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# Exciton-polaritons in 2D Lieb lattice with spin-orbit coupling

D.N. Krizhanovskii

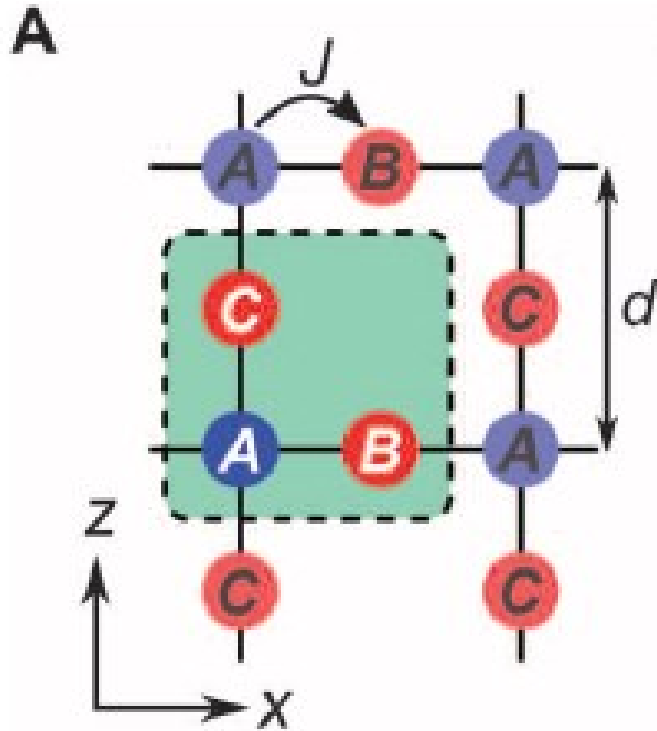
Low-dimensional structures & devices (LDSD)  
group

The University of Sheffield

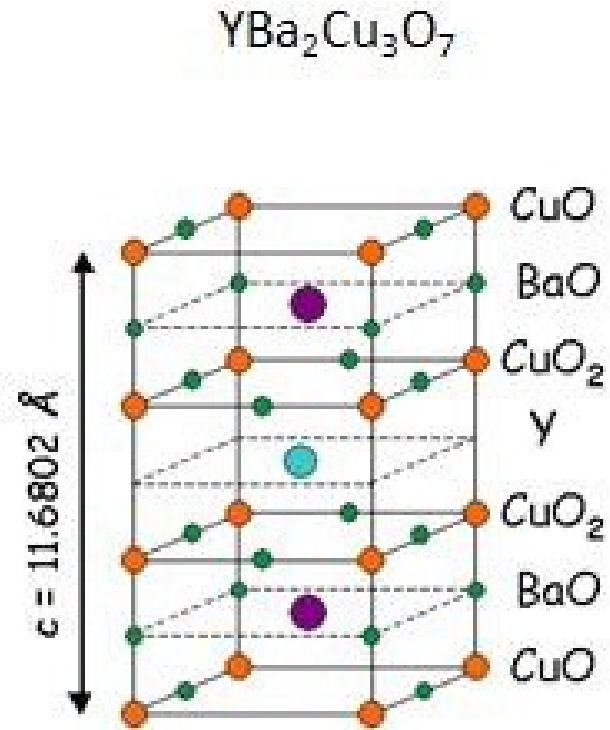
# Outline

- Introduction to Lieb lattices. Importance of flat bands
- Methods of polariton confinement. Photonic spin-orbit coupling
- Polariton 2D Lieb lattice
- Real space patterns with polarisation textures of S and P type flat band condensates
- Condensate fragmentation and effects of interactions
- Conclusions

