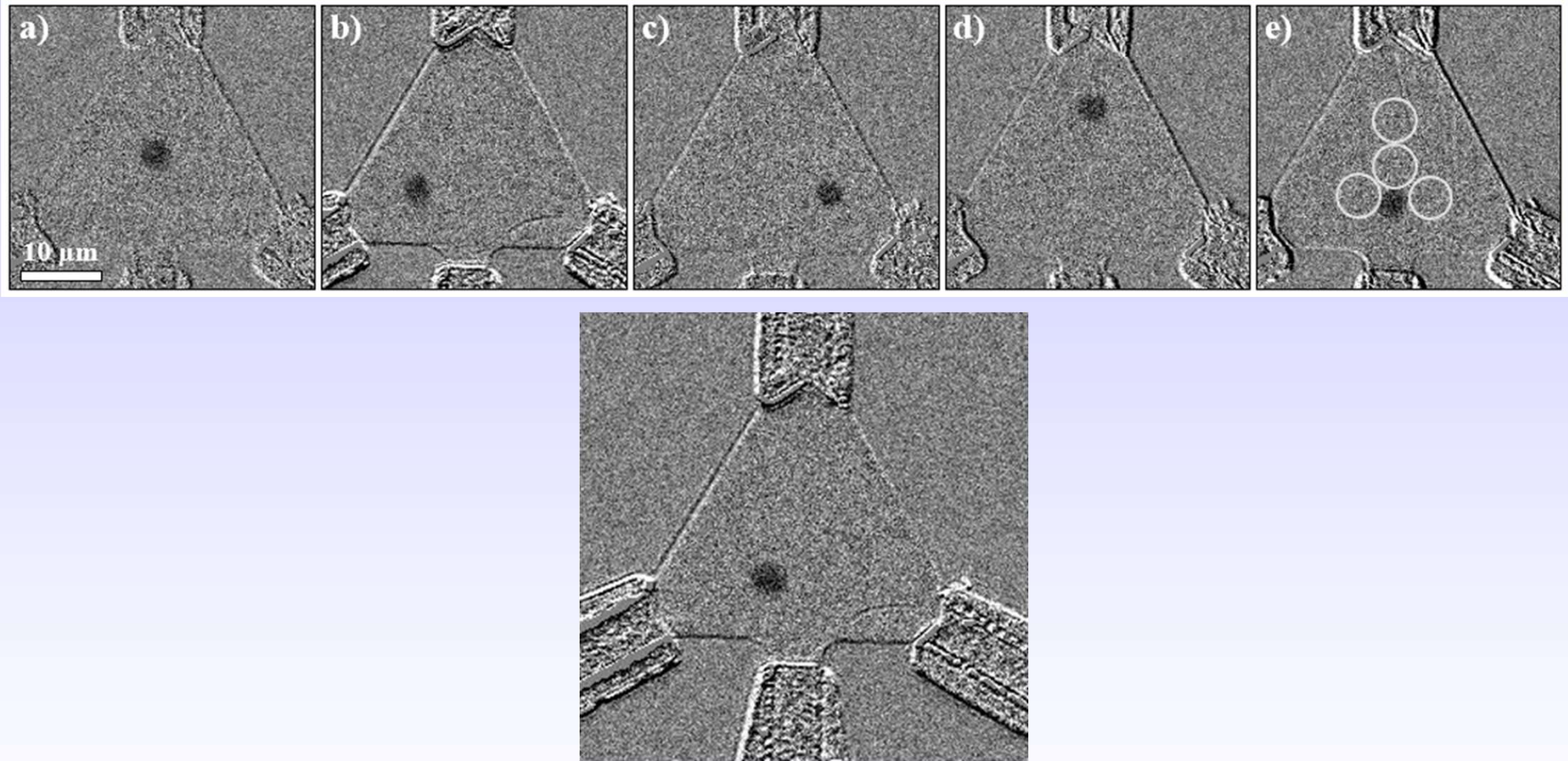
7. Realization of spatial multiplexing reservoir computing



K. Raab, MK et al., Nature Comm. **13**, 6982 (2022)

- Analysis of dynamics of skyrmions in a confined geometry with additional **input currents** → aim to learn input current combinations from skyrmion positions.

