Metal-Insulator transitions in infinitesimally weakly disordered flatbands

arXiv: 2107.11365

Tilen Čadež tilencadez@ibs.re.kr





virtual, August 18, 2021

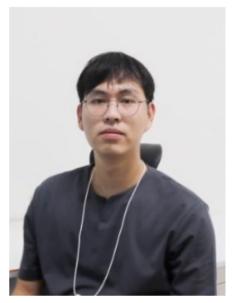


Aim:

Systematic study of all bands flat (ABF) systems in the presence of (infinitesimally) weak disorder.

with

Yeongjun Kim



Alexei Andreanov



Sergej Flach

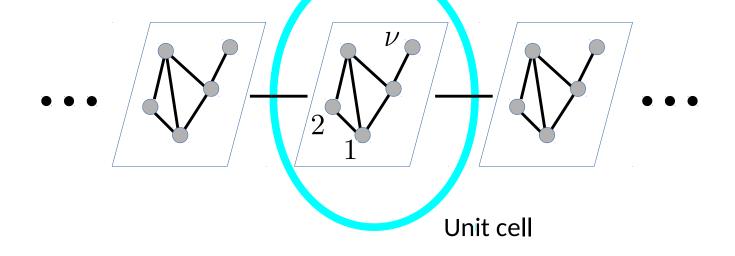


Outline:

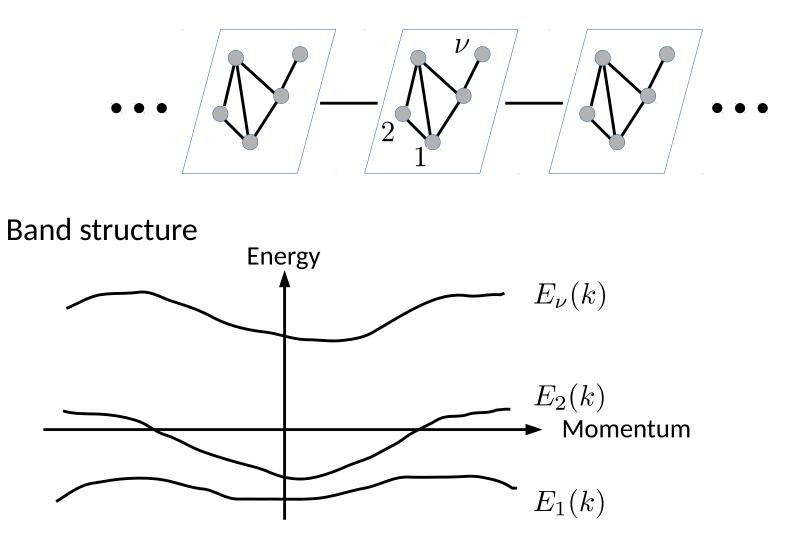
Systematic study of all bands flat (ABF) systems in the presence of (infinitesimally) weak disorder.

- a) ABF construction, 2 bands, d = 1,2,3
- b) Scale free model
- c) Localization in d = 1,2
- d) Metal-insulator transition in d = 3

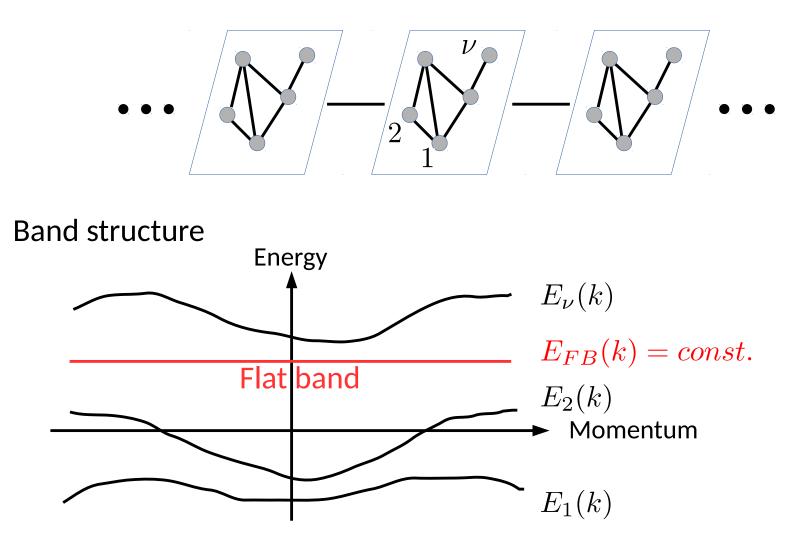
Periodic lattice systems (non-interacting):



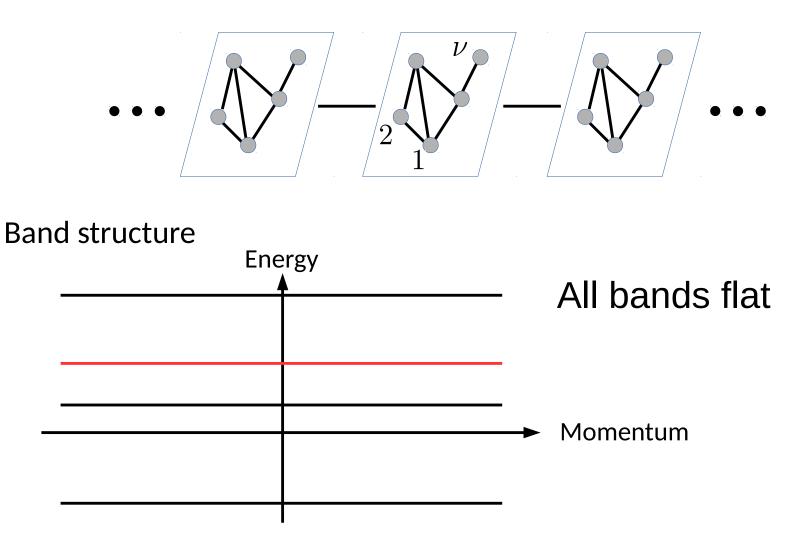
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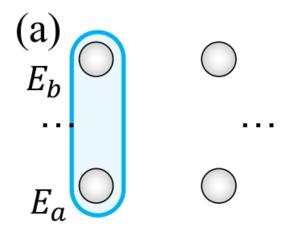
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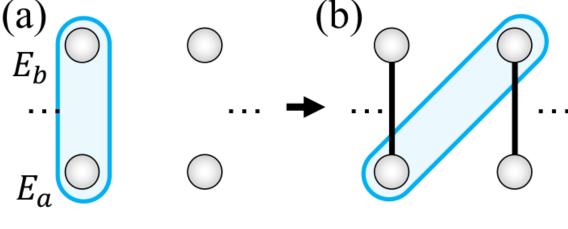
Periodic lattice systems:



a) ABF construction, 2 bands, d = 1 Fully-detangled



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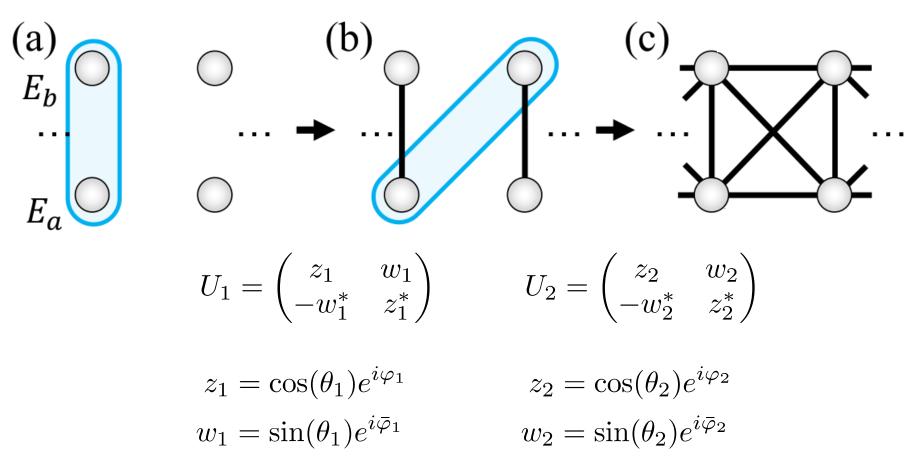
$$U_1 = \begin{pmatrix} z_1 & w_1 \\ -w_1^* & z_1^* \end{pmatrix}$$

Local unitary transformation (LUT)

$$z_1 = \cos(\theta_1)e^{i\varphi_1}$$
$$w_1 = \sin(\theta_1)e^{i\bar{\varphi}_1}$$

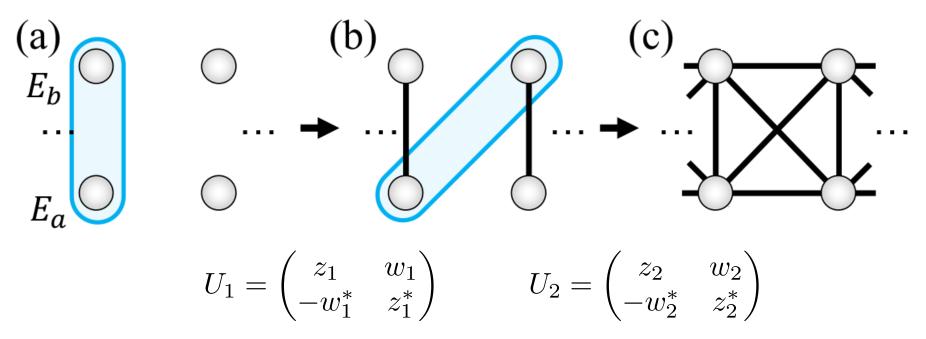
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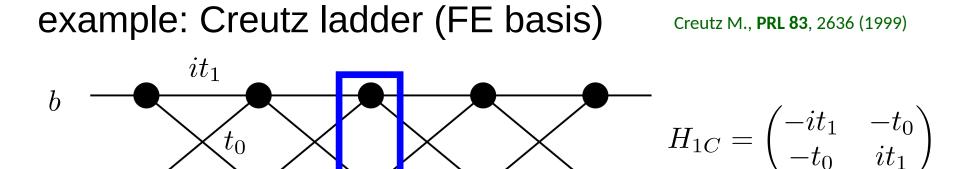


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A manifold of equivalent ABF systems!



$$-it_1$$

$$E_C(k) = \pm 2\sqrt{t_0^2 \cos^2(k) + t_1^2 \sin^2(k)}$$

a

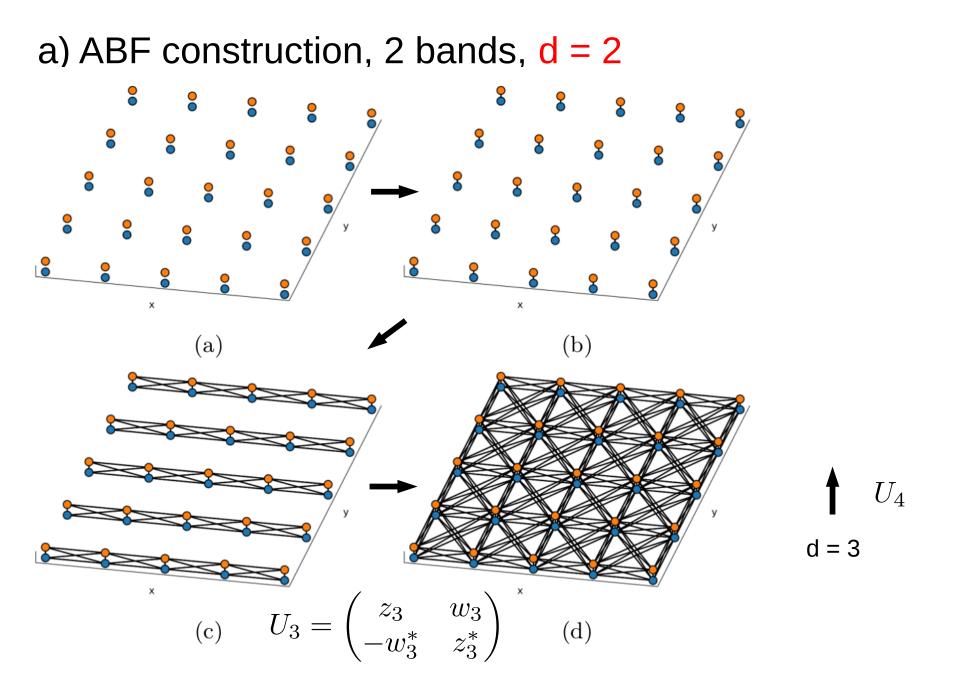
$$t_0 = t_1$$
 ABF

Local unitary transformations (LUT) Danieli C. et al., arXiv 2004.11871 (2020)