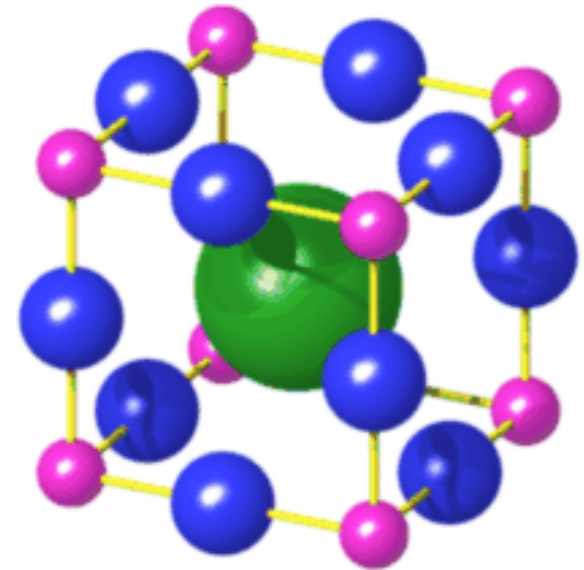
# 2D Lieb lattice



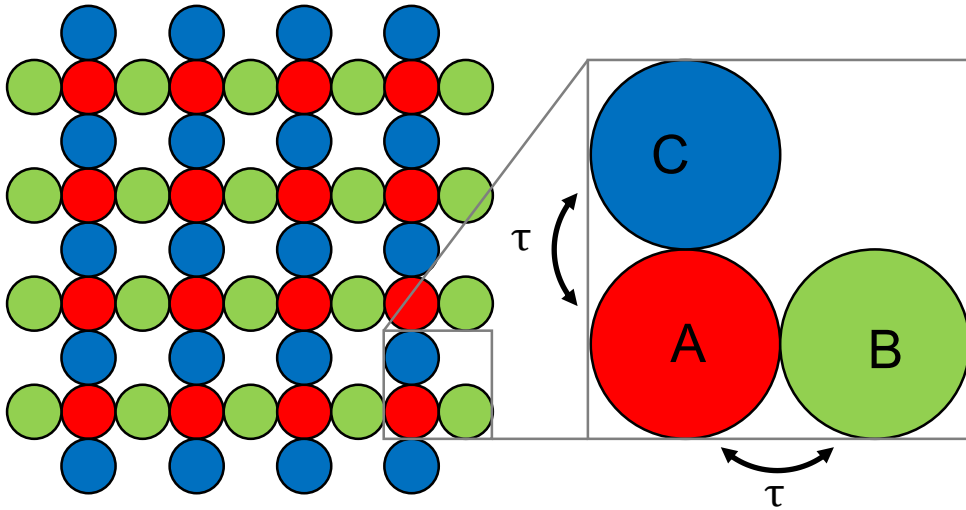
Decorated square lattice (A) with another sublattice centered on each side of the square



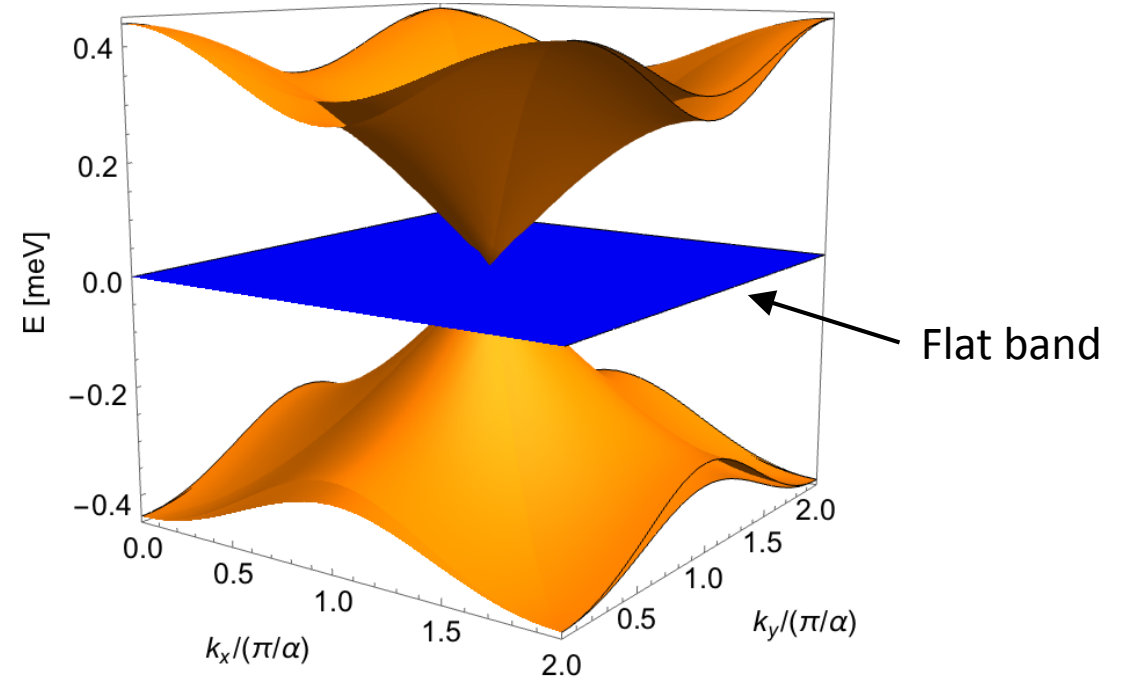
Lieb lattice observed in layered perovskites materials  
 $\text{CuO}_2$  weakly bound layer in high T superconductor  $\text{YBa}_2\text{Cu}_3\text{O}_7$



