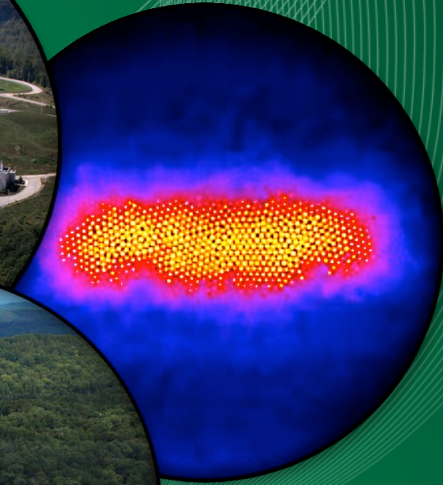
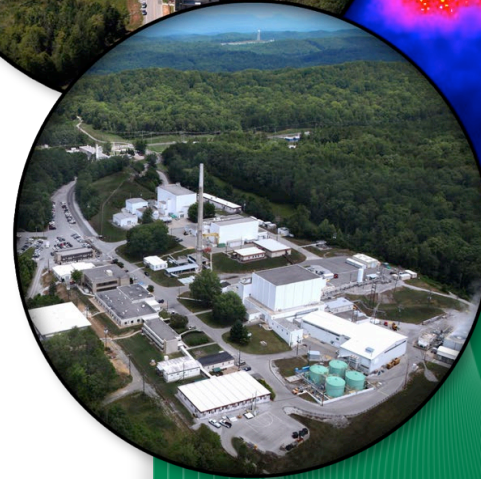


# Magnetic excitations and possible spin liquid physics in $\alpha\text{-RuCl}_3$

Stephen Nagler  
Oak Ridge National Laboratory



# Outline

I. Kitaev's model & materials

II. Ordering in  $\alpha$ - $\text{RuCl}_3$

III. Inelastic neutron scattering in  $\alpha$ - $\text{RuCl}_3$

IV. Higher fields, magnetocaloric effect, T-B phase diagram

# Neutron Scattering Collaborators:

A. Banerjee, A. Aczel, C. Balz, C. Batista, S. Bhattacharjee, C. Bridges, H. Cao, B. Chakoumakos, G. Ehlers, O. Garlea, G. Granroth, Y. Kamiya, J. Knolle, D. Kovrizhin, P. Lampen-Kelley, L. Li, Y. Liu, Z. Lu, M. Lumsden, D. Mandrus, R. Moessner, M. Stone, D. Pajerowski, A. Samarakoon, D. A. Tennant, B. Winn, J.-Q. Yan, Y. Yiu, S. Zhang.



Most recent: Christian Balz et al.,

*PRB 100 060405(R), 2019*

*MCE collaborators:*

X. Hu, S. M. Yadav, Y. Takano

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# Kitaev's model on honeycomb lattice – a special QSL

$$H_{\text{Kitaev}} = - \sum_{\gamma\text{-bonds}} K_{\gamma} S_i^{\gamma} S_j^{\gamma}$$

- Kitaev interaction: Bond-directional dependent Ising coupling
- Exactly solvable Hamiltonian
- **quantum spin liquid** ground state

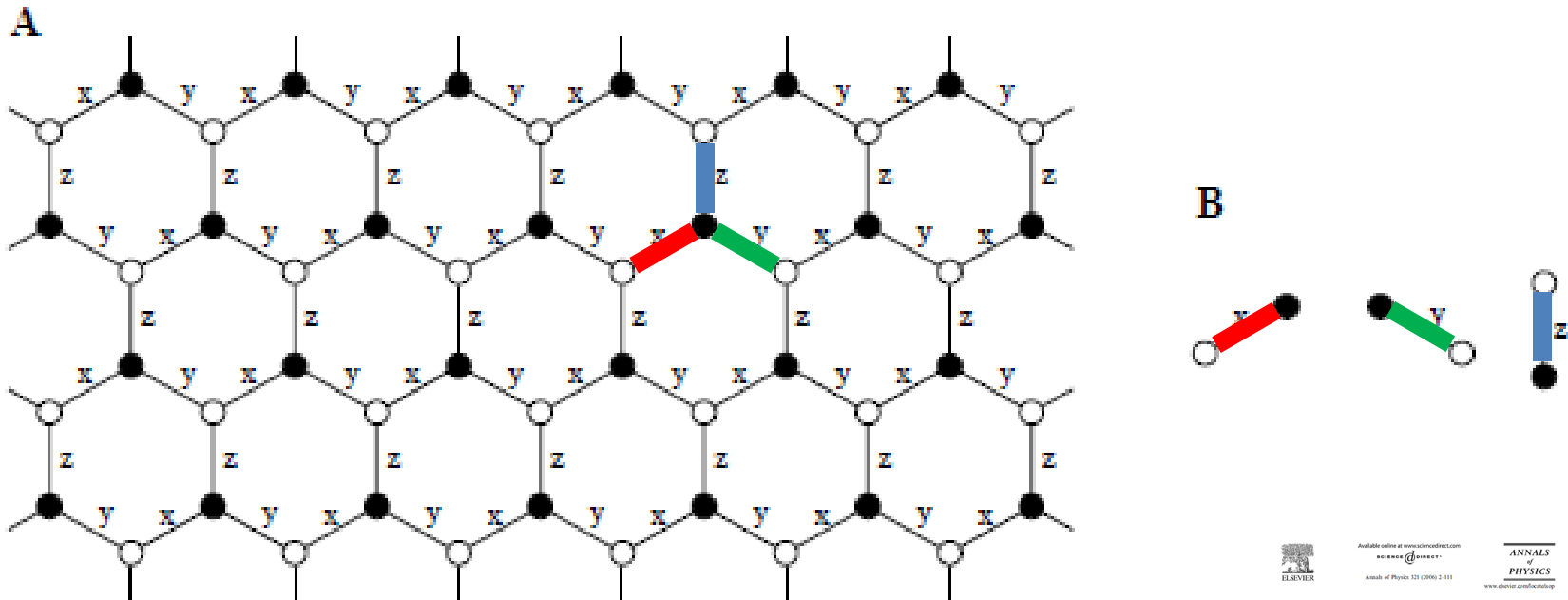


Fig. 3. Three types of links in the honeycomb lattice.



Available online at [www.elsevier.com/locate/annals](http://www.elsevier.com/locate/annals)  
 www.elsevier.com  
 Annals of Physics 321 (2006) 2–111

ANNALS  
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[www.elsevier.com/locate/annals](http://www.elsevier.com/locate/annals)

Anyons in an exactly solved model and beyond

Alexei Kitaev\*

California Institute of Technology, Pasadena, CA 91125, USA  
 Received 21 October 2005; accepted 25 October 2005

# Kitaev interactions in materials

PRL 102, 017205 (2009)

PHYSICAL REVIEW LETTERS

week ending  
9 JANUARY 2009

Mott Insulators in the Strong Spin-Orbit Coupling Limit:  
From Heisenberg to a Quantum Compass and Kitaev Models

G. Jackeli<sup>1,\*</sup> and G. Khaliullin<sup>1</sup>

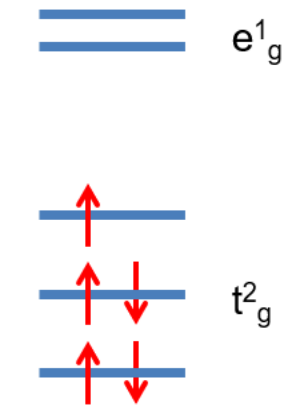
See also:

H. Takagi *et al.*,  
Nature Reviews Physics 1, (2019)

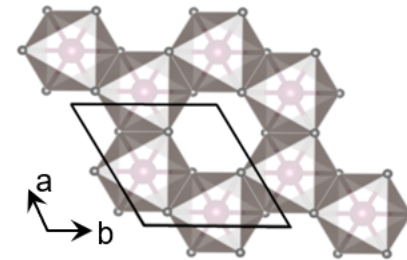
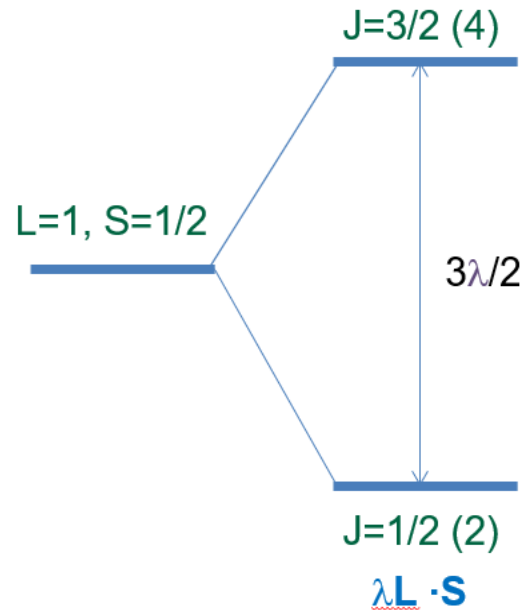
$d^5$  in low spin  
octahedral  
configuration

strong spin-  
orbit coupling

edge-sharing  
octahedra



strong field limit  
 $S=1/2, L_{\text{eff}}=1$   
e.g.  $(5d^5) \text{Ir}^{4+}$   
 $(4d^5) \text{Ru}^{3+}$



# Heisenberg – Kitaev Phase Diagram

PRL **110**, 097204 (2013)

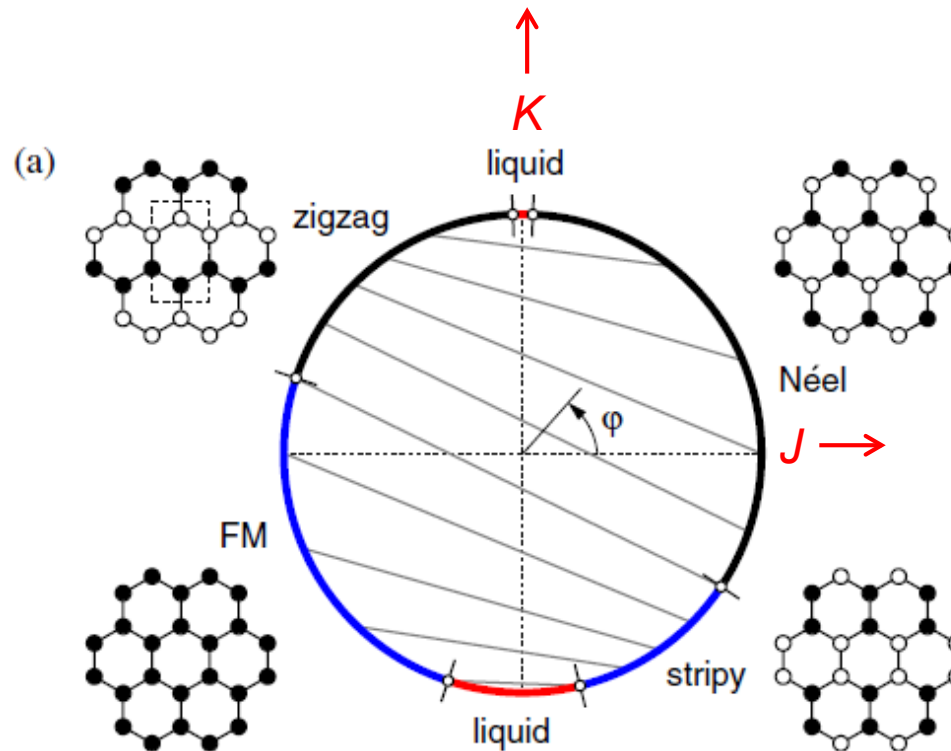
PHYSICAL REVIEW LETTERS

week ending  
1 MARCH 2013

## Zigzag Magnetic Order in the Iridium Oxide $\text{Na}_2\text{IrO}_3$

Jiří Chaloupka,<sup>1,2</sup> George Jackeli,<sup>1,\*</sup> and Giniyat Khaliullin<sup>1</sup>

$$\mathcal{H}_{ij}^{(\gamma)} = 2KS_i^\gamma S_j^\gamma + JS_i \cdot S_j.$$



# Effect of additional interactions

PRL 112, 077204 (2014)

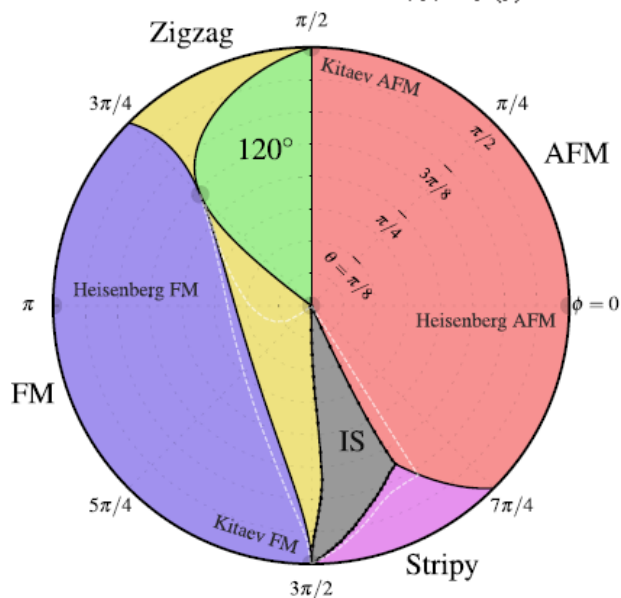
PHYSICAL REVIEW LETTERS

week ending  
21 FEBRUARY 2014

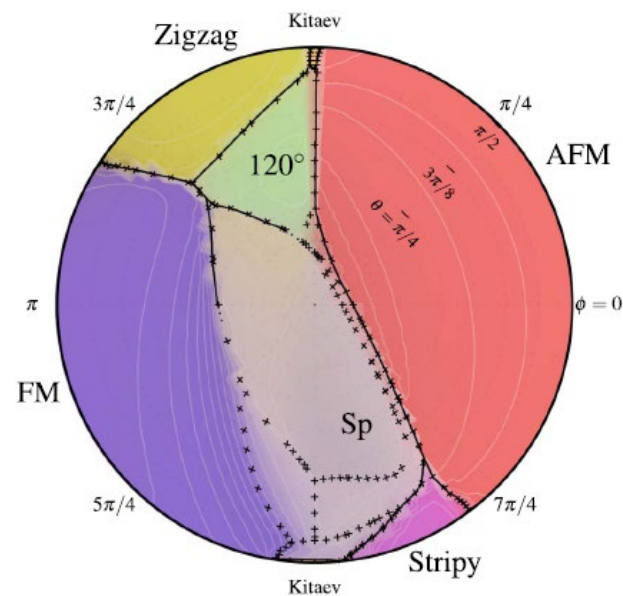
## Generic Spin Model for the Honeycomb Iridates beyond the Kitaev Limit

Jeffrey G. Rau,<sup>1</sup> Eric Kin-Ho Lee,<sup>1</sup> and Hae-Young Kee<sup>1,2,\*</sup>

$$H = \sum_{\langle ij \rangle \in \alpha\beta(\gamma)} [J\vec{S}_i \cdot \vec{S}_j + KS_i^\gamma S_j^\gamma + \Gamma(S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha)],$$



(a) Classical phase diagram with  $\Gamma > 0$



(a) Phase diagram for  $\Gamma > 0$

PHYSICAL REVIEW B 90, 155126 (2014)

Importance of anisotropic exchange interactions in honeycomb iridates: Minimal model for zigzag antiferromagnetic order in  $\text{Na}_2\text{IrO}_3$

Yuriy Szyuk,<sup>1,2</sup> Craig Price,<sup>3</sup> Peter Wölfle,<sup>1,4</sup> and Natalia B. Perkins<sup>1,2</sup>



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# $\alpha$ -RuCl<sub>3</sub> : quasi - 2D honeycomb material

- Honeycomb lattice
- Ru<sup>3+</sup> in octahedral low spin
- $J_{1/2} \rightarrow J_{3/2}$  transition  $\approx 200$  meV