$$\theta_1 = \theta_2 = \pi/4 \qquad E_a = -E_b = 2t_0$$

$$\varphi_1 = -\bar{\varphi}_1$$

$$\varphi_2 = 2\bar{\varphi}_2 = \pi$$

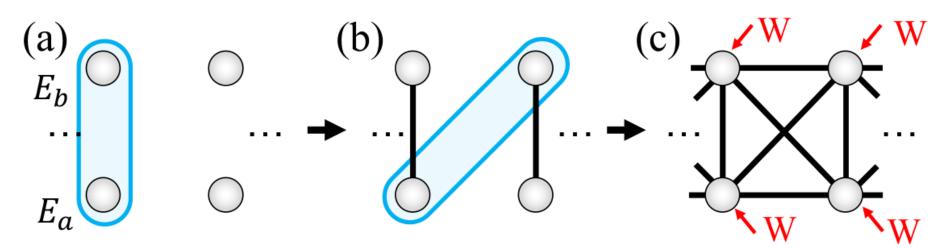


Disorder

Fully-detangled

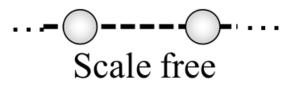
Semi-detangled

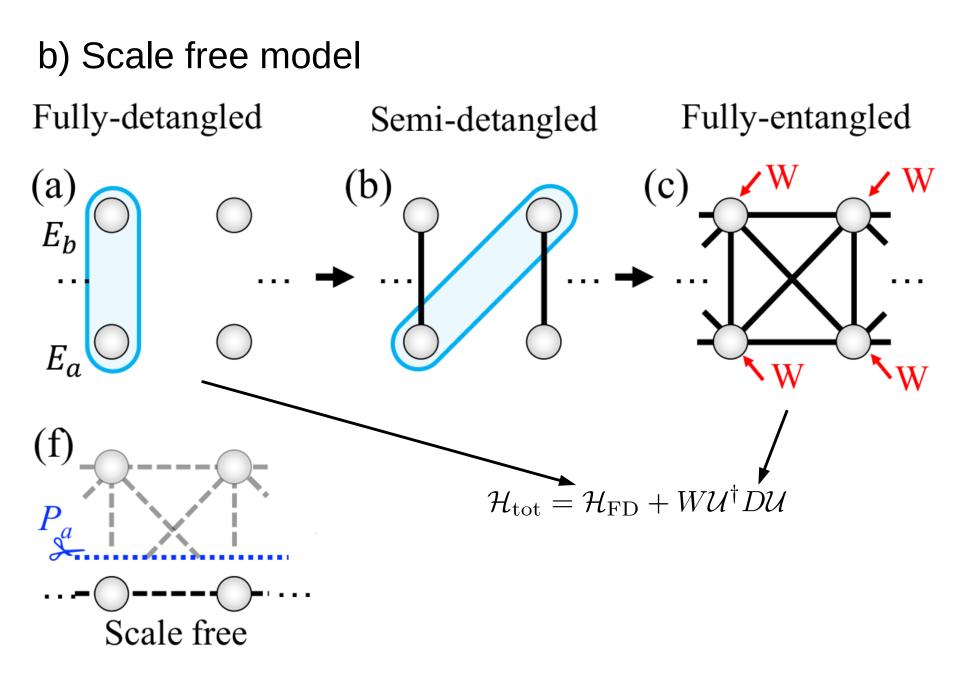
Fully-entangled

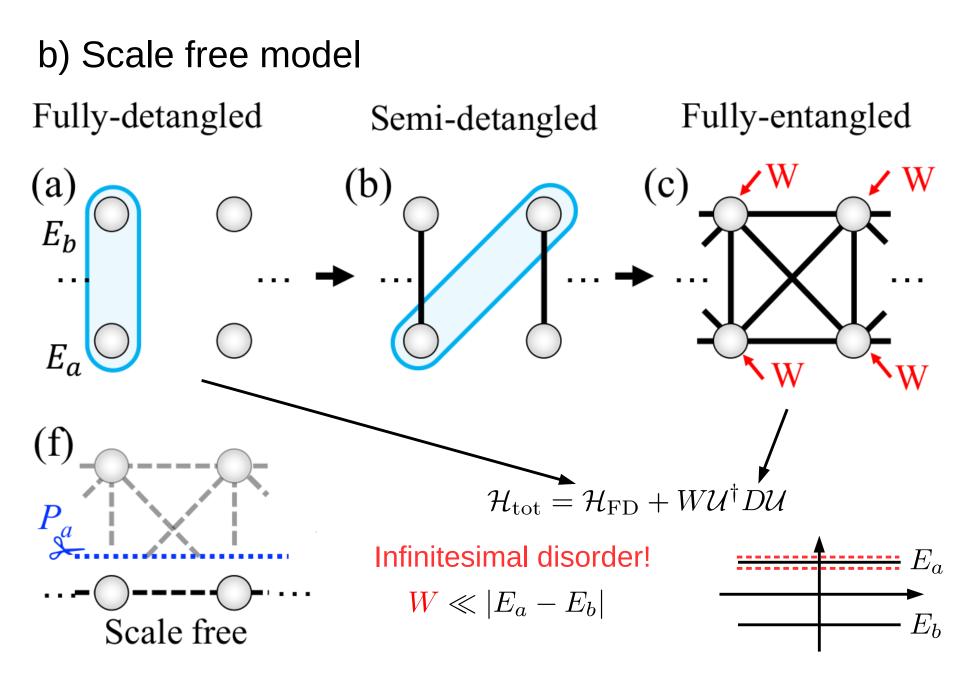


Adding potential (onsite) disorder $\varepsilon_n \in [-W/2, W/2]$

b) Scale free model, 2 bands, d = 1 Fully-detangled Semi-detangled Fully-entangled (c)(a)(b) E_b E_a (f) (\mathbf{d}) (e