# Energy band structure and flat bands



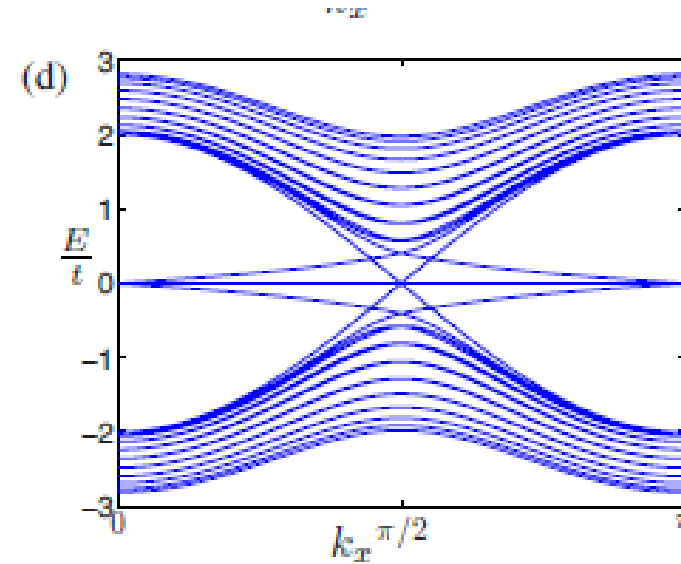
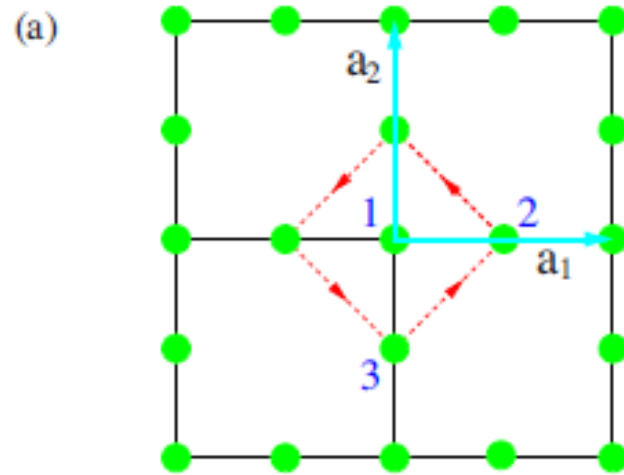
- Ferromagnetic ordering
- Quantum Hall phases
- Linear and nonlinear self-trapped wave packets (compactons)



Flat band arises from destructive interference between quasiparticles tunnelling from C to A and from B to A.

Linear dispersion crossing flat band at the edge of BZ

# Topological and correlated phases in Lieb Lattice

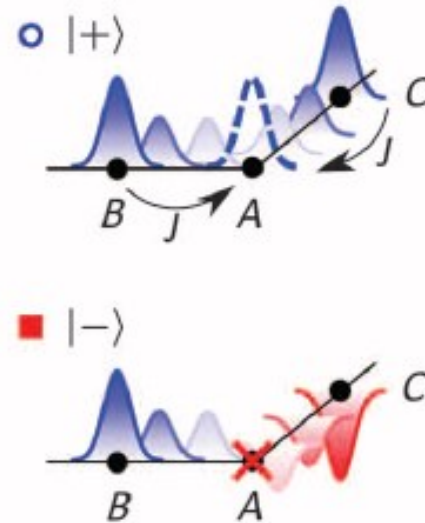
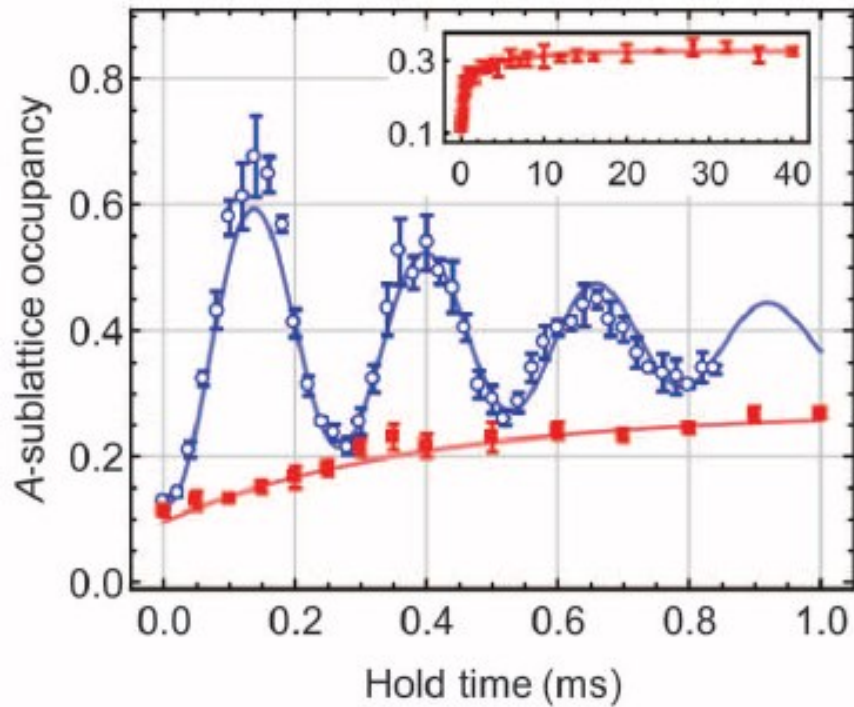