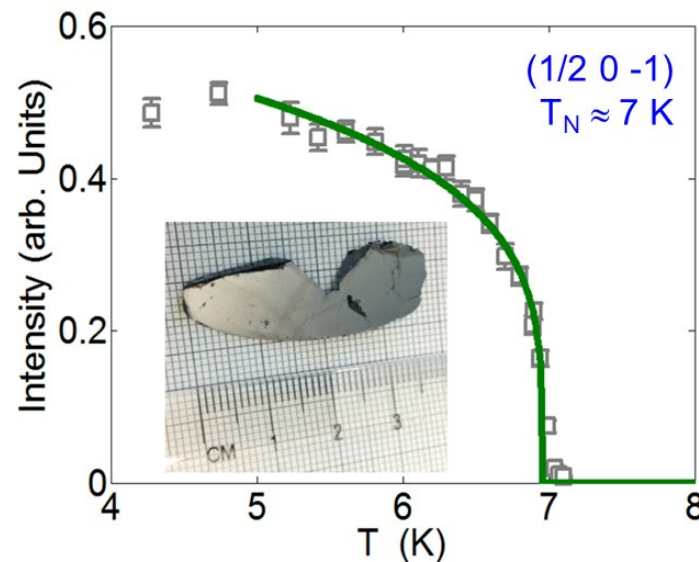
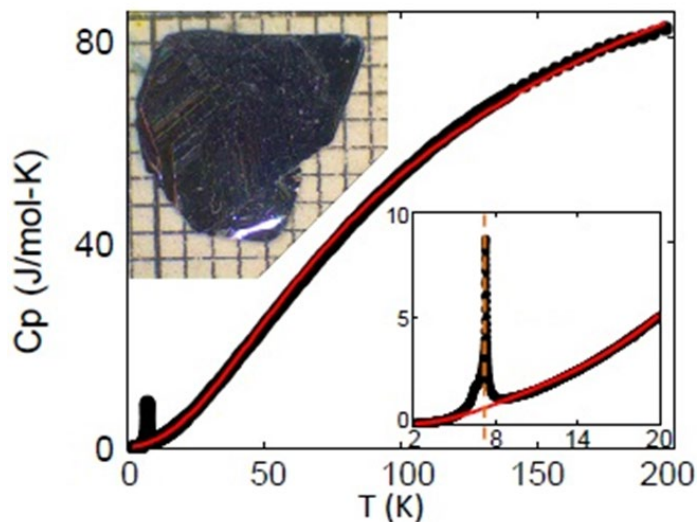
No. 4898 September 14, 1963

NATURE

## CHEMISTRY

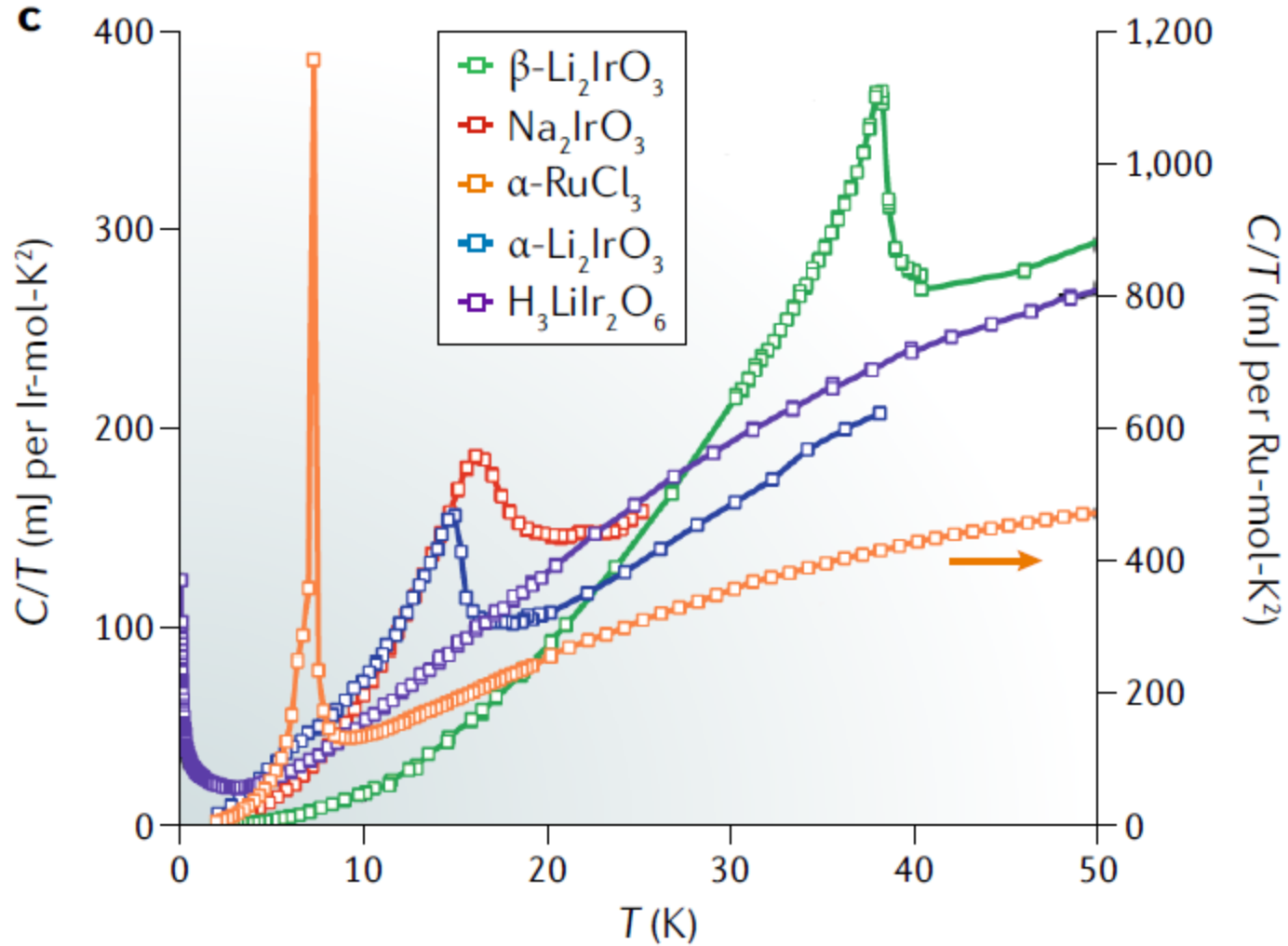
Anhydrous Ruthenium Chlorides

J. M. FLETCHER  
W. E. GARDNER  
E. W. HOOPER  
K. R. HYDE  
F. H. MOORE  
J. L. WOODHEAD

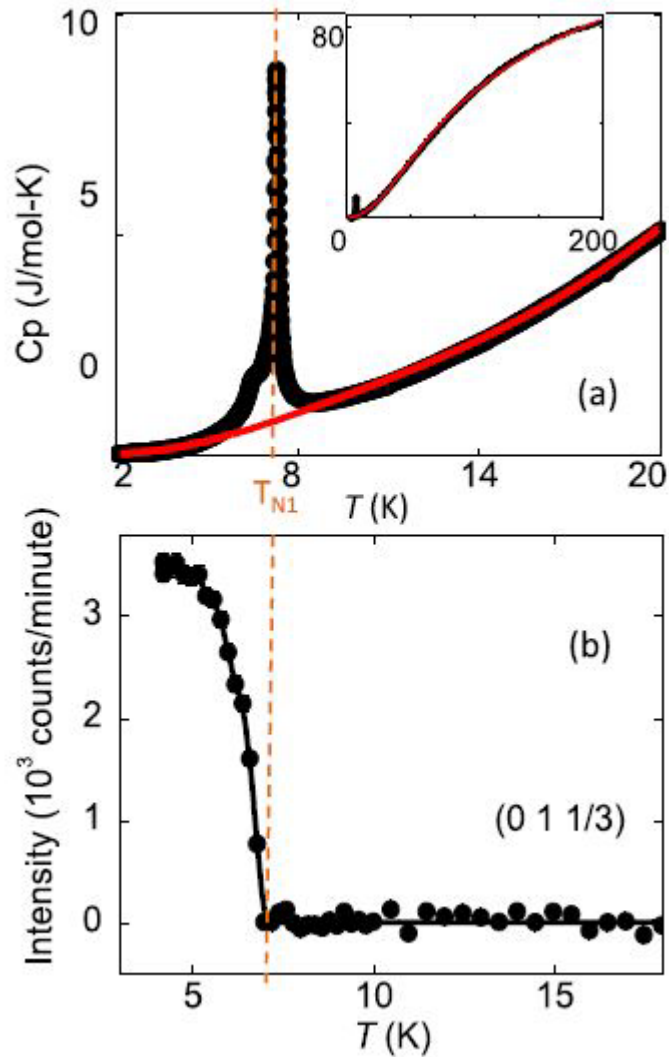


Transition to zig-zag order at  $T_N = 7$  K

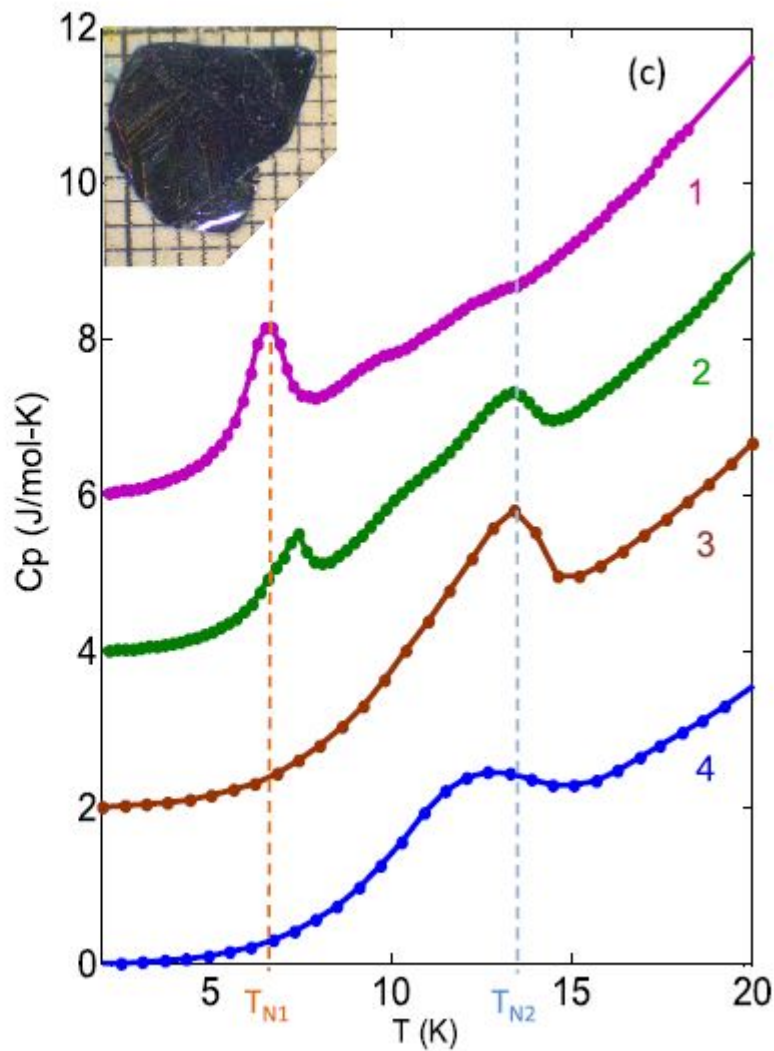
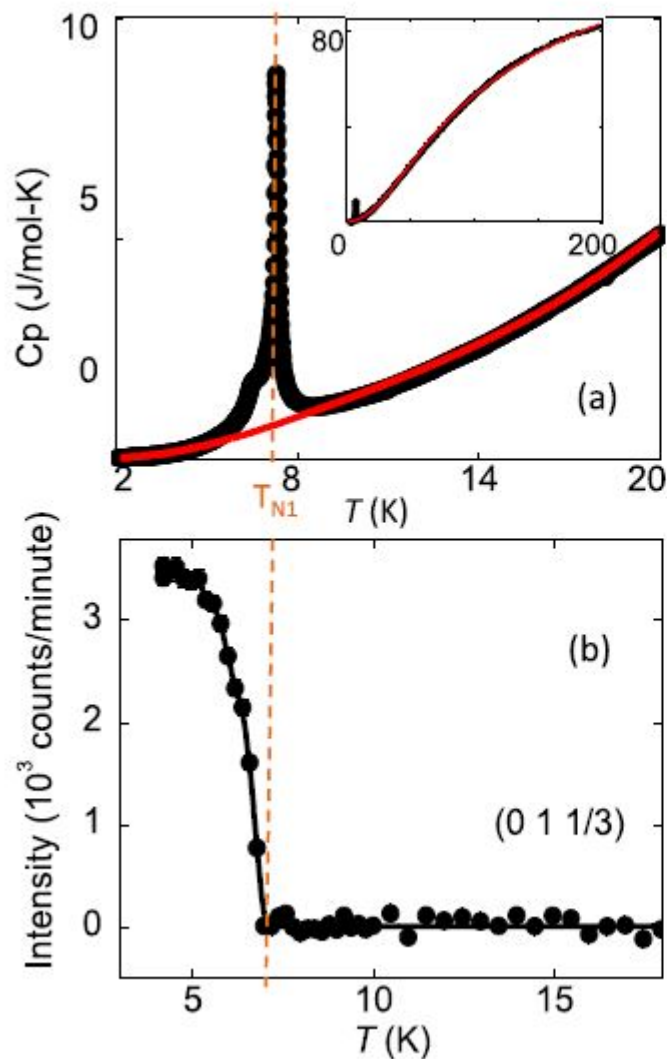
# Comparisons of specific heat



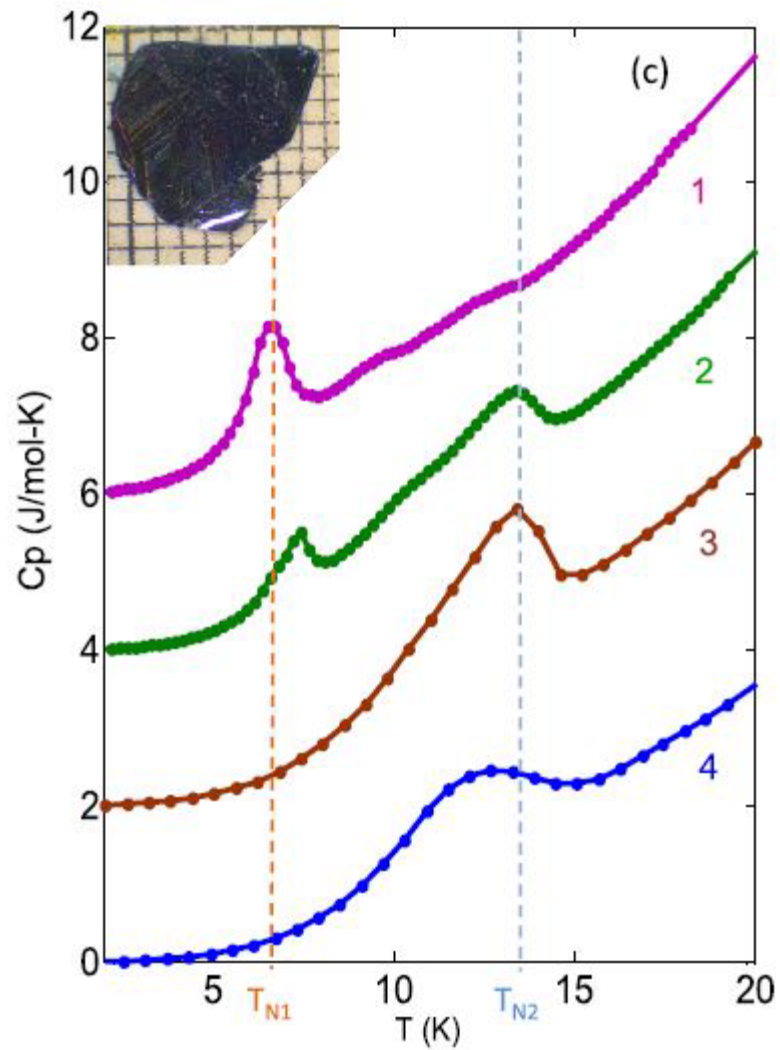
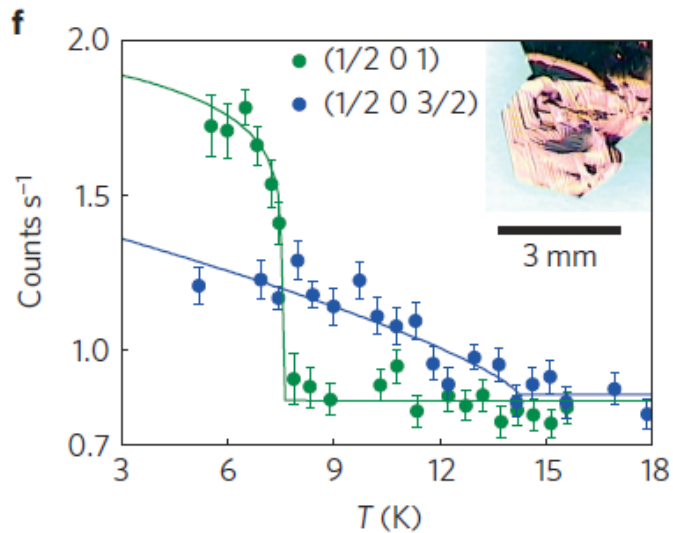
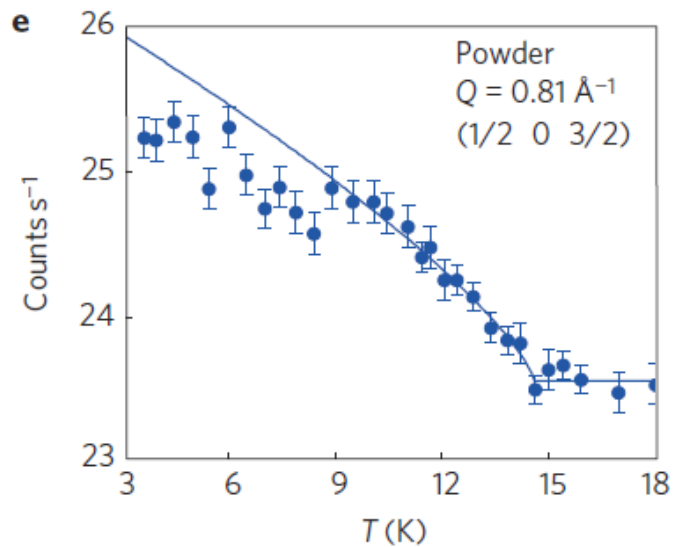
# Effect of stacking faults in $\alpha$ -RuCl<sub>3</sub>