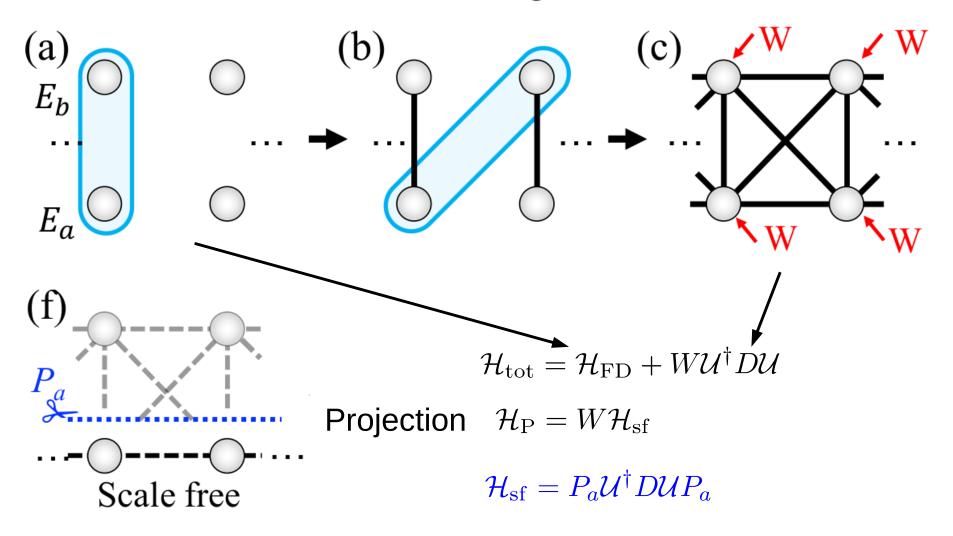


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Fully-detangled

Semi-detangled

Fully-entangled



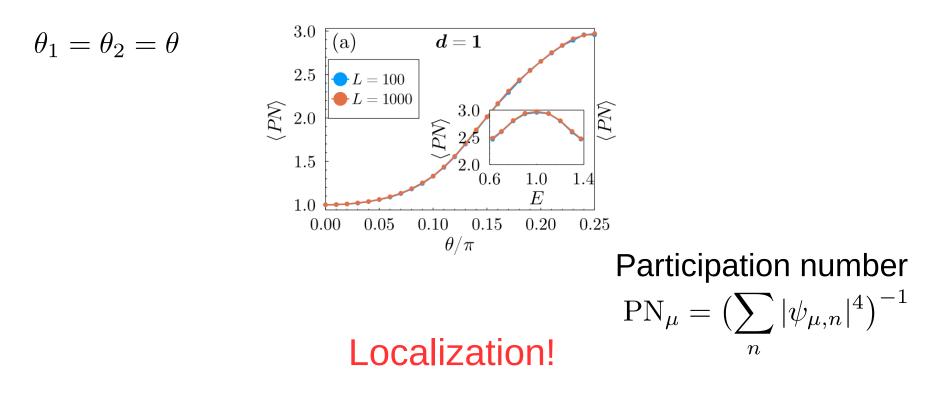
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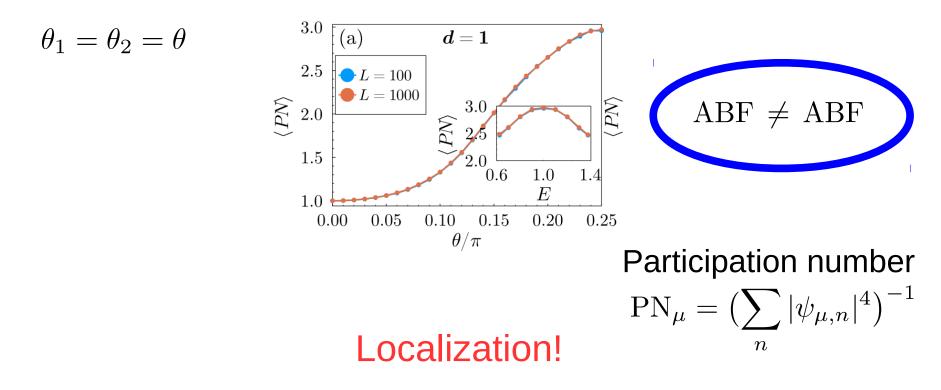
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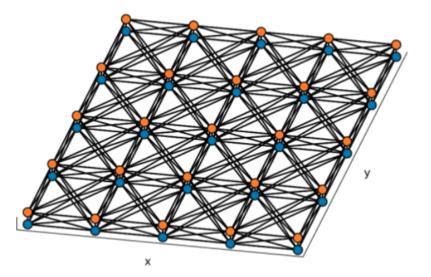
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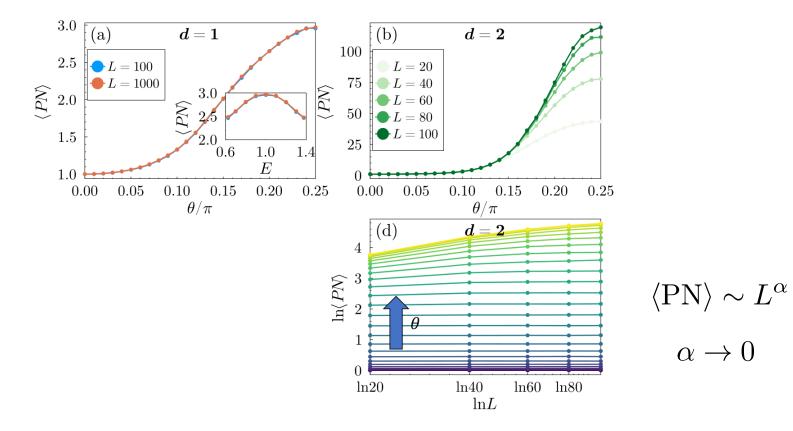
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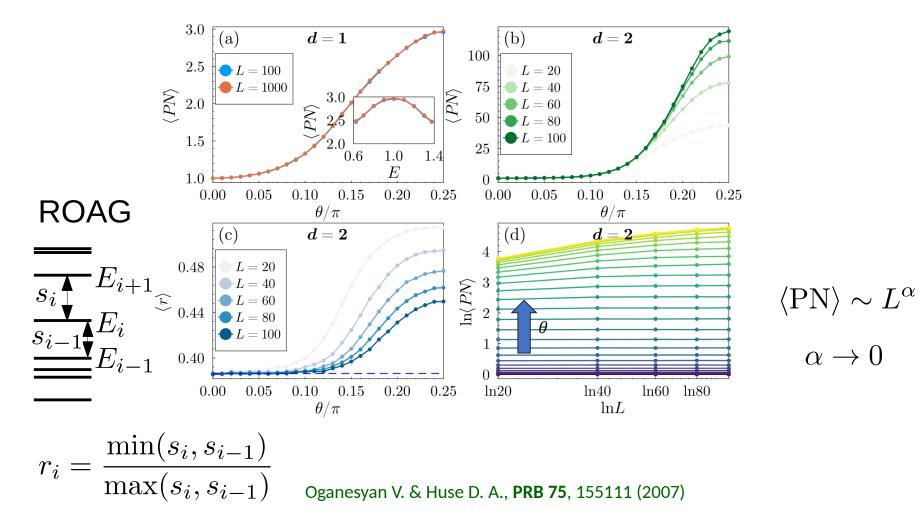
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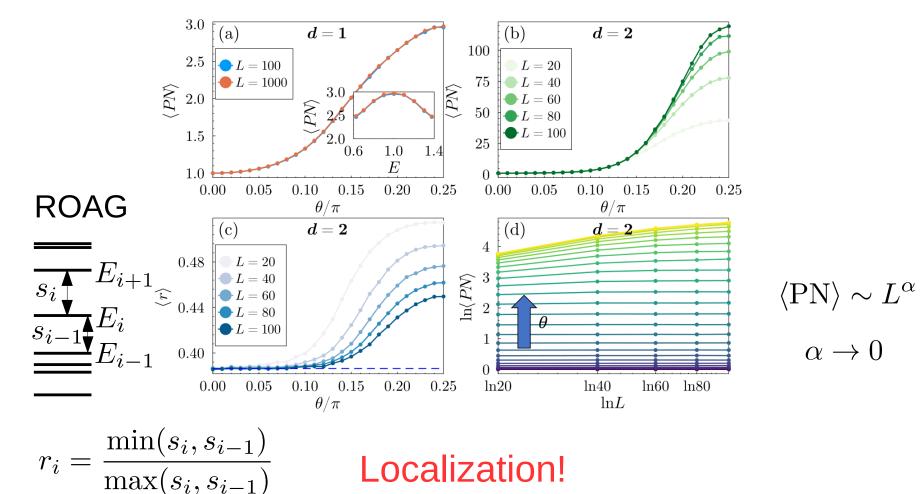
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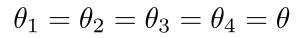