Spin-orbit induced next nearest neighbour coupling opens gap

Formation of topologically protected edge states

*PRB 82, 085310 (2010)*

# BEC of cold atoms in Lieb lattice

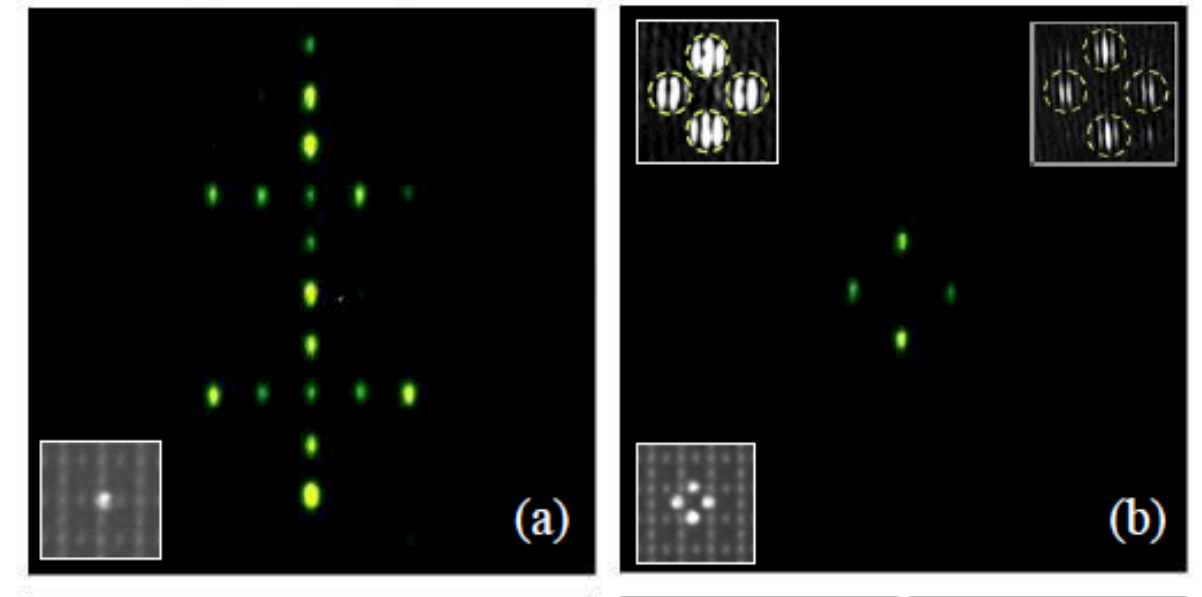
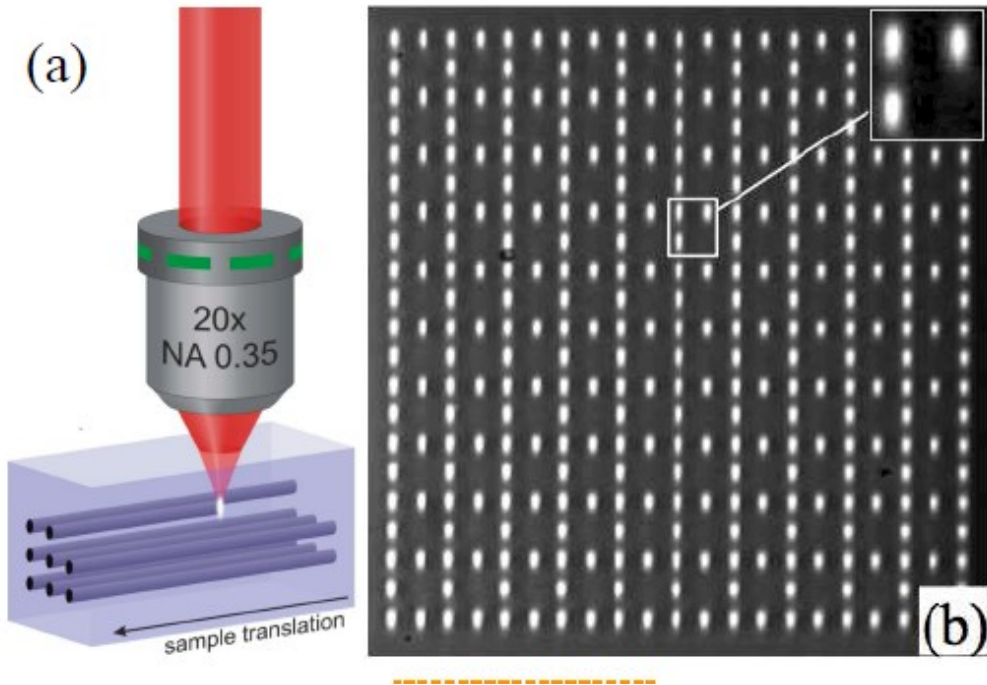