# Effect of stacking faults in $\alpha$ - $\text{RuCl}_3$



# Stacking faults $\rightarrow$ 14 K transition



# Magnetic Field Effects

Kubota *et al.*, Johnson *et al.* showed that a modest in-plane field kills magnetic order (out of plane needs > 50 Tesla to saturate)

PHYSICAL REVIEW B **92**, 235119 (2015)

## Monoclinic crystal structure of $\alpha$ -RuCl<sub>3</sub> and the zigzag antiferromagnetic ground state

R. D. Johnson,<sup>1,2,\*</sup> S. C. Williams,<sup>1</sup> A. A. Haghighirad,<sup>1</sup> J. Singleton,<sup>3</sup> V. Zapf,<sup>3</sup> P. Manuel,<sup>2</sup> I. I. H. O. Jeschke,<sup>5</sup> R. Valentí,<sup>5</sup> and R. Coldea<sup>1</sup>

PHYSICAL REVIEW B **91**, 094422 (2015)

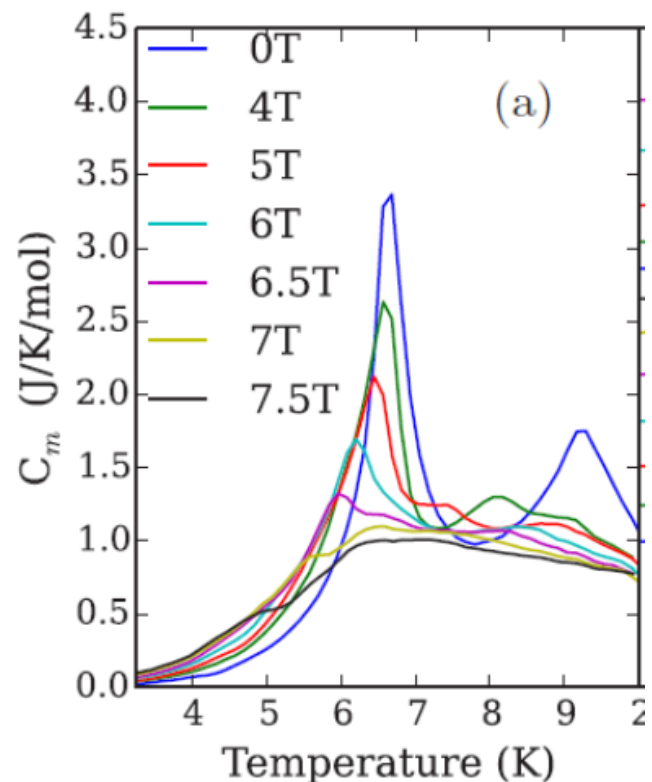
## Successive magnetic phase transitions in $\alpha$ -RuCl<sub>3</sub>: XY-like frustrated magnet on the honeycomb lattice

Yumi Kubota,<sup>1</sup> Hidekazu Tanaka,<sup>1,\*</sup> Toshio Ono,<sup>2</sup> Yasuo Narumi,<sup>3</sup> and Koichi Kindo<sup>4</sup>

PHYSICAL REVIEW B **95**, 180411(R) (2017)

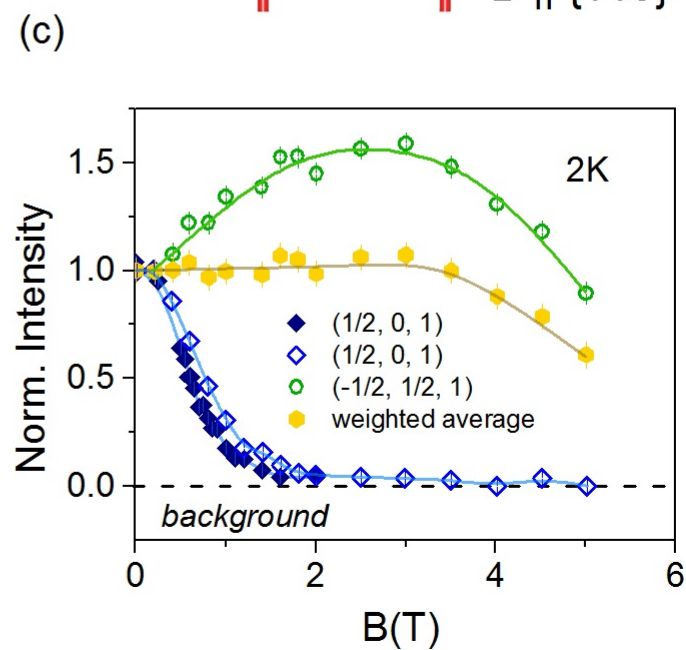
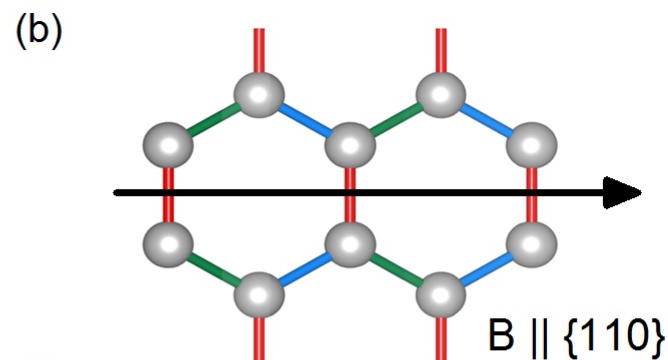
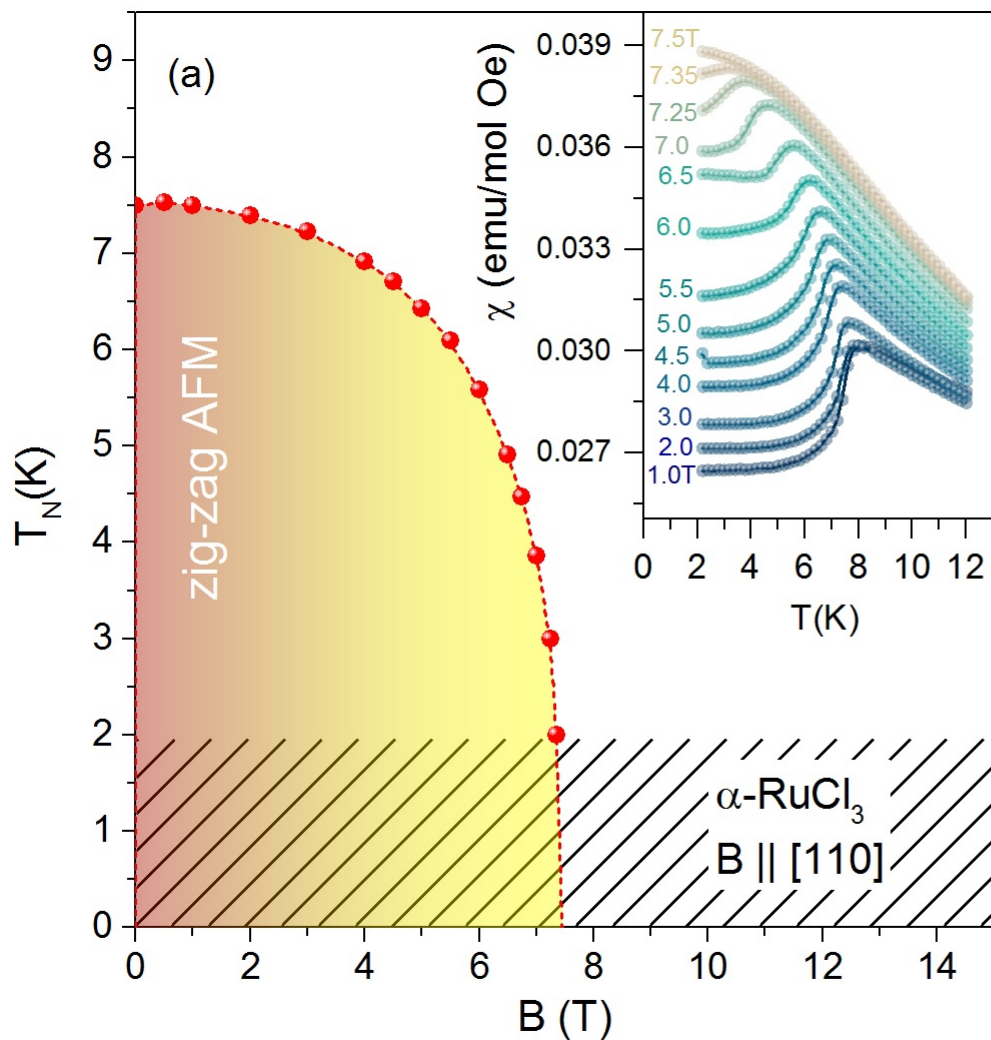
## Phase diagram of $\alpha$ -RuCl<sub>3</sub> in an in-plane magnetic field

J. A. Sears,<sup>1</sup> Y. Zhao,<sup>2,3</sup> Z. Xu,<sup>2,3</sup> J. W. Lynn,<sup>2</sup> and Young-June Kim<sup>1,\*</sup>



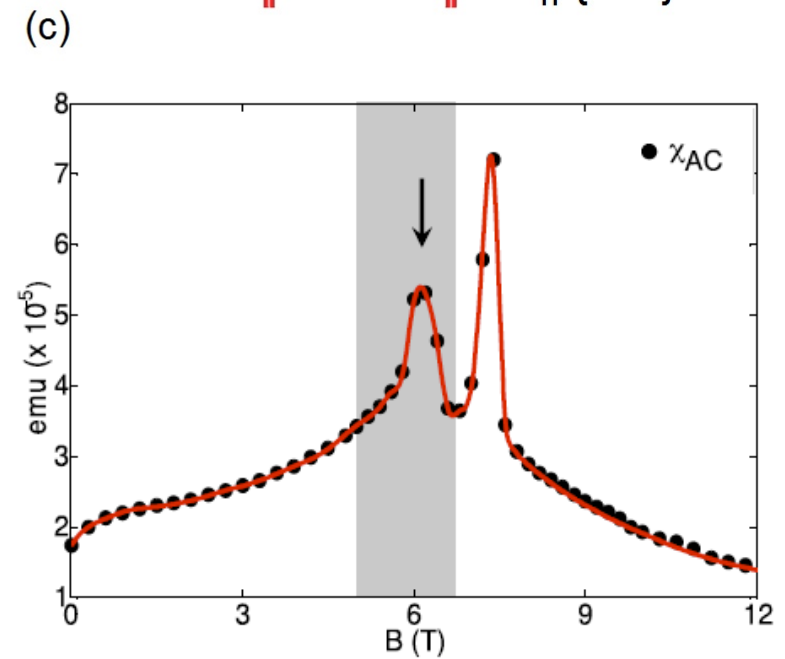
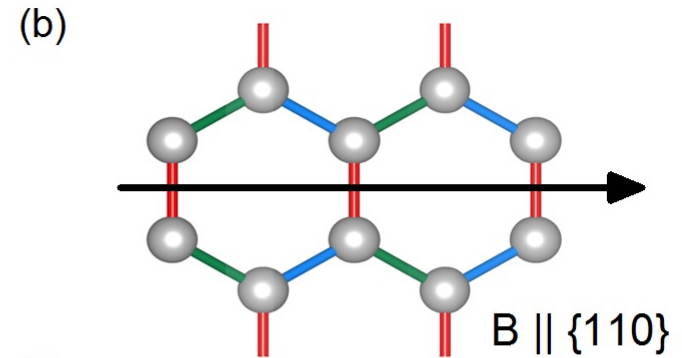
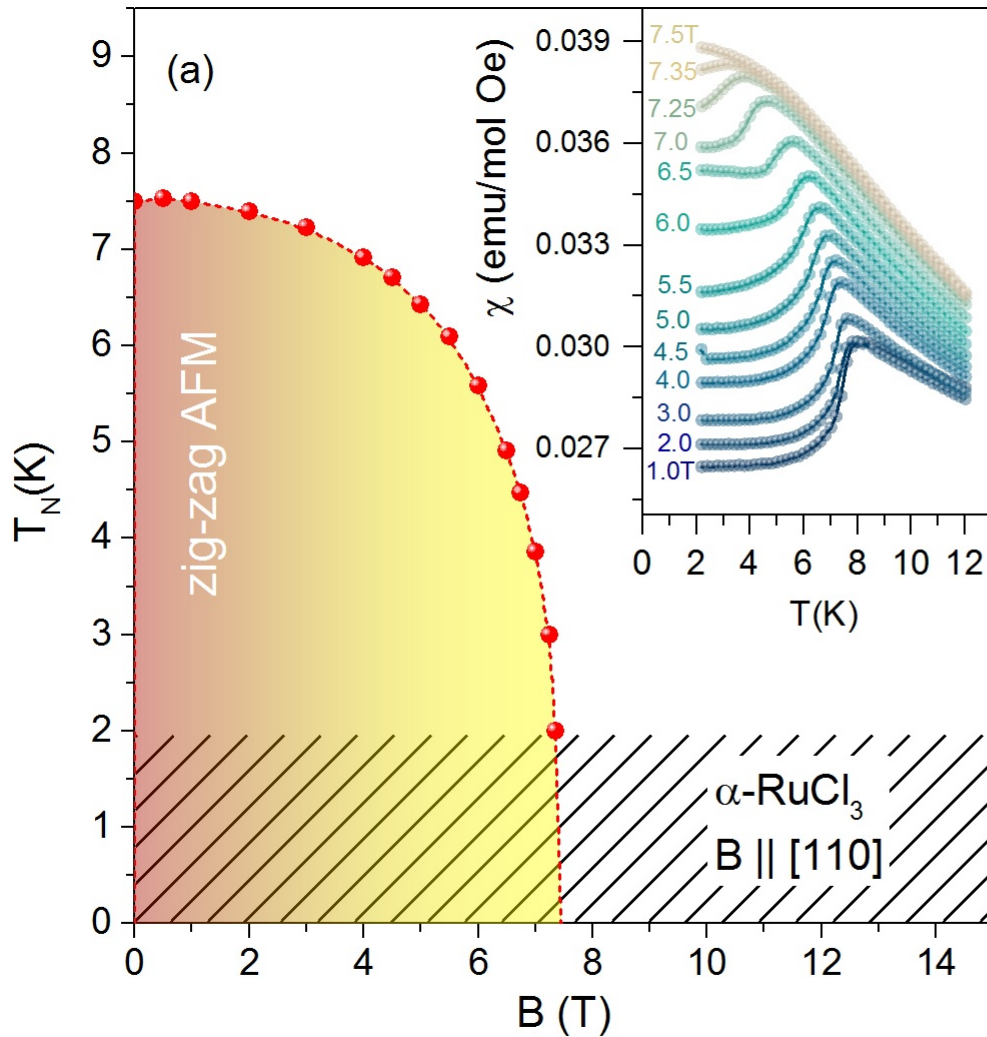
# Field dependence of $T_N$