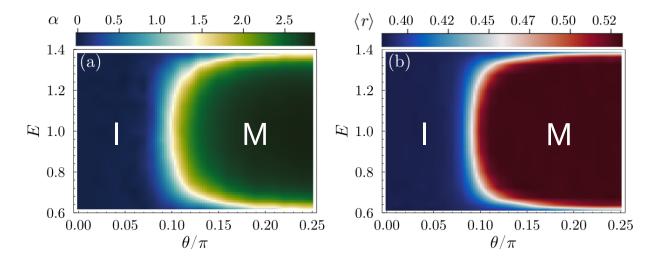
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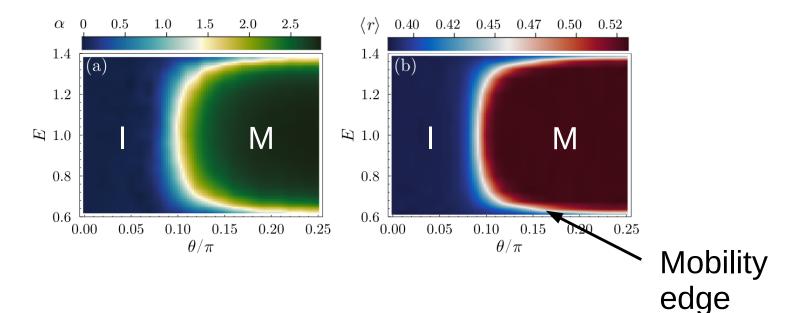
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Exact diagonalization (ED)

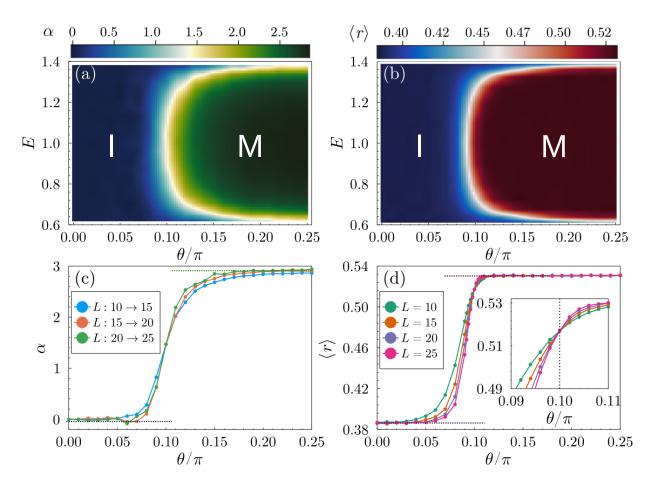




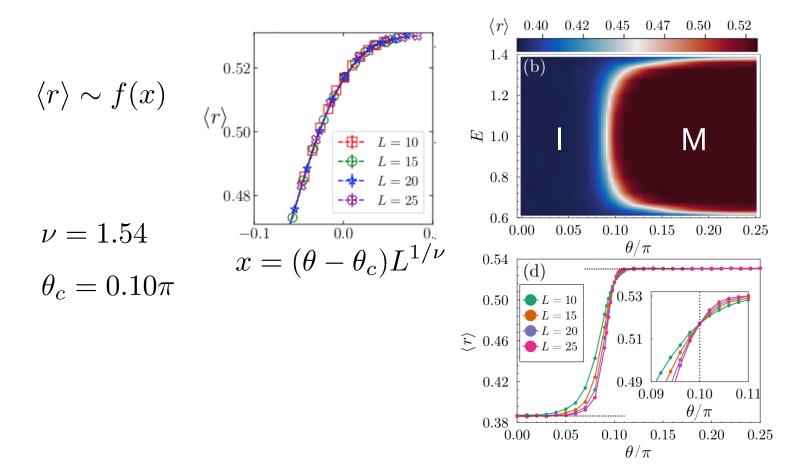
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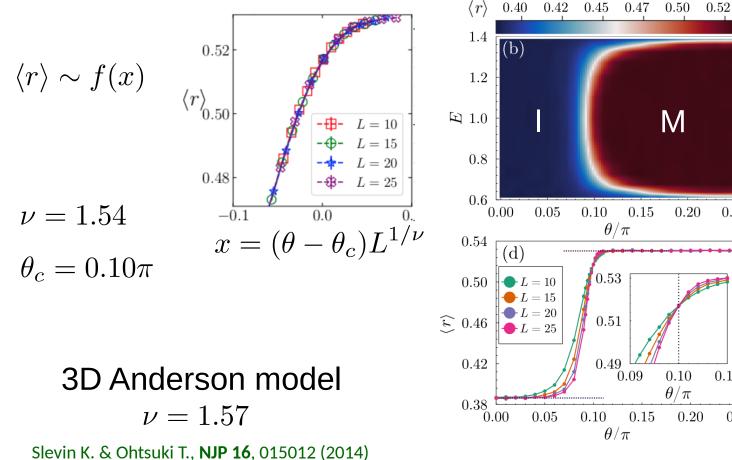
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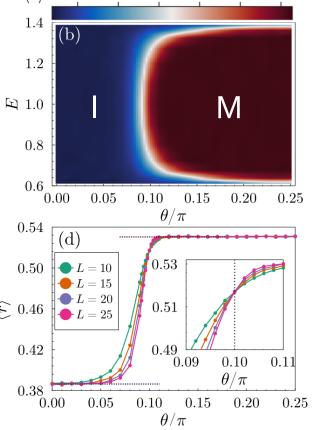


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• ν bands, LUT SU(ν) matrices, $\nu^2 - 1$ real parameters

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Conclusions:

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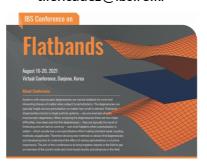
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PCS Center for Theoretical Physics of Complex Systems