Atomic BEC in optically induced Lieb lattice

Localisation in a flat band

*Science Advances 1, 10, (2015)*

# Compactons in Lieb lattice of coupled waveguides

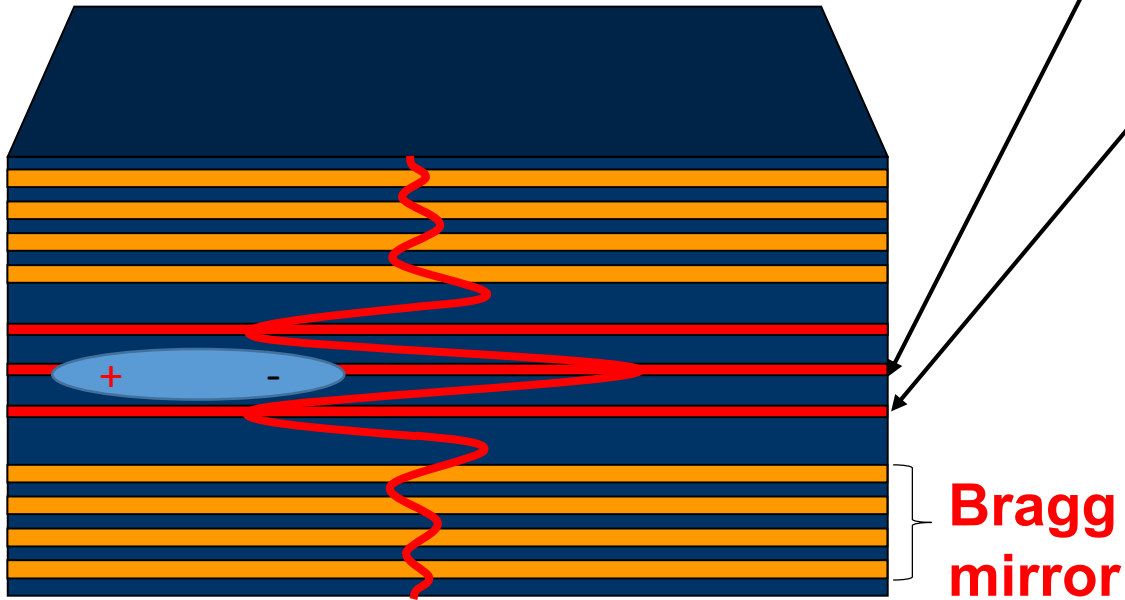


PRL 114, 245503 (2015)

# STRONG EXCITON-PHOTON COUPLING IN SEMICONDUCTOR MICROCAVITIES

quantum well (III-V, II-VI or 2D materials of  $\text{MoSe}_2$ ,  $\text{WSe}_2$ .)