$B_C \approx 7.3 \text{ T}$

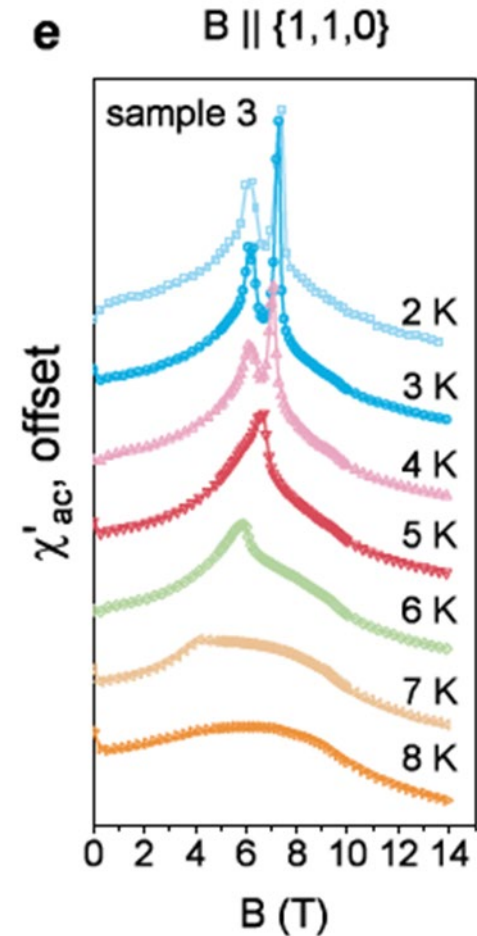
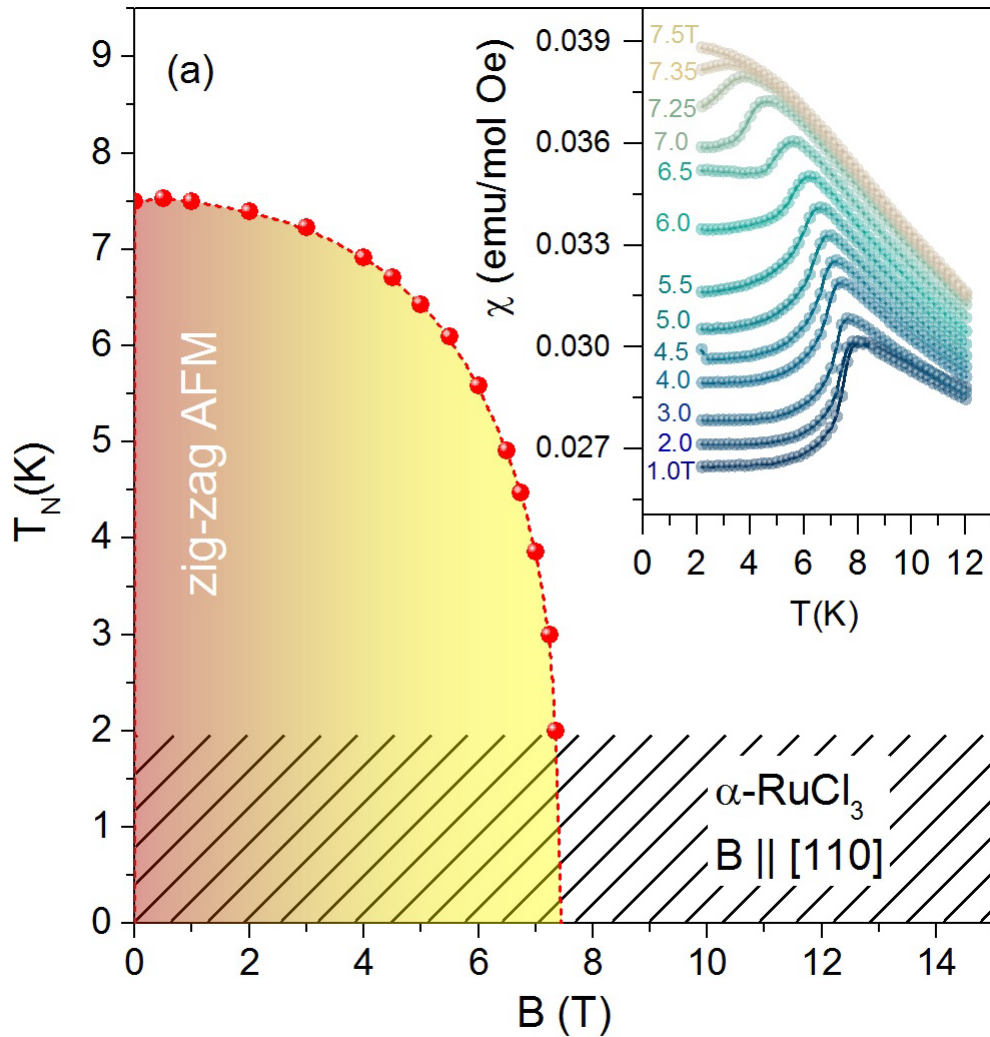




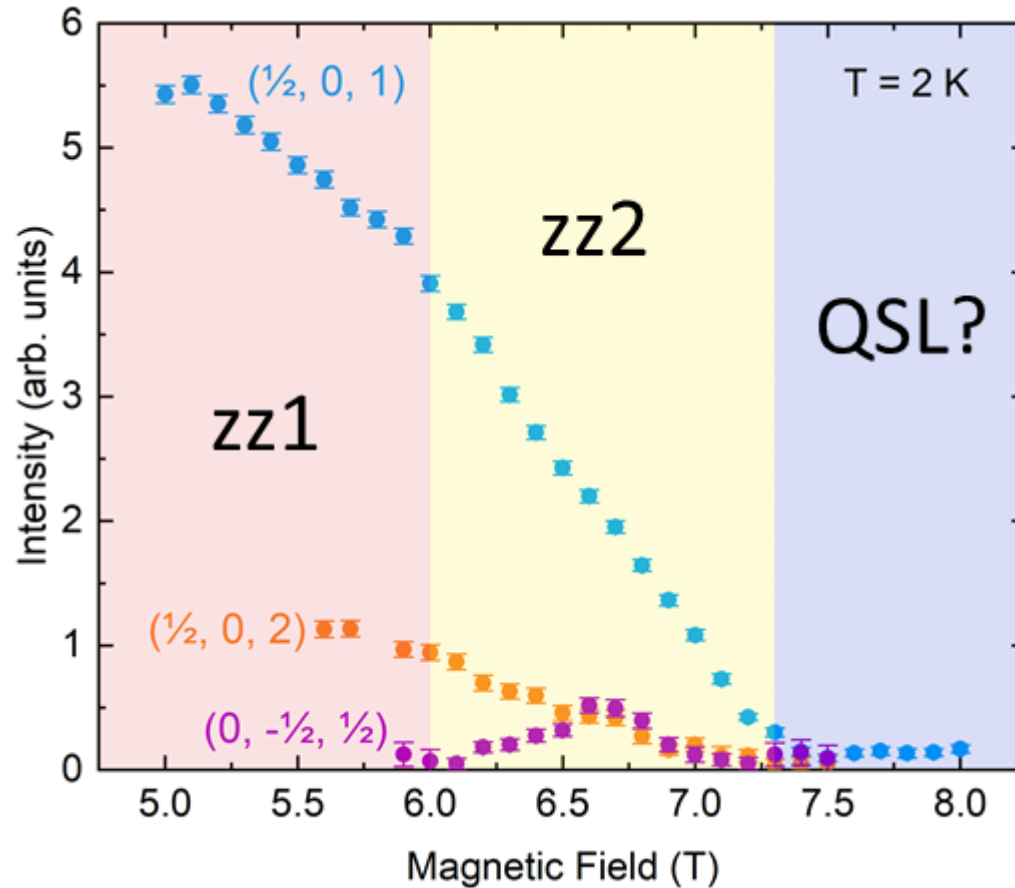
# Additional ordered phase 6 – 7.3 T



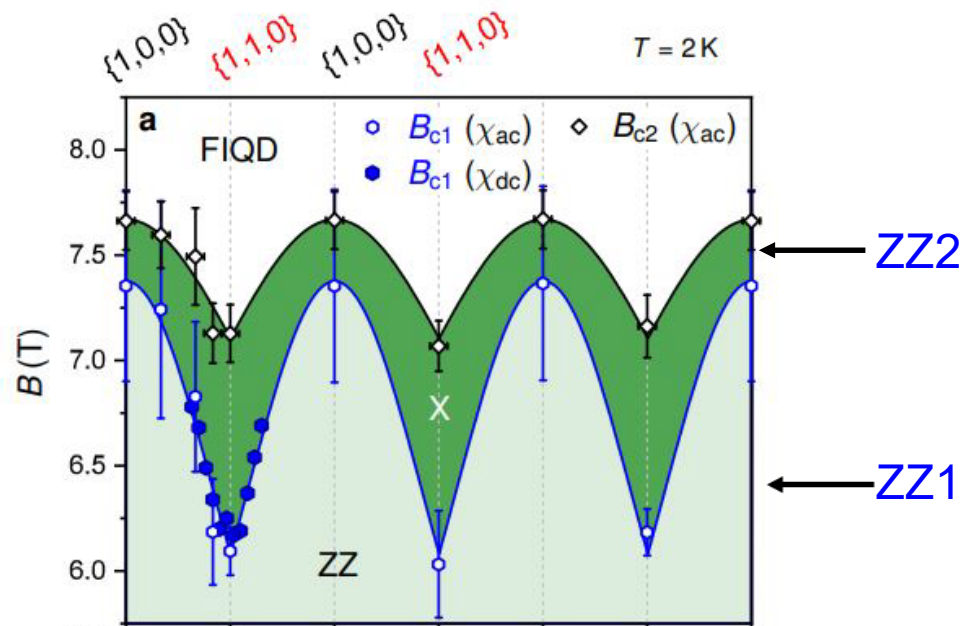
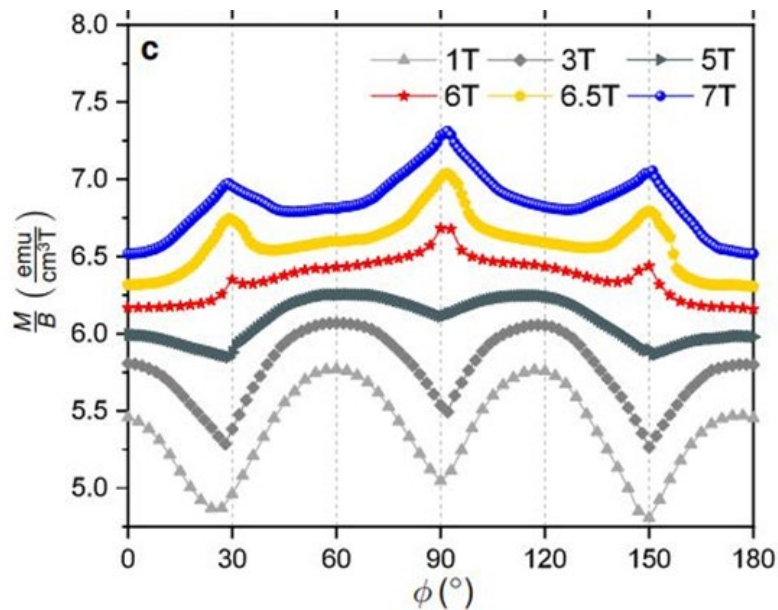
# Additional ordered phase 6 – 7.3 T



# Diffraction: 2<sup>nd</sup> zigzag w/ different stacking



# In-plane field direction dependence



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# Unpolarized neutron intensity for magnetic scattering:

$$I^{\text{mag}}(\mathbf{Q}, \omega) \propto |f(\mathbf{Q})|^2 \sum_{\alpha, \beta} \left( \delta^{\alpha\beta} - \hat{Q}^\alpha \hat{Q}^\beta \right) S^{\alpha\beta}(\mathbf{Q}, \omega)$$

magnetic form factor

magnetic structure factor

components of spin  $\alpha, \beta = x, y, z$ .

unit vector in direction of  $\mathbf{Q}$

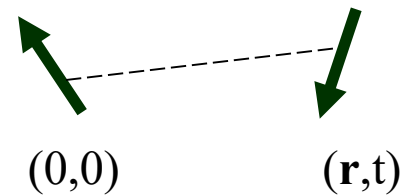
## Magnetic Structure Factor:

$$S^{\alpha\beta}(\mathbf{Q}, \omega) = \int \langle m^\alpha(0,0) m^\beta(\mathbf{r}, t) \rangle e^{i(\mathbf{Q} \cdot \mathbf{r} - \omega t)} d\mathbf{r} dt$$

$$m^\alpha = L^\alpha + 2S^\alpha$$

$$S^{\alpha\beta}(\mathbf{Q}, \omega) \propto \text{Im} \{ \chi^{\alpha\beta}(\mathbf{Q}, \omega) \}$$

Fluctuation dissipation theorem



For magnons usually  $S(\mathbf{Q}, \omega) \propto \delta(\omega - \omega_{\mathbf{Q}})$