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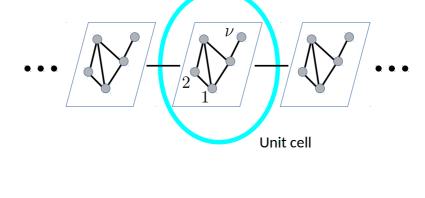
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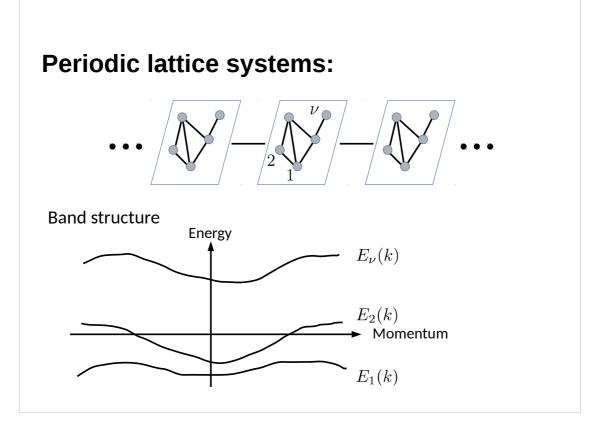
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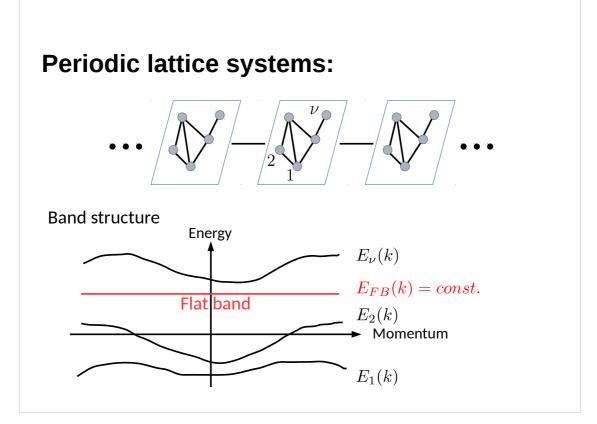
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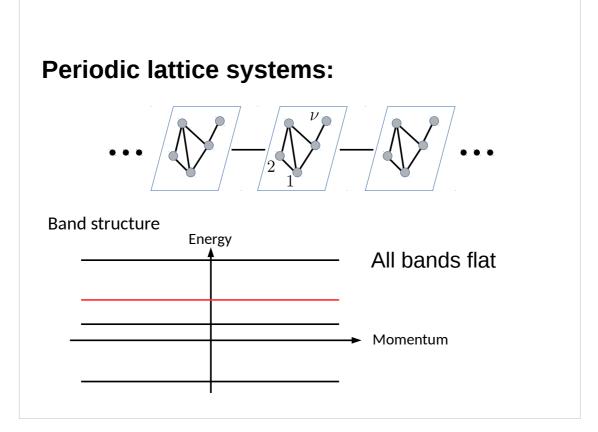
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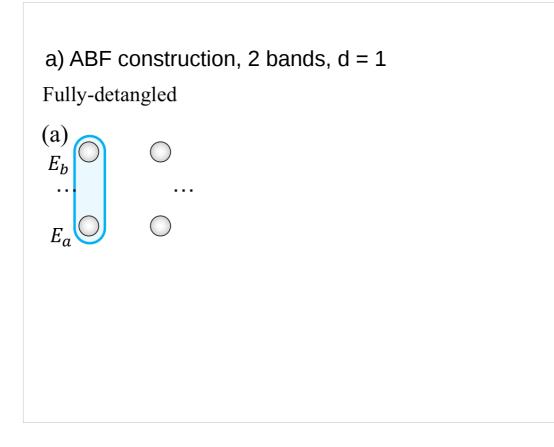
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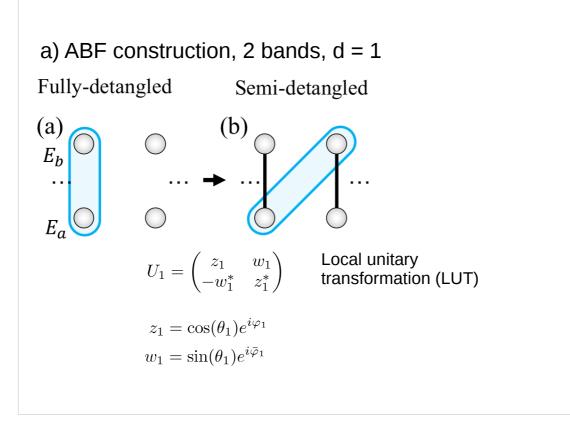