$$\Psi = X|\text{exciton} \rangle + C|\text{photon} \rangle$$

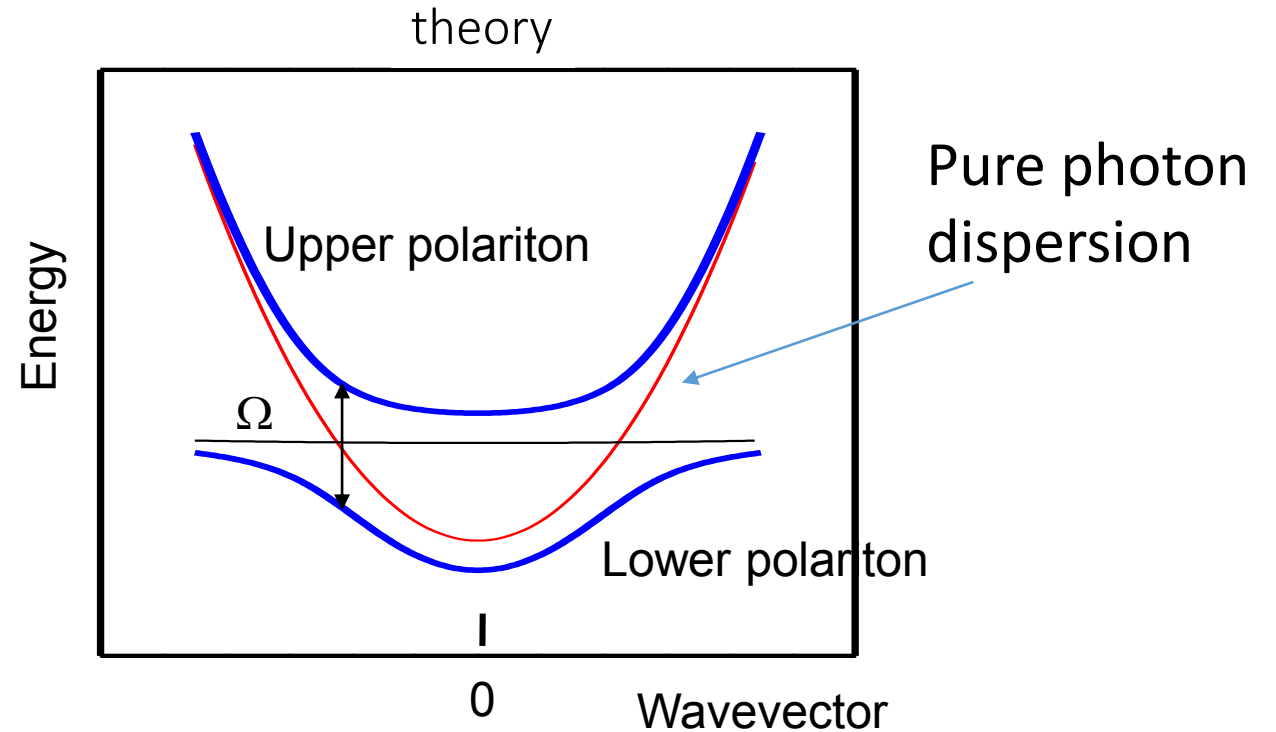
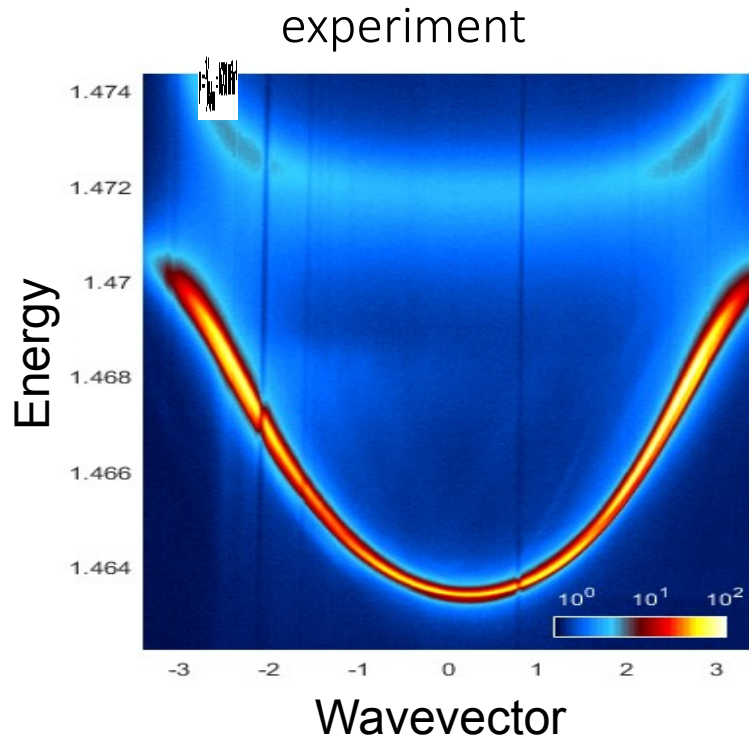


Photon mode is in resonance with quantum well exciton

Strong exciton-photon coupling leads to mixed exciton-photon states, so-called 2D polaritons



# MICROCAVITY POLARITON DISPERSION

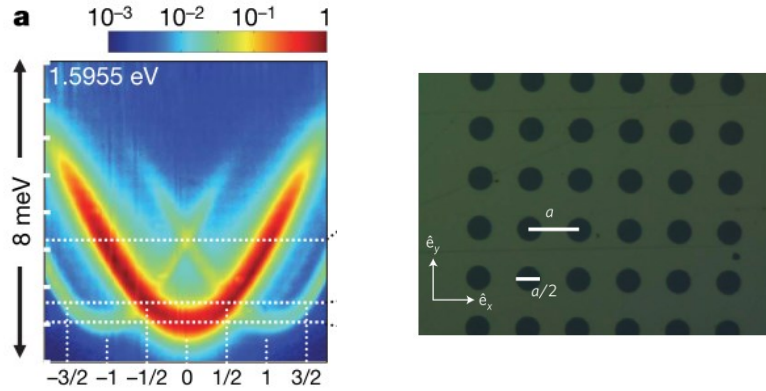


- Strong polariton-polariton interactions due to exciton
- Fast response on ps timescale=> suitable for optical signal processing
- Low mass (low density of state).  $10^{-8-9}$  times smaller than an atom mass