# Exactly solvable quantum spin system

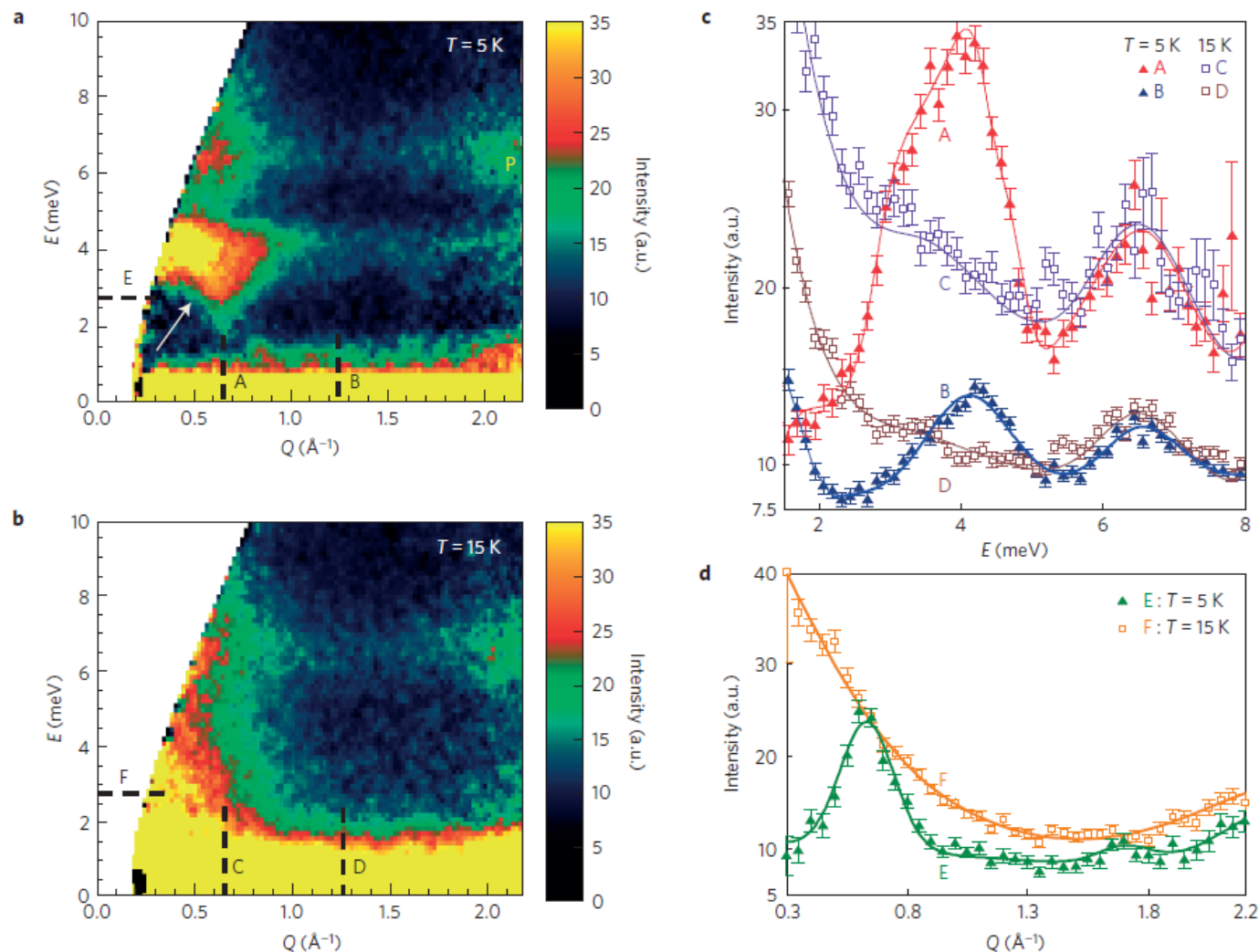
$$T=0: \quad S^{\alpha\alpha}(\vec{Q}, \omega) = \sum_E \left| \langle E | S_{\vec{Q}}^{\alpha} | G \rangle \right|^2 \delta(\omega - E)$$

$$T>0: \quad S^{\alpha\alpha}(\vec{Q}, \omega) = Z^{-1} \sum_{E, E'} e^{-\beta E} \left| \langle E' | S_{\vec{Q}}^{\alpha} | E \rangle \right|^2 \delta(\omega + E - E')$$

$$\text{where } Z = \sum_E e^{-\beta E} \quad \text{and} \quad S_{\vec{Q}}^{\alpha} = \sum_{\vec{R}} S_{\vec{R}}^{\alpha} e^{-i\vec{Q} \cdot \vec{R}}$$

Neutron scattering is sensitive to matrix elements where  $\Delta S$  or  $\Delta L = 0, \pm 1$

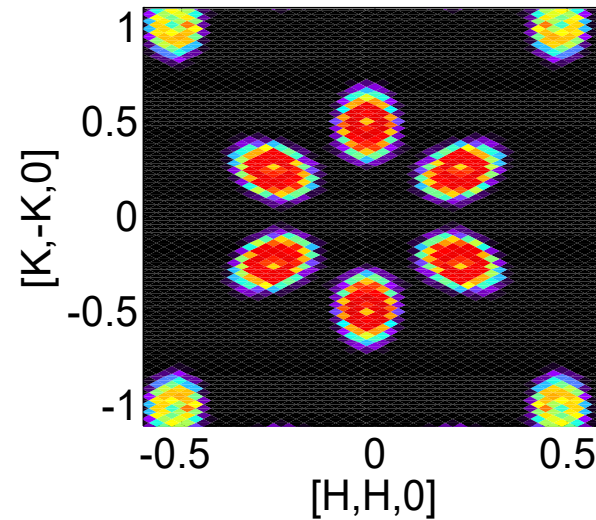
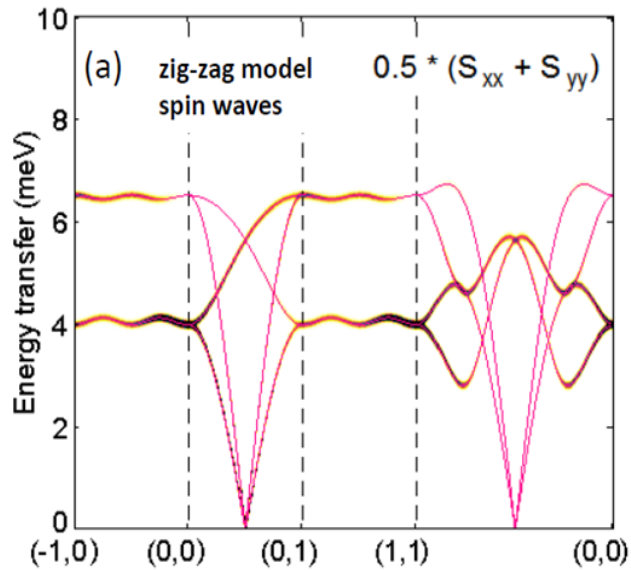
# $\alpha$ -RuCl<sub>3</sub> powder – inelastic neutron scattering



Nature Materials **15**, 733 (2016).



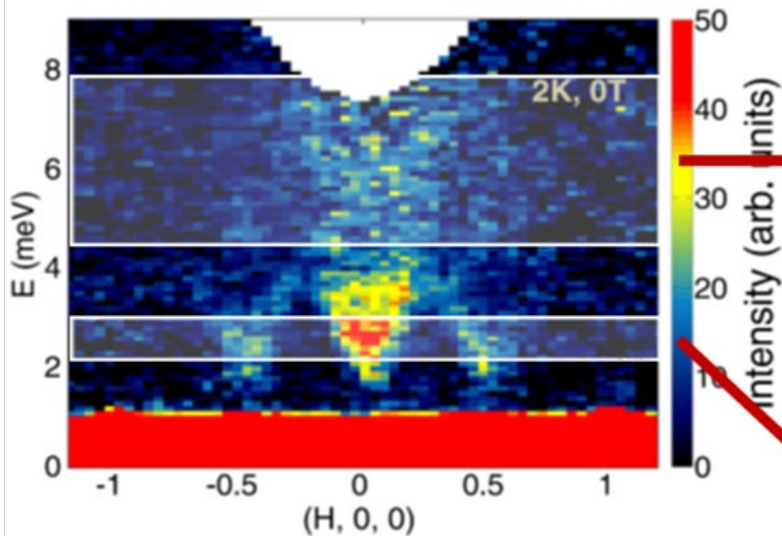
# Expectations for spin waves in a zigzag state



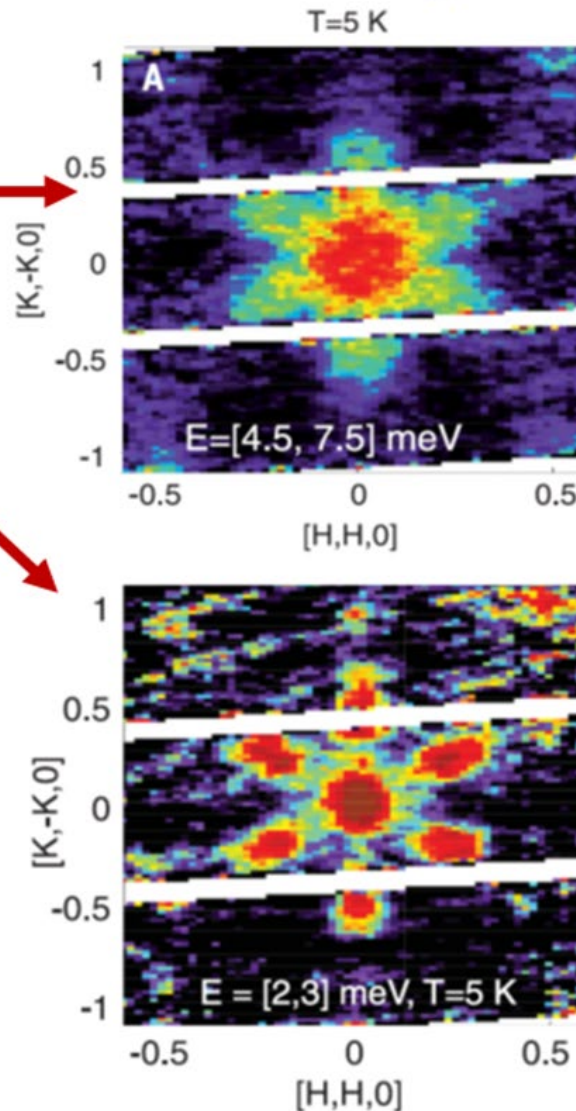
- Dispersion minima at ordering wavevectors (M points)
- Low energy constant E slices show cone shaped dispersion surfaces around the M points
- Less general, but true for Heisenberg-Kitaev model:  
     $\Gamma$  points show flat modes sharp in energy

# $\alpha$ -RuCl<sub>3</sub> single crystal - INS

Energy vs wavevector slice



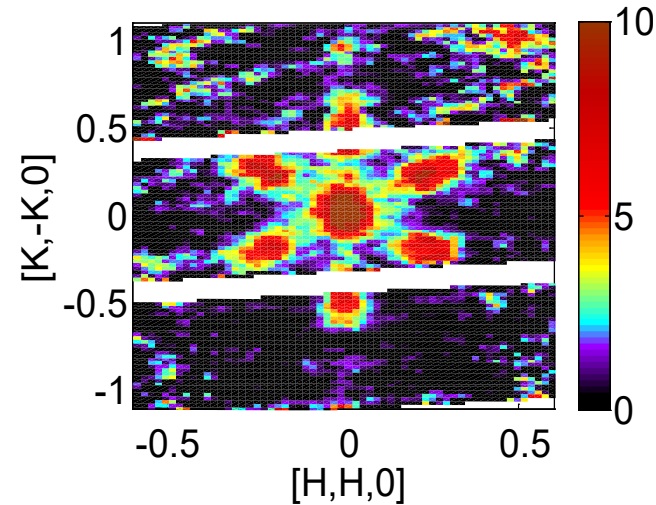
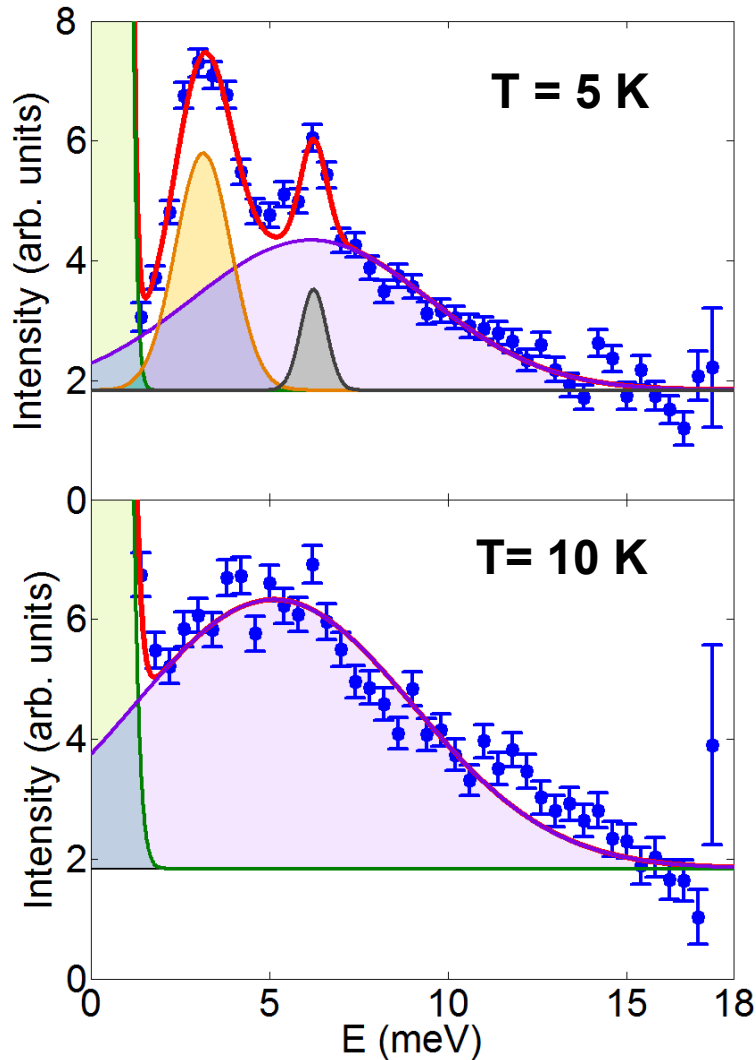
Constant energy slice



Zero field excitations:

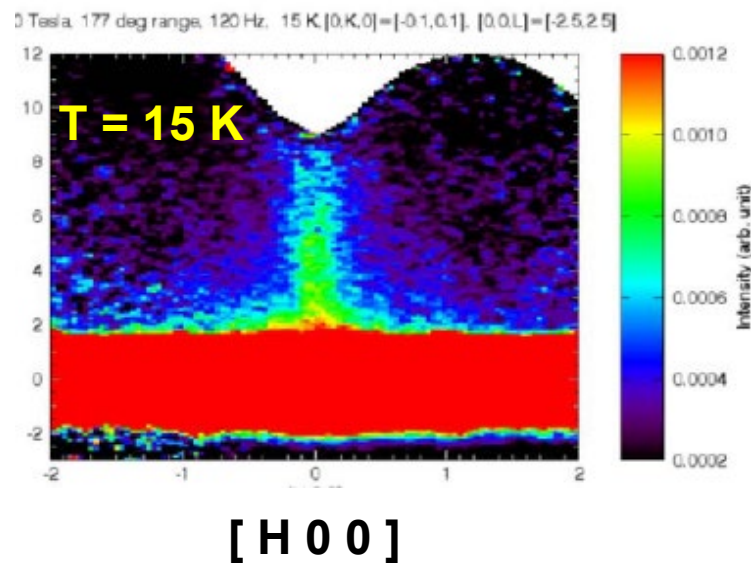
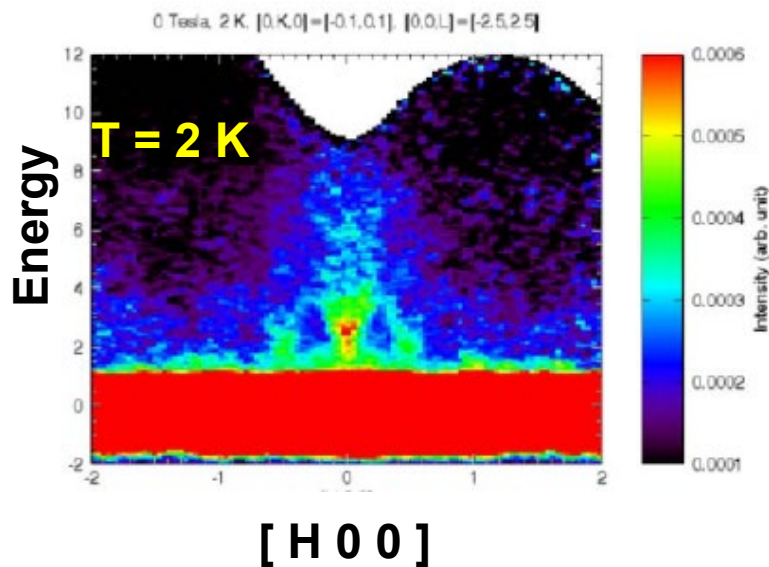
- Low energy, gapped spin waves.
- Superimposed on broad continuum at  $\Gamma$ -point