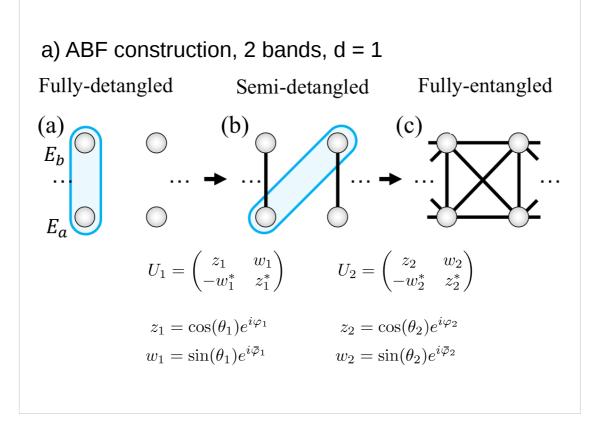


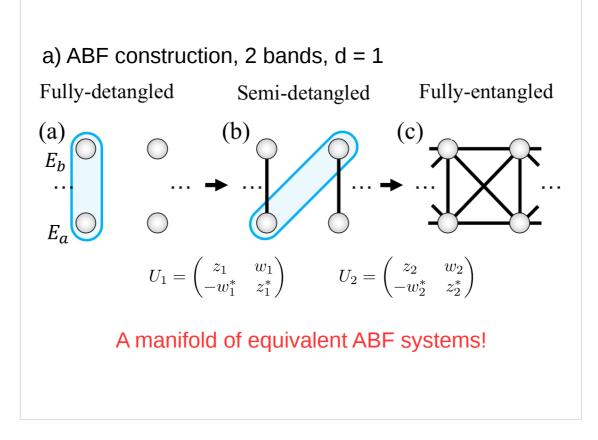


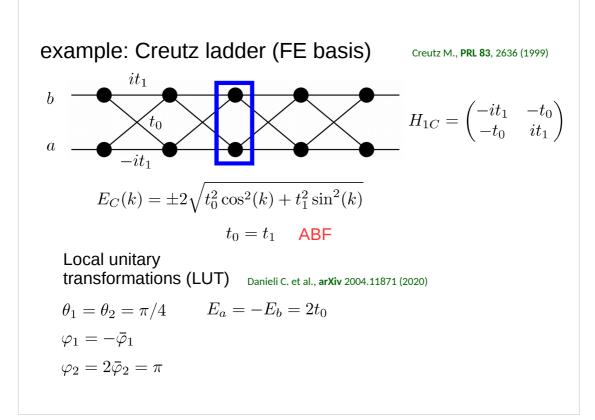


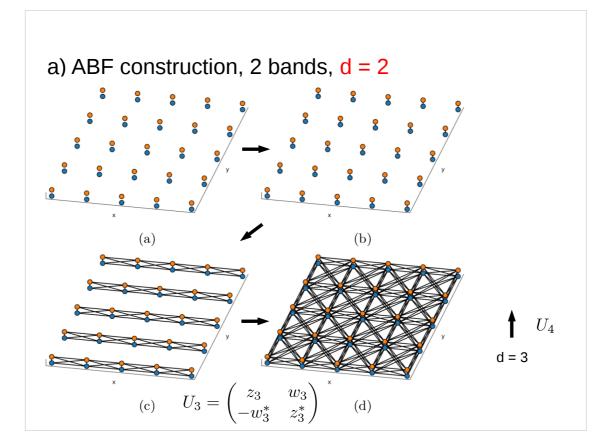


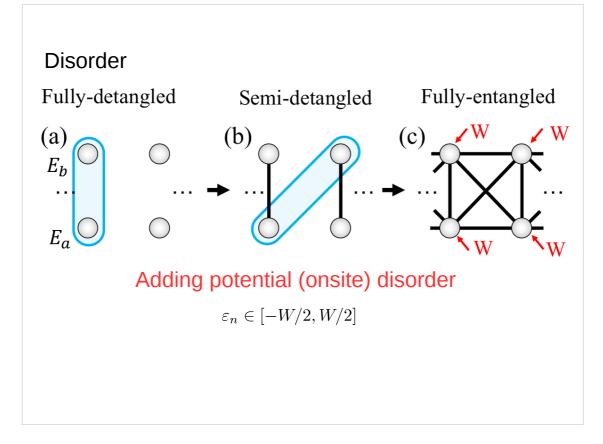


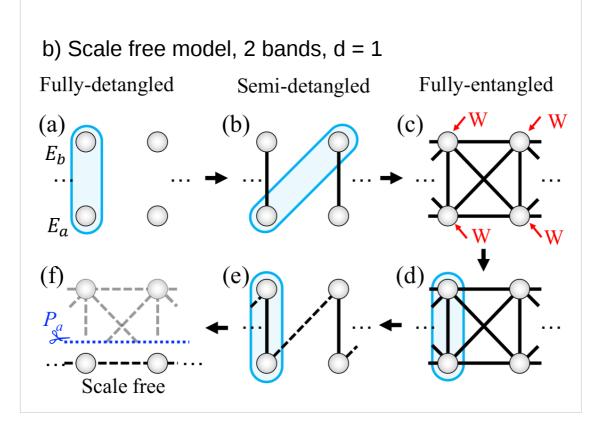


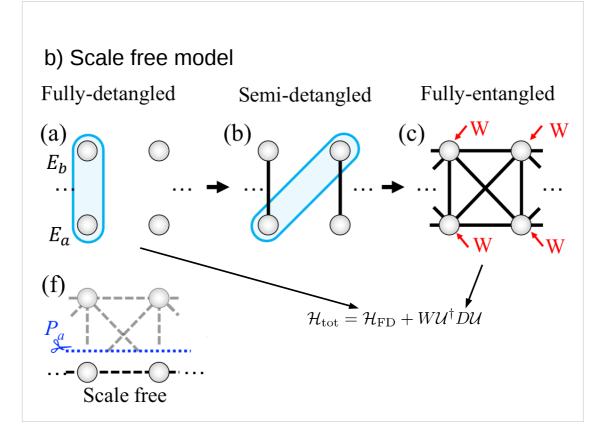


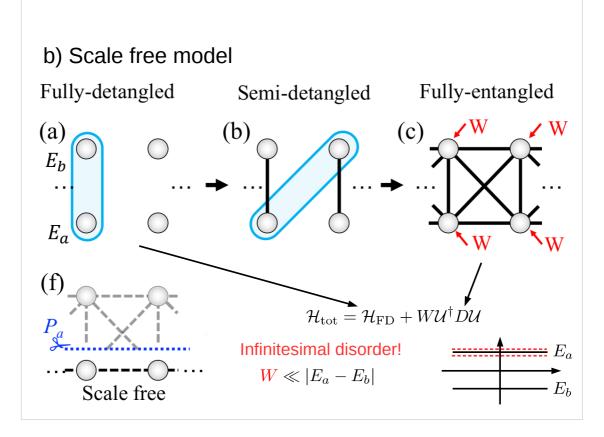


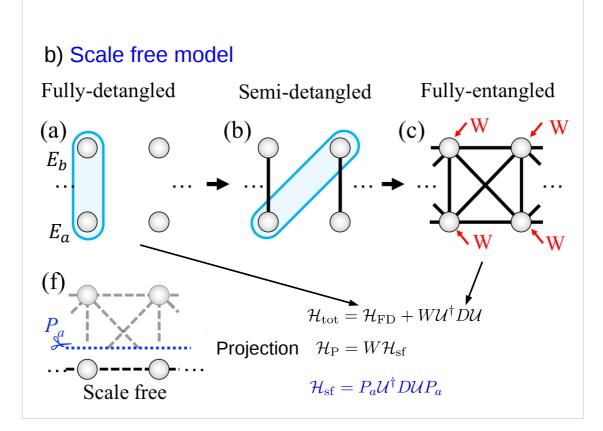












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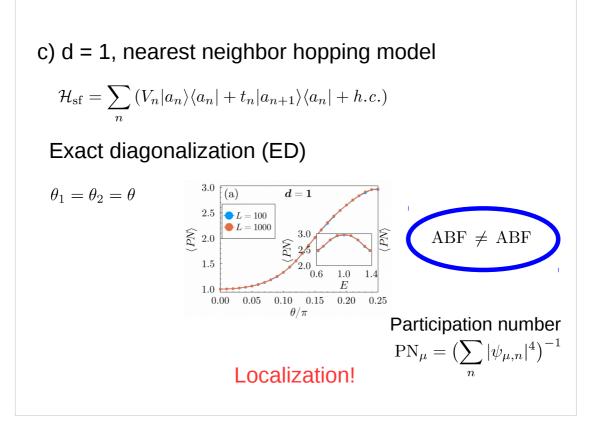
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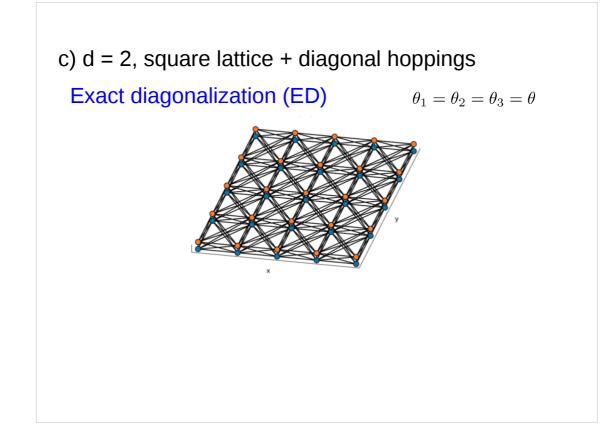