**Polariton Bose-Einstein condensation at high T can be observed**

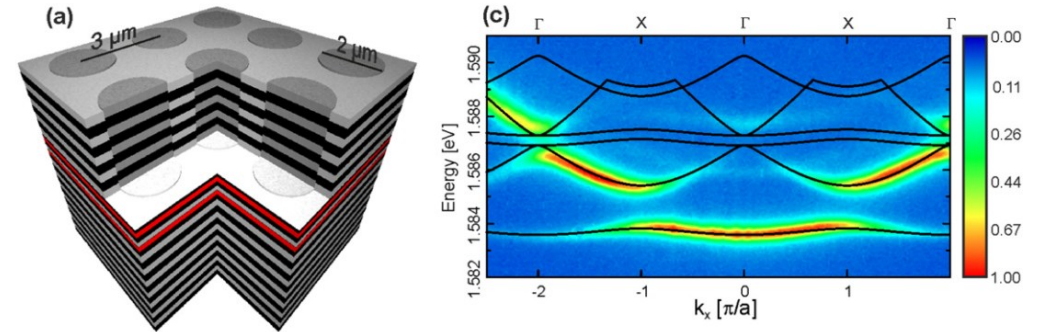
# Methods of exciton-polariton confinement

Metal deposition (100's  $\mu\text{eV}$ )



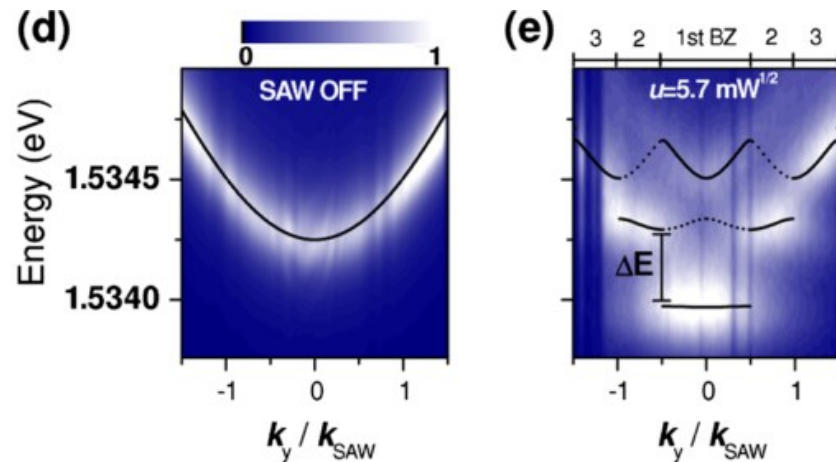
*Nature* **450**, 529-532 (2007); *Nature Phys.* **7**, 681-686 (2011)

Mesa traps (several meV)



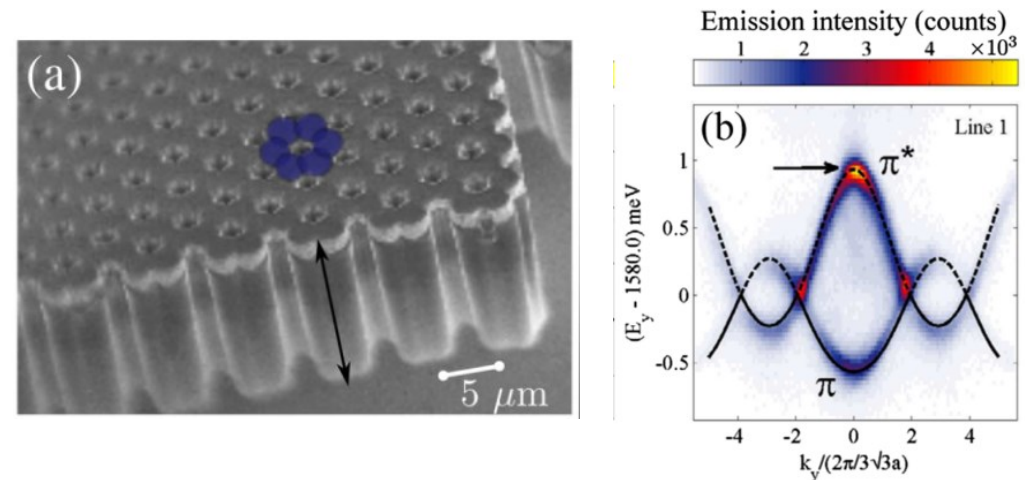
*New J. Phys.* **17**, 023001 (2015)

Surface acoustic waves (100's  $\mu\text{eV}$ )



*Phys. Rev. Lett.* **105**, 116402 (2010)

Etched micropillars (10's meV)



*Phys. Rev. Lett.* **112**, 116402 (2014)