# Experiment: $\Gamma$ point signal inconsistent with SW



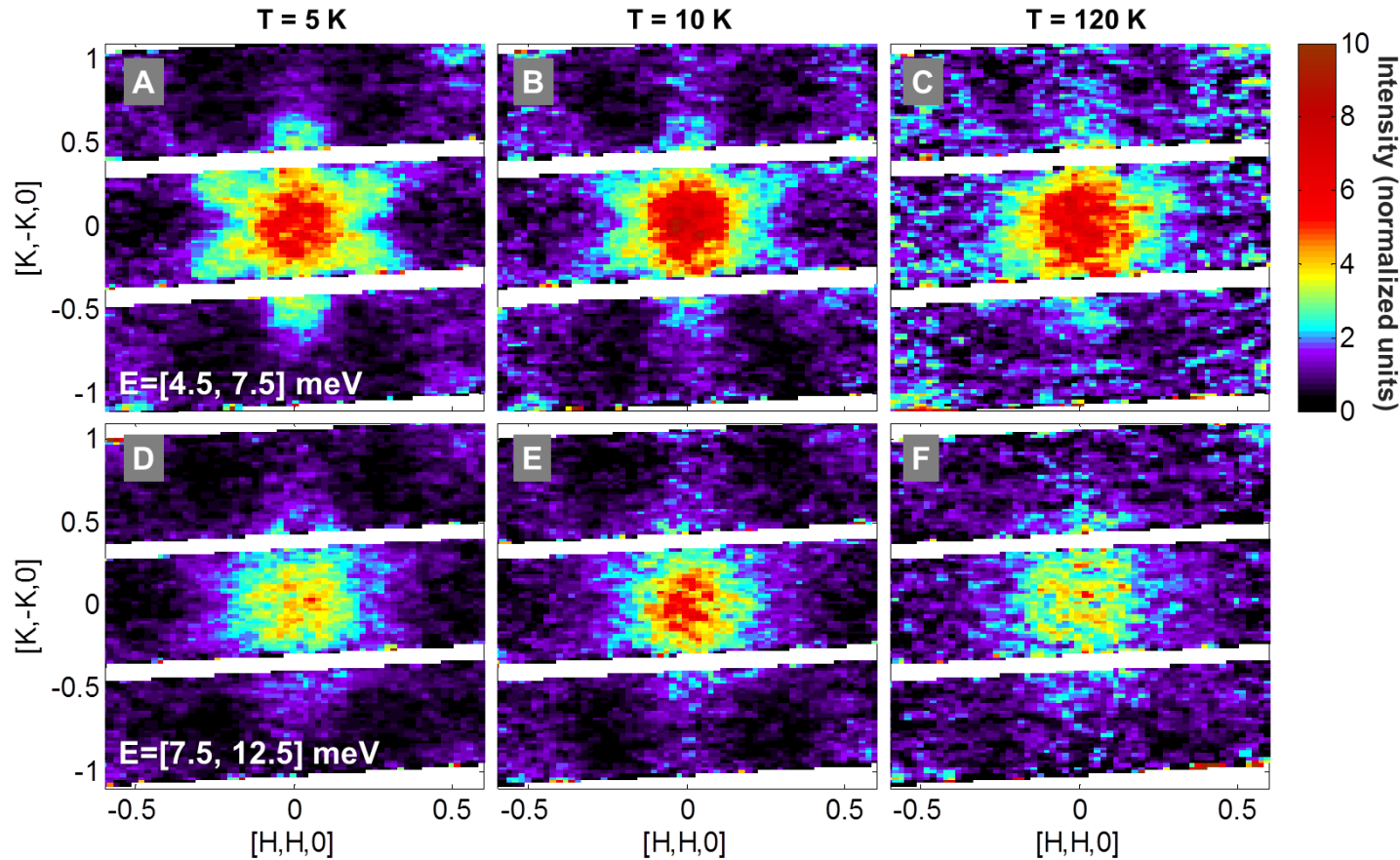
- Below TN -  $\Gamma$  point shows spin waves plus continuum
- Above TN – only continuum remains
- Large sustained continuum at  $\Gamma$  is absent in spin wave theory

# Scattering through the Brillouin zone



- At  $T_N \approx 7$  K the spin waves disappear throughout the Brillouin zone
- Above  $T_N$  the continuum near the  $\Gamma$  point persists

# Q,T dependence of the continuum scattering

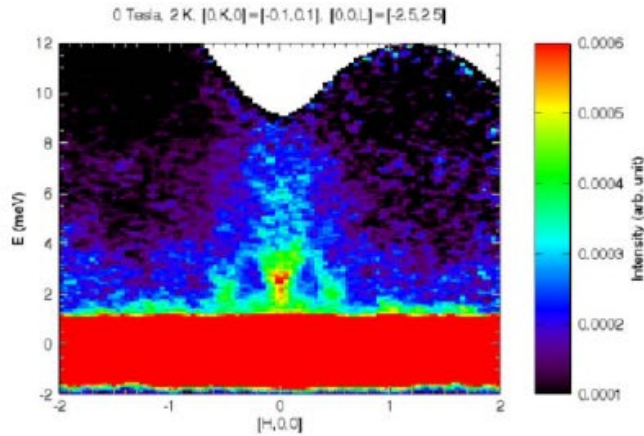


- circular column centered on  $H=K=0$ , extending to higher energies
- at low  $T$ , moderate energy SW peaks and column merge and scattering resembles a six pointed Star of David
- scattering persists to high  $T$

# How does field affect the magnetic excitations?

- Does killing order with an applied field lead to a QSL?

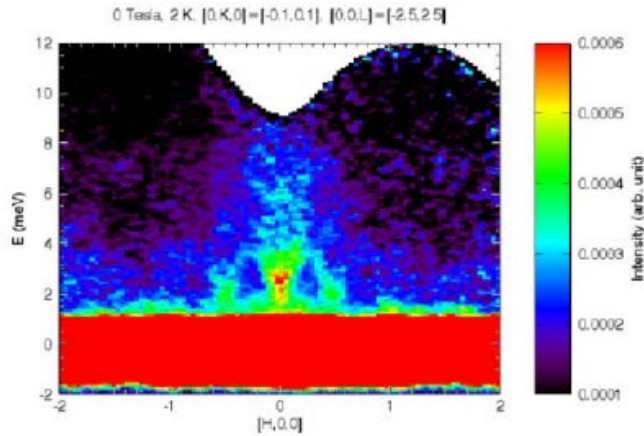
2K, 0T



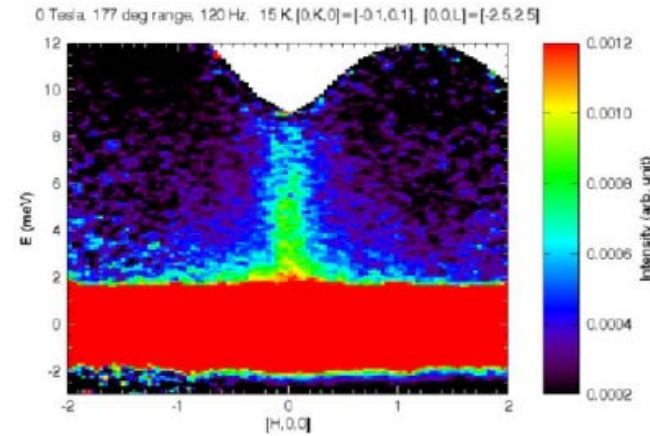
# How does field affect the magnetic excitations?

- Does killing order with an applied field lead to a QSL?

2K, 0T



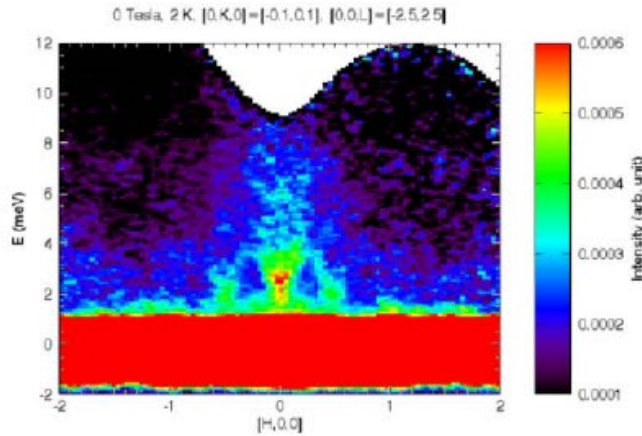
15K, 0T



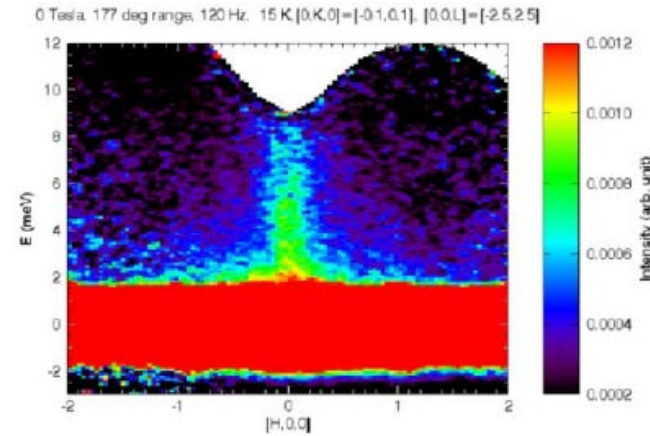
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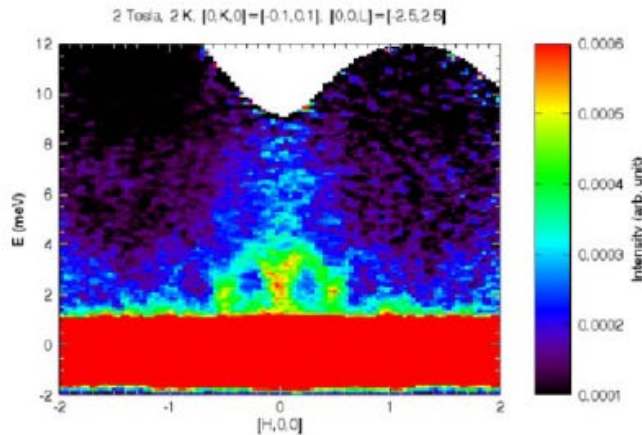
2K, 0T



15K, 0T



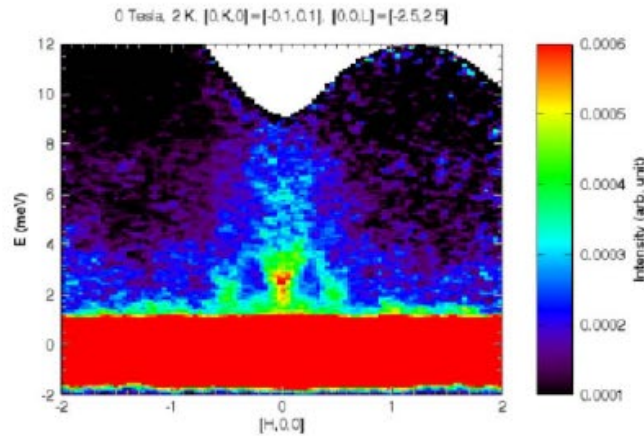
2K, 2T



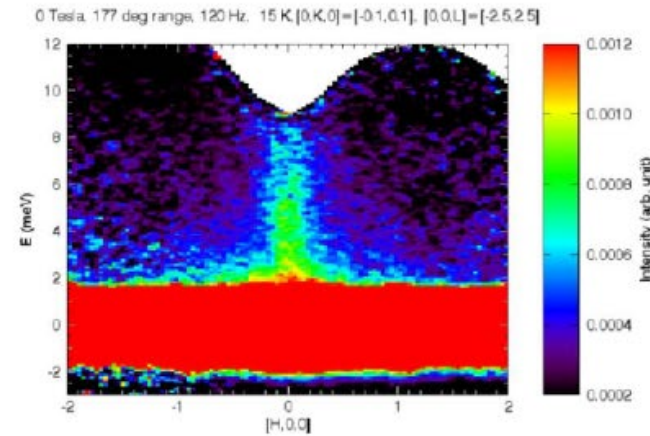


# How does field affect the magnetic excitations?

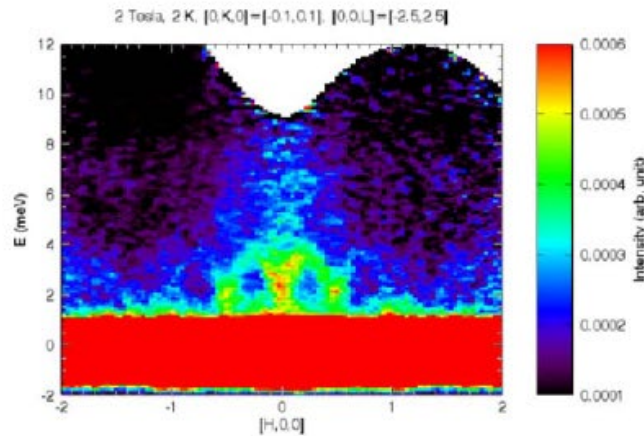
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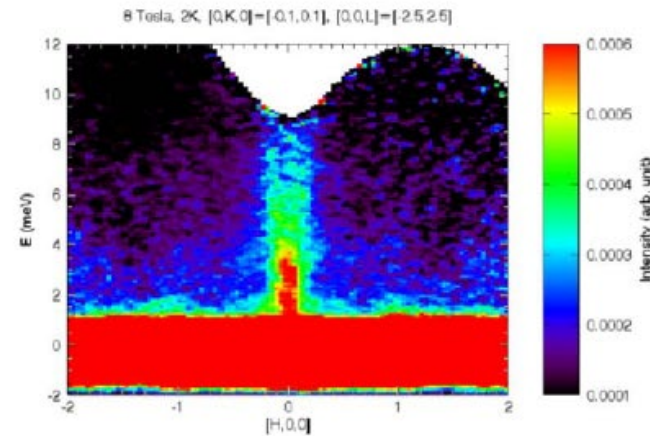
15K, 0T



2K, 2T

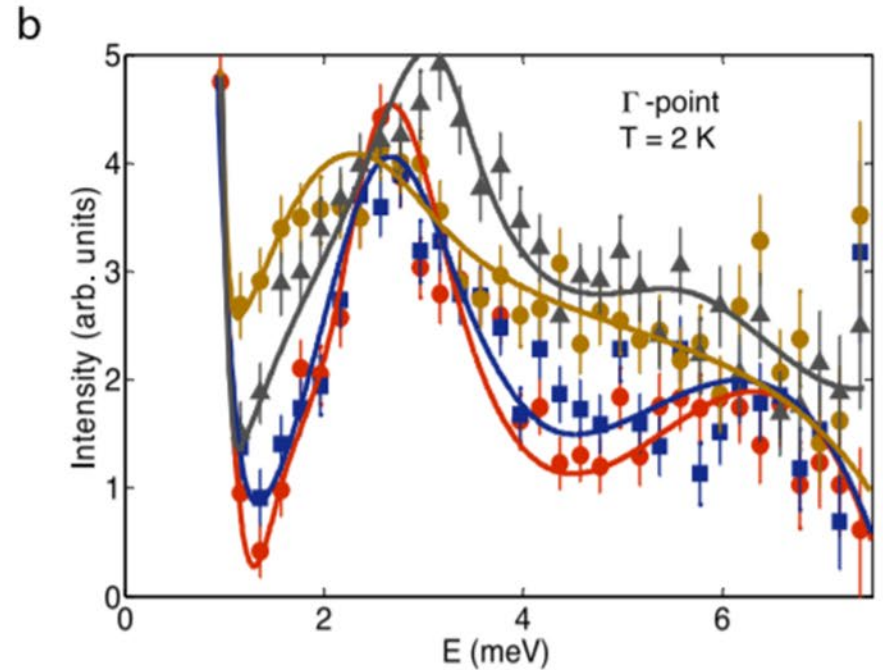
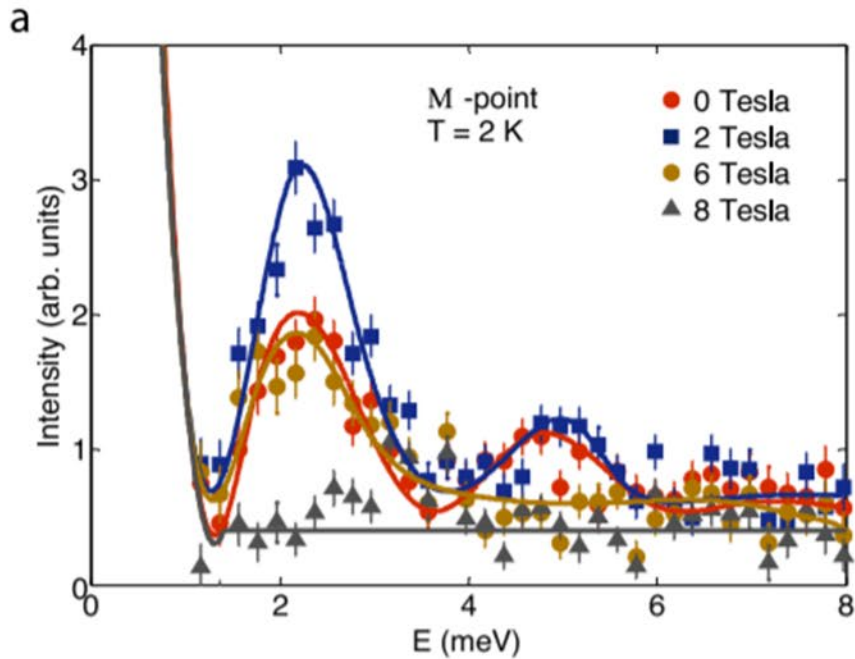


2K, 8T



Npj Quantum Materials 3, 8 (2018).