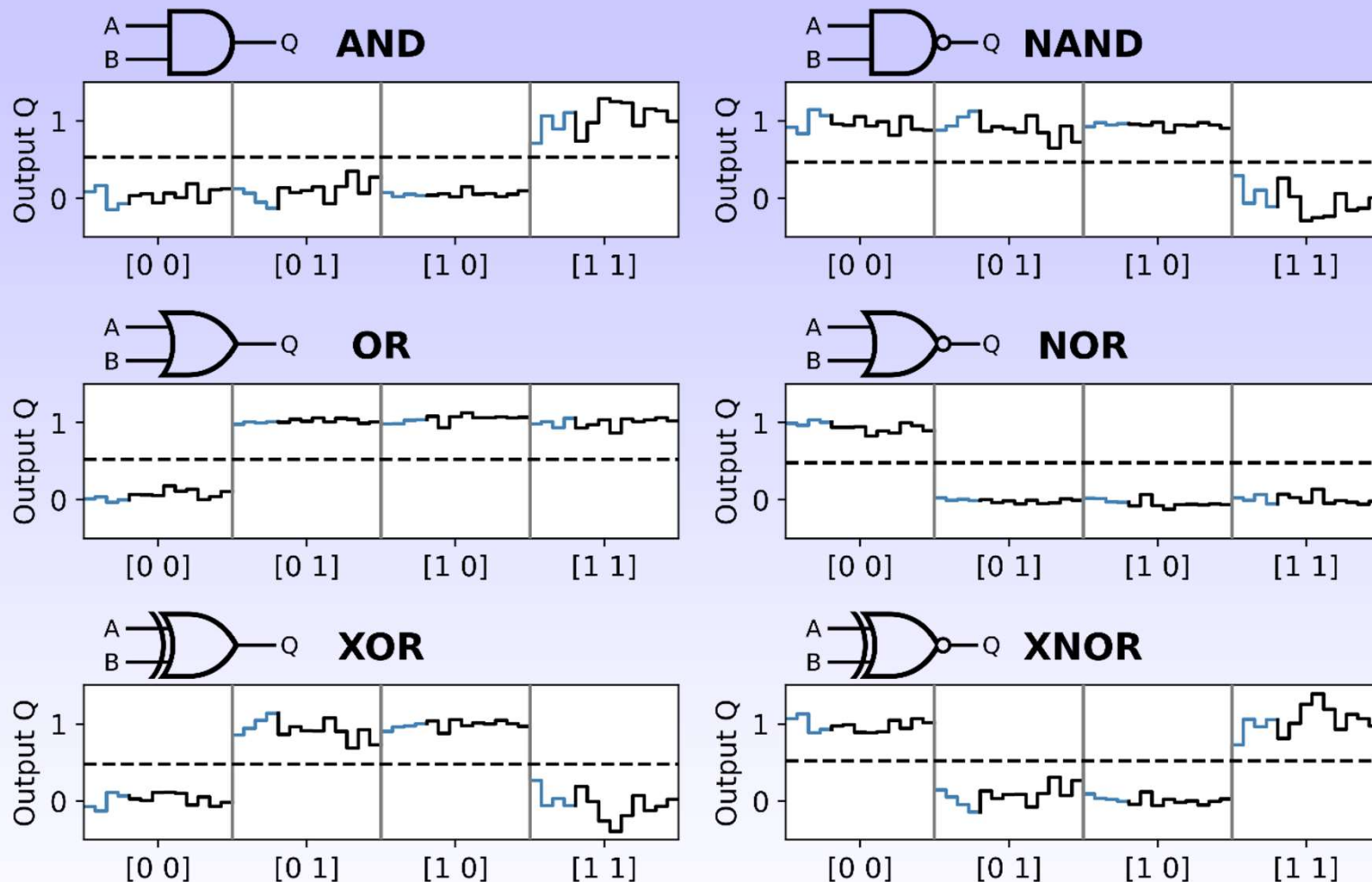
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7. Realization of spatial multiplexing reservoir computing



K. Raab, MK et al.,
Nature Comm. **13**,
6982 (2022)

← Non-separable
functions
(outperforming
simple perceptron)

Analysis of Output $Q = W_{left}P_{left} + W_{right}P_{right} + W_{top}P_{top} + W_{middle}P_{middle} + W_{intercept}$

- Outputs of the linear read-out optimized for different Boolean operations.
- For each input combination $[A\ B]$ the output Q of the linear read-out is shown for sets of local skyrmion occurrence probabilities. Light blue: training sets; Black: sets used for testing
- Dashed horizontal line indicates a possible threshold for perceptron read-out.