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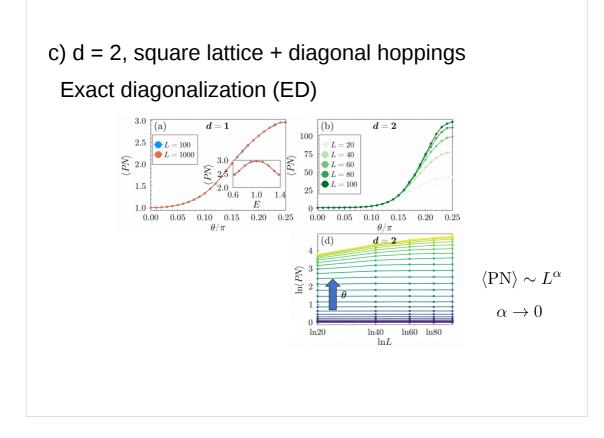
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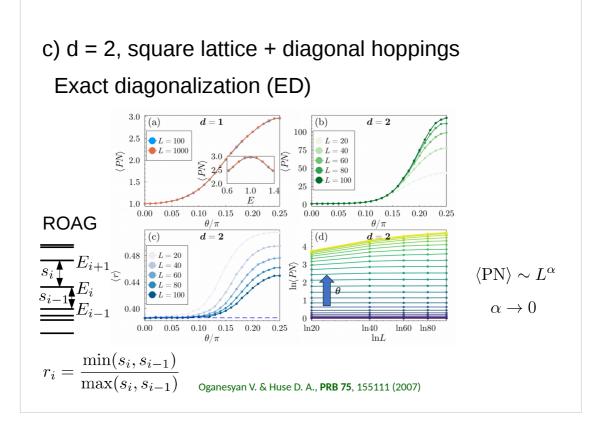
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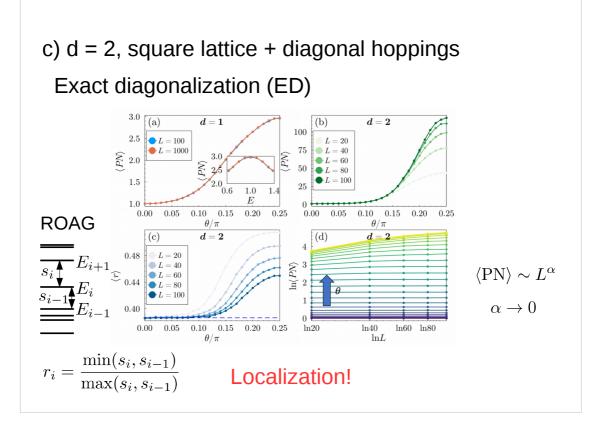
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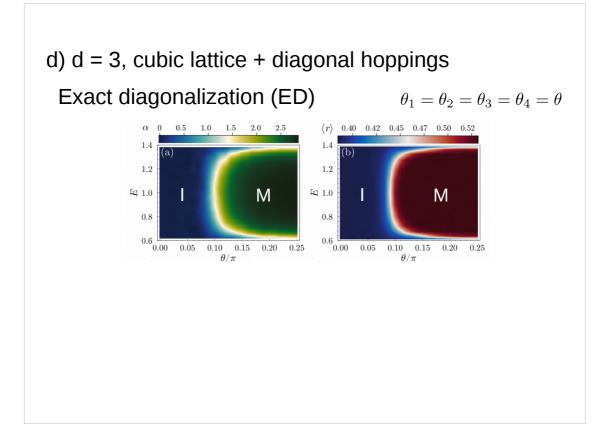


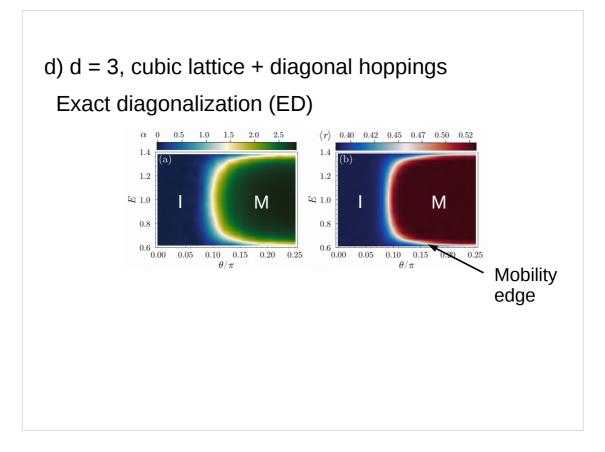


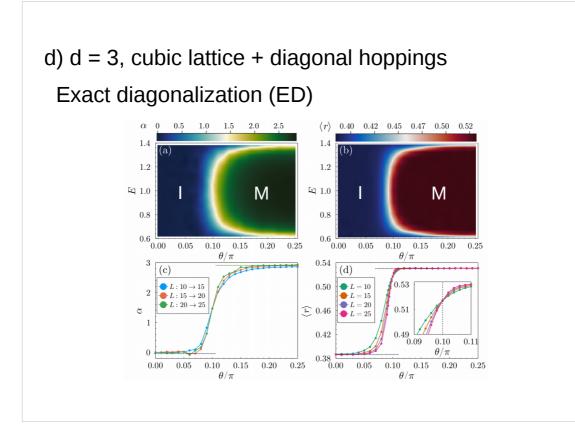


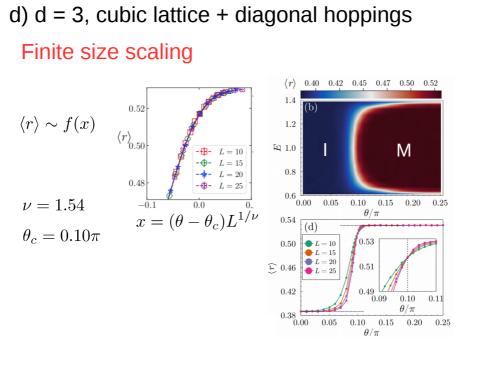


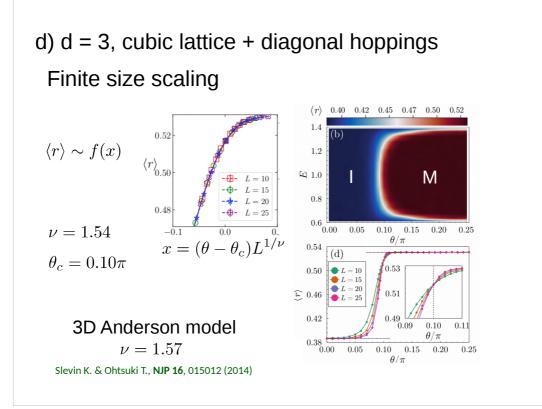












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