# Is the scattering gapped at the $\Gamma$ point?



Npj Quantum Materials **3**, 8 (2018).

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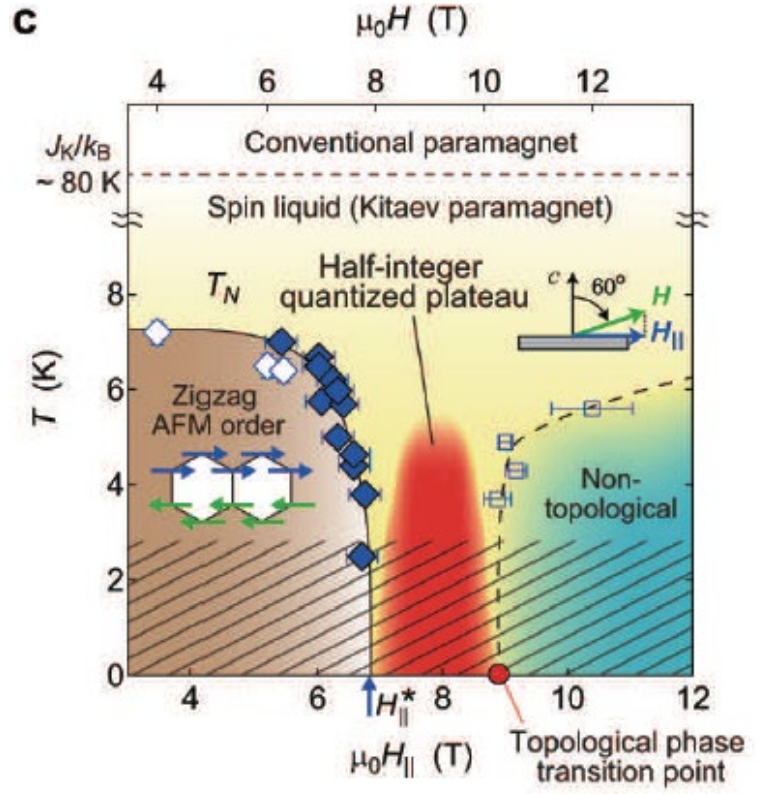
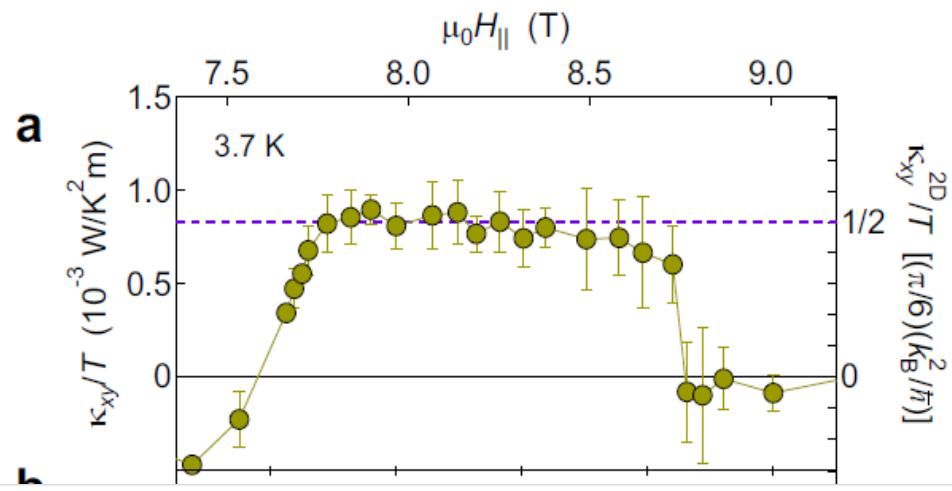
# Evidence of fractionalization from thermal Hall ?

## Majorana quantization and half-integer thermal quantum Hall effect in a Kitaev spin liquid

Y. Kasahara<sup>1</sup>, T. Ohnishi<sup>1</sup>, N. Kurita<sup>2</sup>, H. Tanaka<sup>2</sup>, J. Nasu<sup>2</sup>, Y. Motome<sup>3</sup>, T. Shibauchi<sup>4</sup>, and Y. Matsuda<sup>1</sup>

$\kappa_{xy}^{2D}$  reaches a quantum plateau as a function of applied magnetic field. That is,  $\kappa_{xy}^{2D}/T$  attains a quantization value of  $(\pi/12)(k_B^2/\hbar)$ , which is exactly half of  $\kappa_{xy}^{2D}/T$  in the integer QHE. This half-integer thermal Hall conductance observed in a bulk material is a direct signature of topologically protected chiral edge currents of charge neutral Majorana fermions, particles that are their own antiparticles, which possess half degrees of freedom of conventional fermions [13–16]. These signatures demonstrate the fractionalization of spins into itinerant Majorana fermions and  $Z_2$  fluxes predicted in a Kitaev QSL [1, 3]. Above

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# Field dependence of scattering at specific $\Gamma$ points

CHRISTIAN BALZ *et al.*

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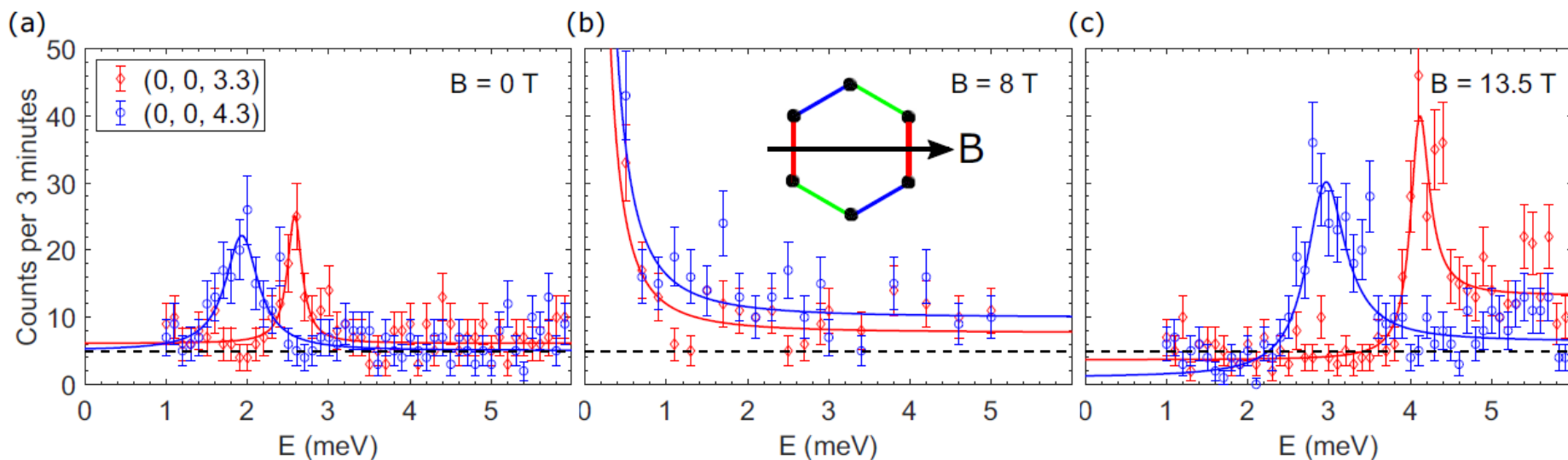
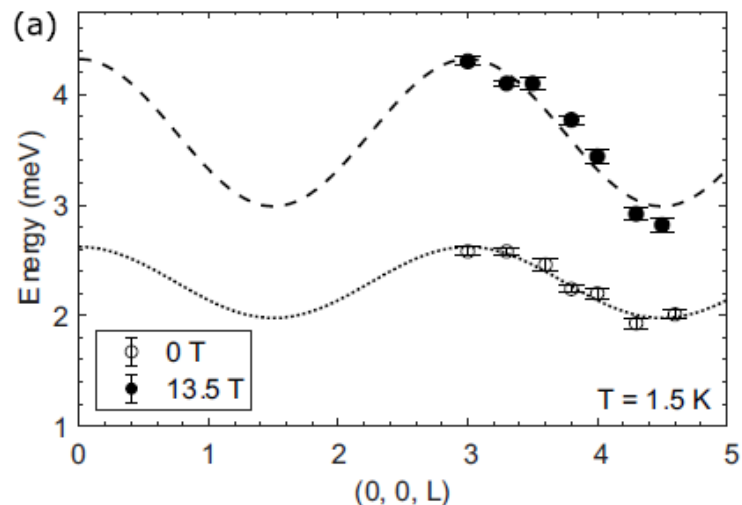
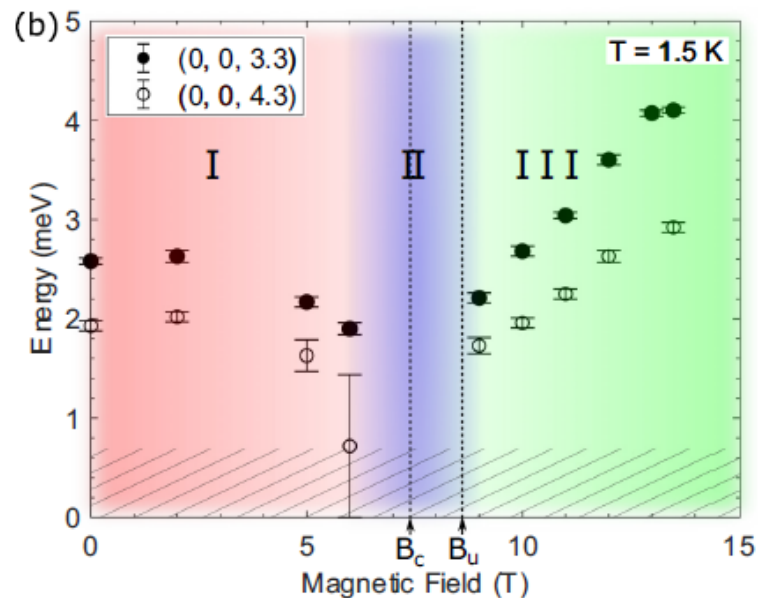


FIG. 1. Field dependence of the inelastic neutron scattering at the 2D  $\Gamma$  point for two values of the out-of-plane wave-vector transfer. Data obtained at 1.5 K on a 2 g single crystal of  $\alpha$ - $\text{RuCl}_3$  using the FLEXX triple-axis spectrometer. (a) Zero-field data. A field of (b) 8 T and (c) 13.5 T was applied in the honeycomb plane perpendicular to a Ru-Ru bond [see inset of (b)]. The solid lines are fits and the dashed lines show the model free background for (0,0,3.3) as described in the text. Error bars represent one standard deviation assuming Poisson statistics.

# L dispersion and band width



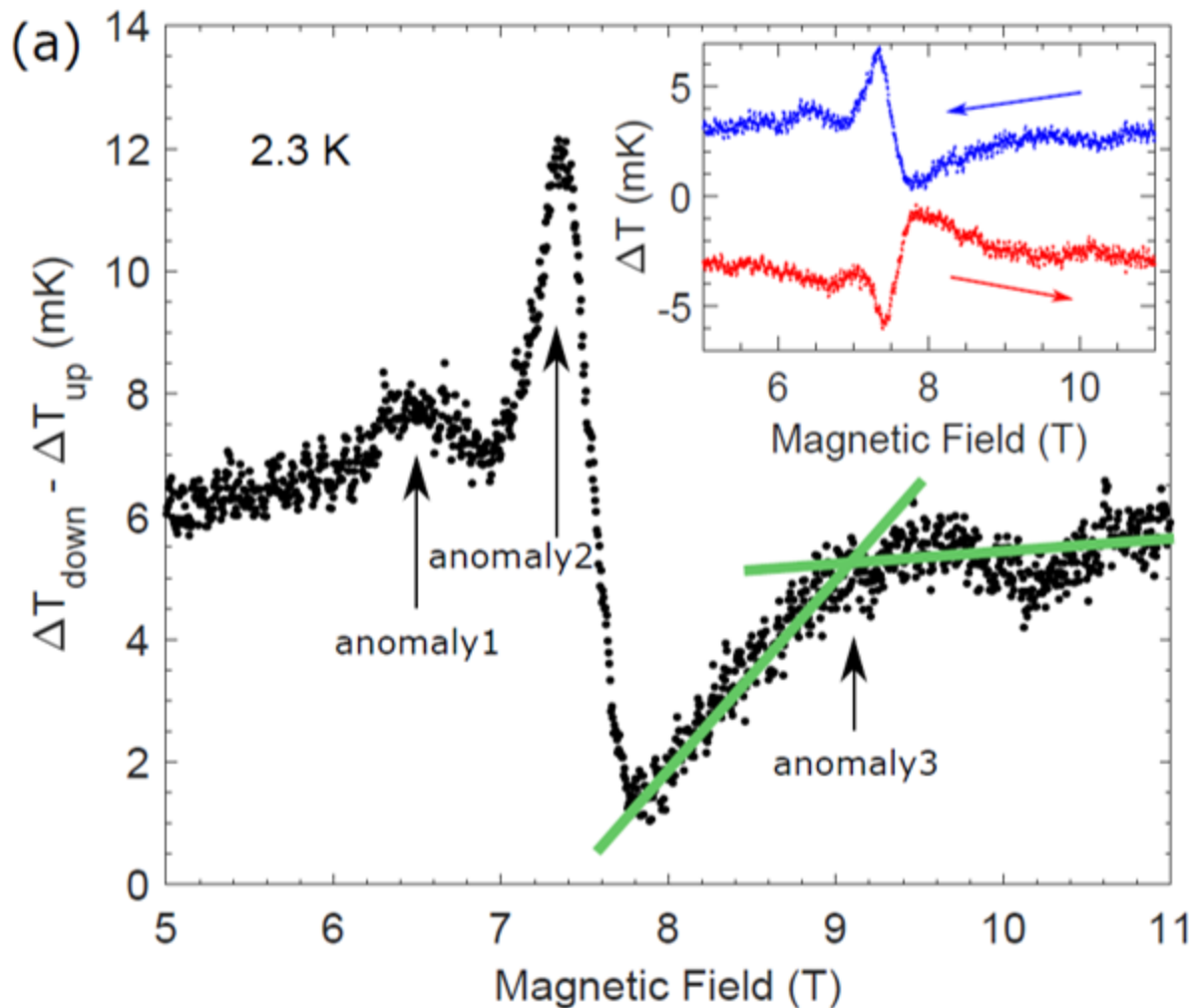
- The dispersion in L is a measure of the magnetic interactions perpendicular to the plane



- The reduction of the bandwidth near the region where magnons are not detected is a signature of enhanced two-dimensionality