Thanks!

1. Great people@JGU

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J. Rothörl, T. Winkler, M. Schmitt, C. Song,
T. Sparmann, G. Beneke, T. Saunderson,
K. Leutner, **P. Virnau**, **R. Frömter**, **M. Jourdan**, **G. Jakob**...and former group members!



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H. Stoll, J. Förster, M. Weigand, G. Schütz MPI-IS&BESSY; O. Gomonay,
P. Virnau, D. Pinna, K. Everschor-Sitte, J. Sinova, Y. Mokrousov JGU Mainz;
S. Yochelis, Y. Kapon, N. Bar-Gil, Y. Paltiel, HUJI, 3D MAGiC Consortium
A. Qaiumzadeh, A. Brataas, NTNU

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EU (ITN MagnEFI, STREPs A-SPIN, s-Nebula), Infineon,
European Research Council Grant 3D MAGiC, ADI, Antaios
Stanford-Tohoku-Mainz SpinNet, Samsung, TopDyn Centre



Summary:

- **DMI stabilizes chiral spin structures with defined topology: pinning at domain walls**

Nature Materials **15**, 501 (2016); Nature Materials **18**, 703 (2019); Nano Lett ('23)
Nature Commun. **11**, 6304 (2020); Nature Commun. **13**, 3144 (2022);

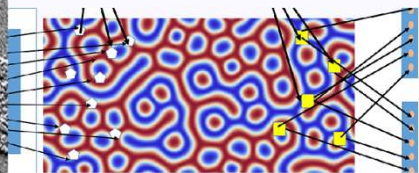
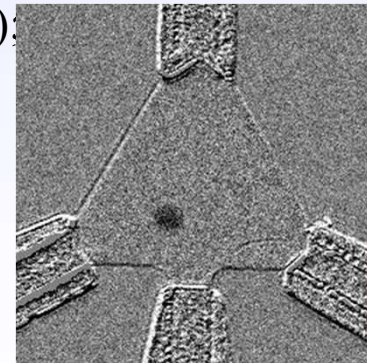
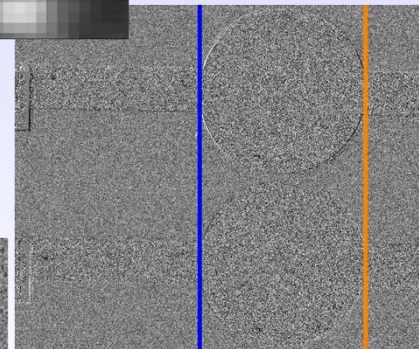
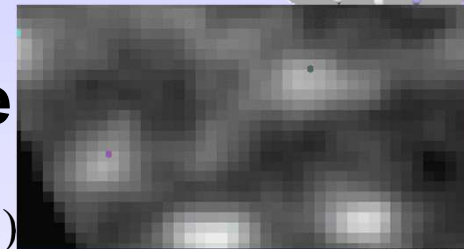
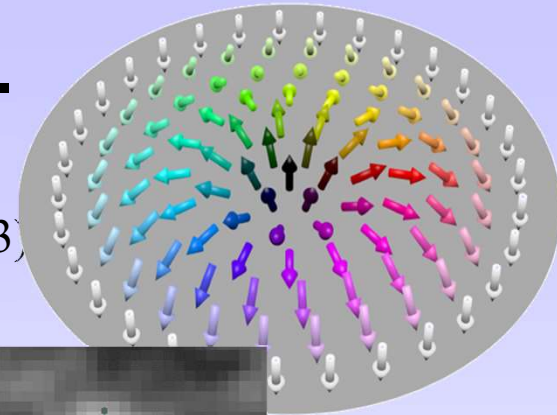
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