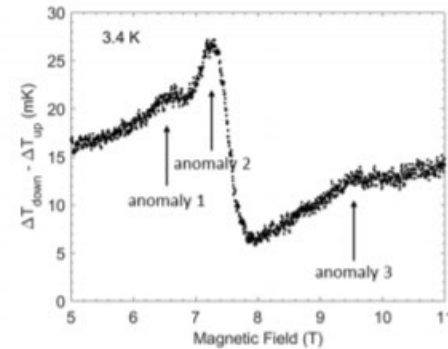
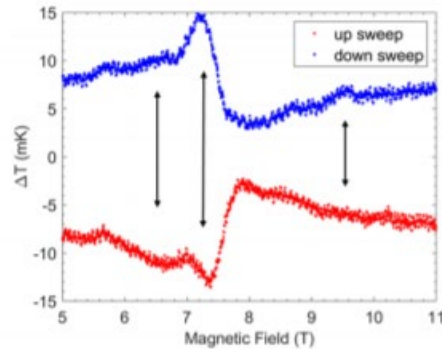
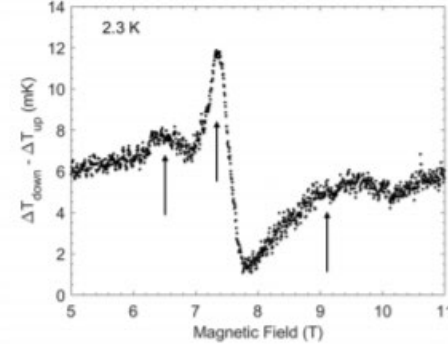
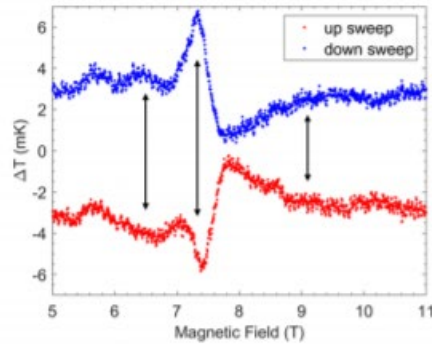
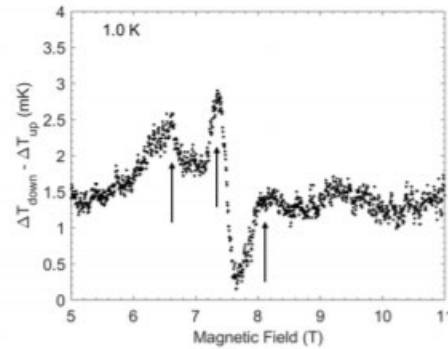
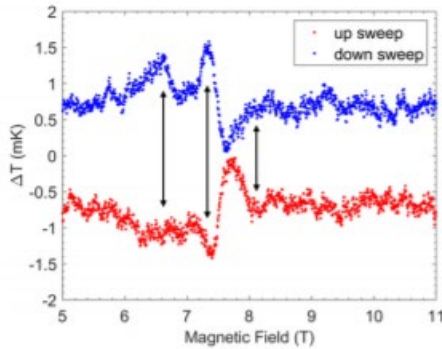
# Magnetocaloric effect

Y. Takano group



$$\Delta T \propto -T \left( \frac{\partial M}{\partial T} \right)_H \Delta H$$

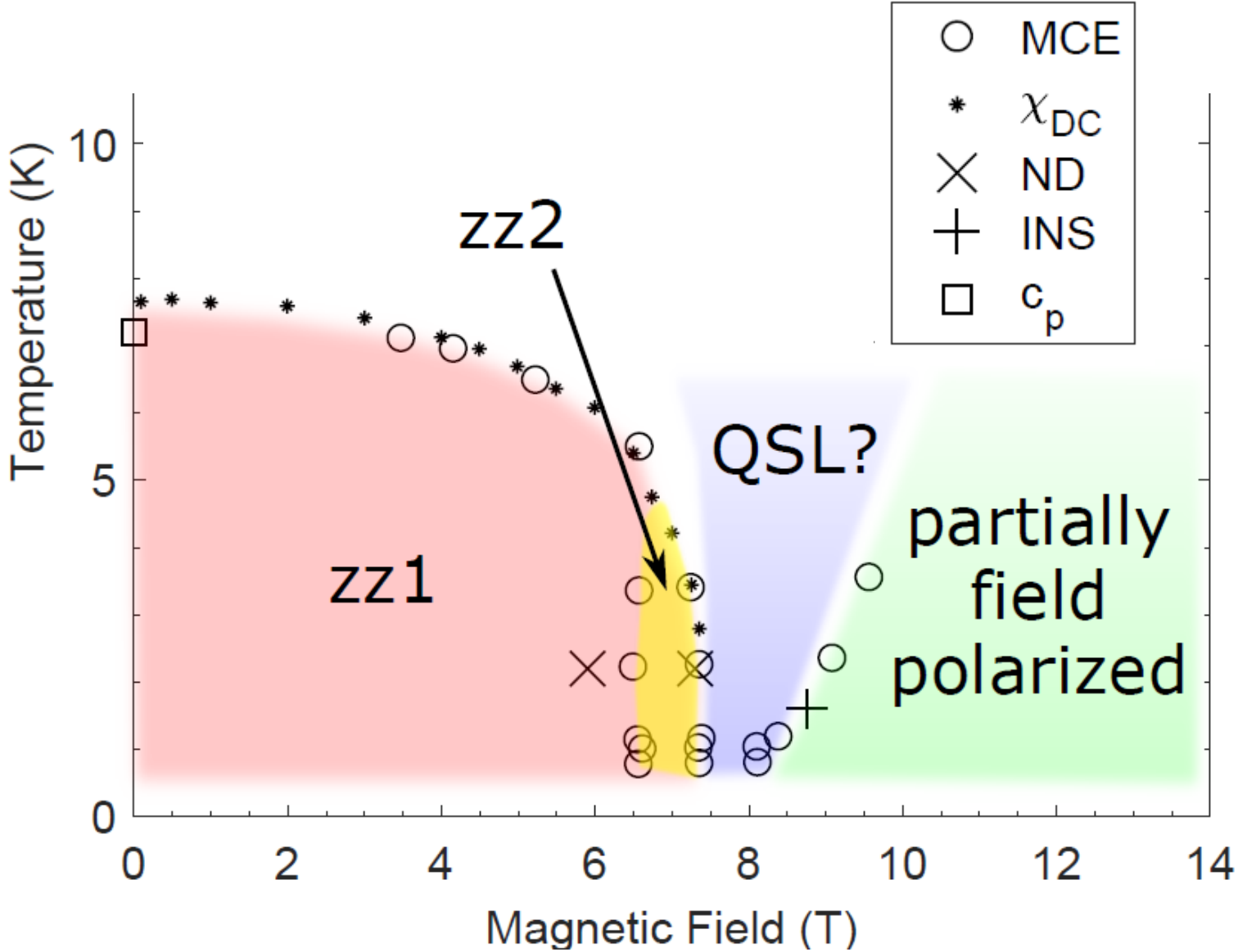
# Magnetocaloric effect at different T



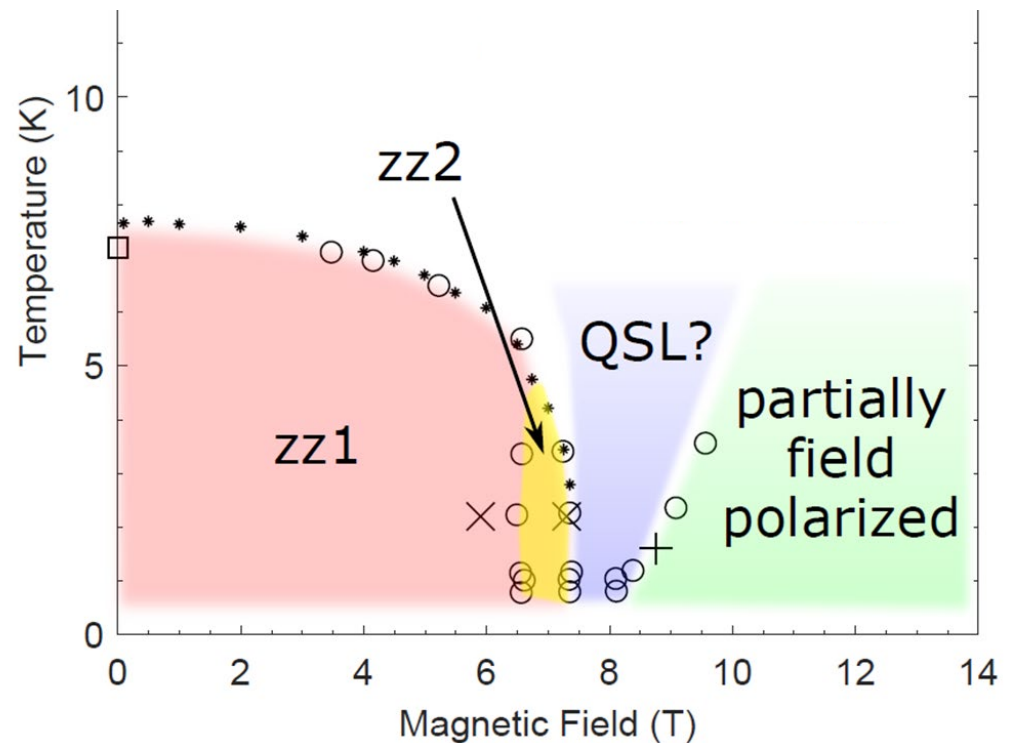
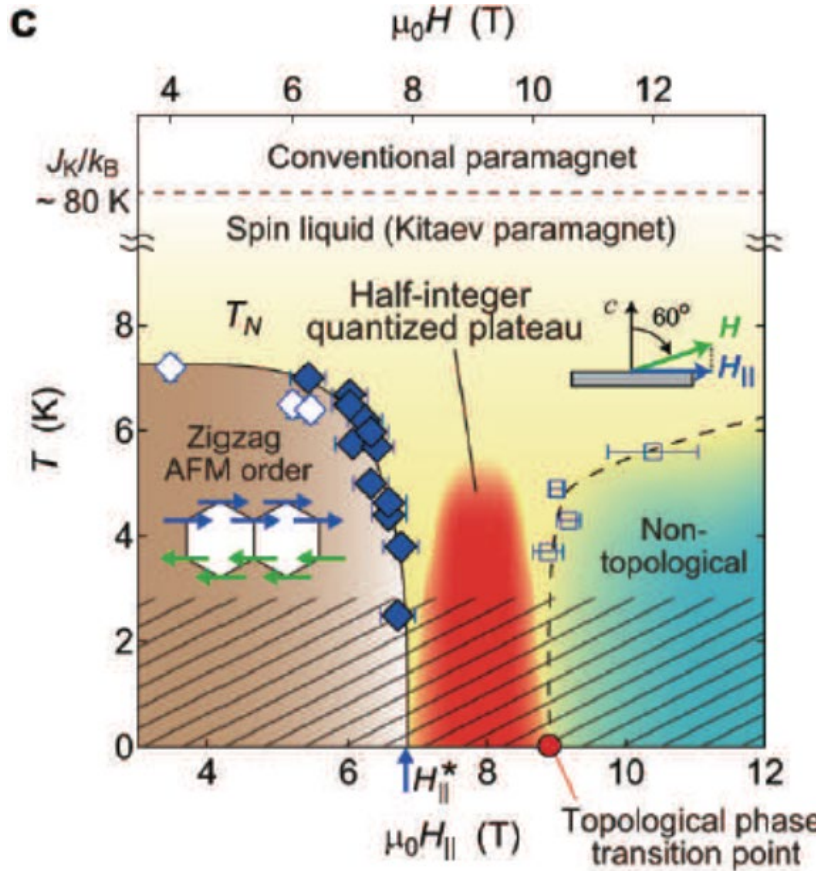
- Measurements at different temperatures allow one to construct a phase diagram



# More complete phase diagram



# Comparison with Kasahara *et al.* phase diagram



# Some conclusions

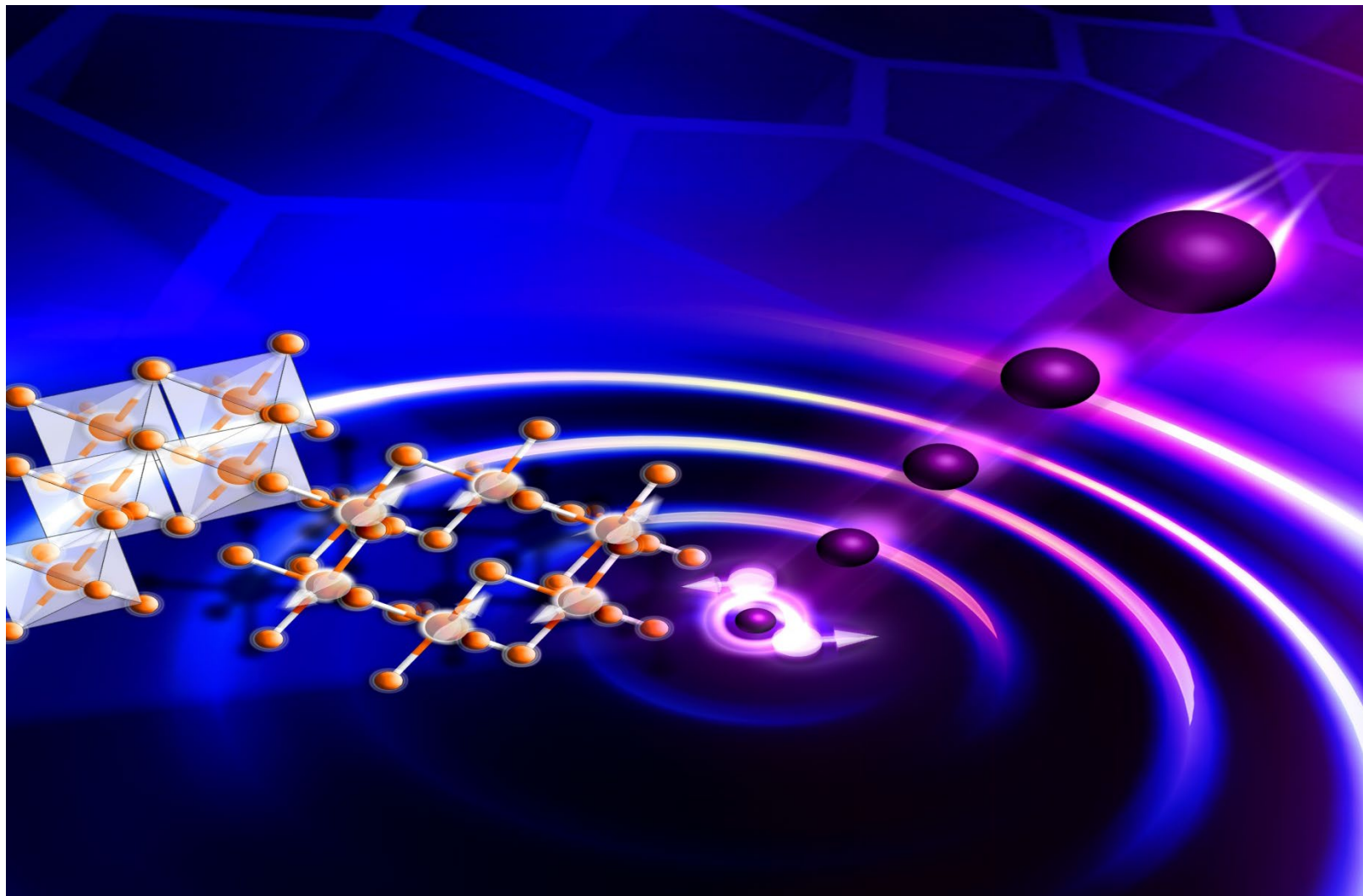
- Inelastic neutron scattering in  $\alpha$ - $\text{RuCl}_3$  is consistent with fractional excitations
- An external magnetic field applied in-plane leads to a magnetically disordered state, with a higher field transition to a state that seems to be partially polarized and supports magnons
- The intermediate field disordered state is consistent with a QSL

# Some ORNL references on $\alpha$ -RuCl<sub>3</sub>

## Neutron scattering experiments:

- A. Banerjee *et al.* Nature Materials **15**, 733(2016).
- H. Cao, A. Banerjee *et al.* PRB **93**, 134423 (2016).
- A. Banerjee *et al.* SCIENCE **356**, 1055 (2017).
- P. Lampen–Kelley *et al.* PRL **119**, 237203, (2017).
- A. Banerjee *et al.*, Npj Quantum Materials **3**, 8 (2018).
- C. Balz *et al.*, PRB **100**, 060405(R) (2019).

# Thank you for your attention



# Questions?