# Photonic spin-orbit coupling

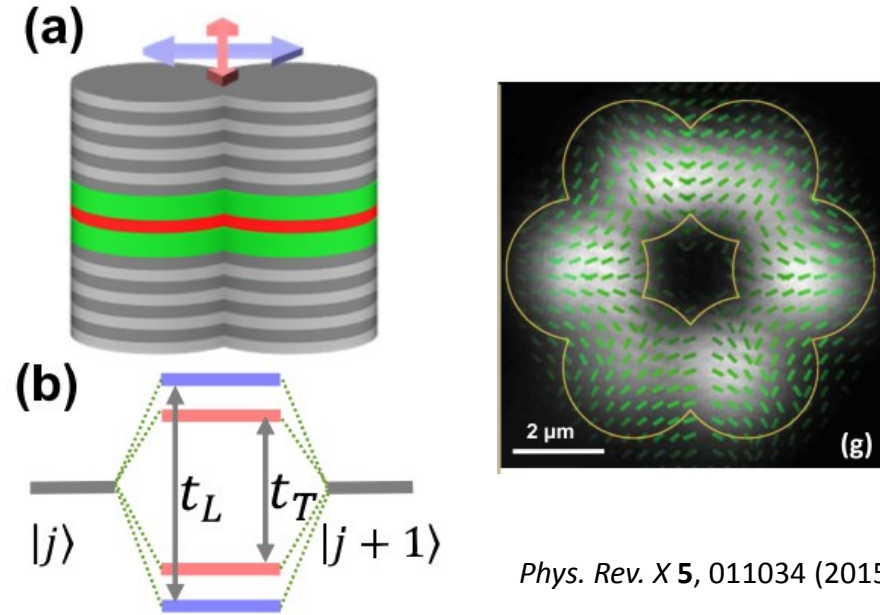
- Strong TE-TM splitting of photonic mode
- Introduces effective magnetic field acting on polariton pseudospin (polarisation)

$$\begin{pmatrix} H(\mathbf{k}) & \Omega_{LT}(\mathbf{k})e^{-2i\theta} \\ \Omega_{LT}(\mathbf{k})e^{+2i\theta} & H(\mathbf{k}) \end{pmatrix} = H(\mathbf{k})I + \boldsymbol{\Omega}_{LT} \cdot \boldsymbol{\sigma}$$

*C. R. Physique* **17**, 920-933 (2016)

*Phys. Rev. Lett.* **115**, 116402 (2015)

## Polarization-dependent hopping in micropillars



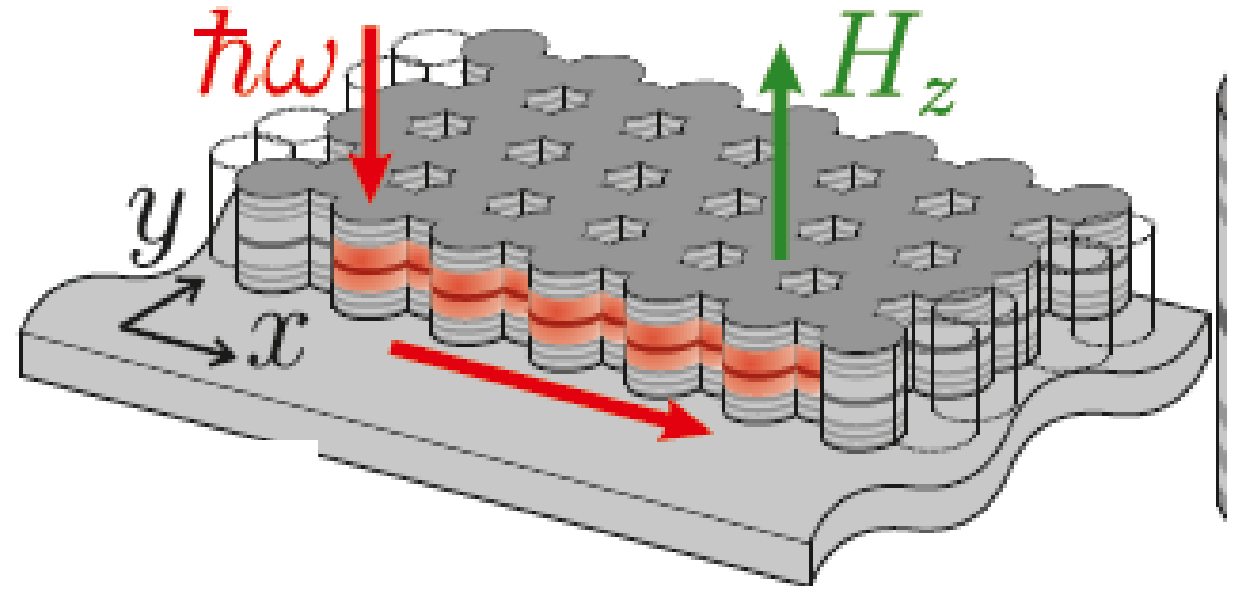
*Phys. Rev. X* **5**, 011034 (2015)

- One way to realize SSH Hamiltonian
- Large SOC + Zeeman splitting  $\rightarrow$  opening of a topologically non-trivial gap in honeycomb lattices

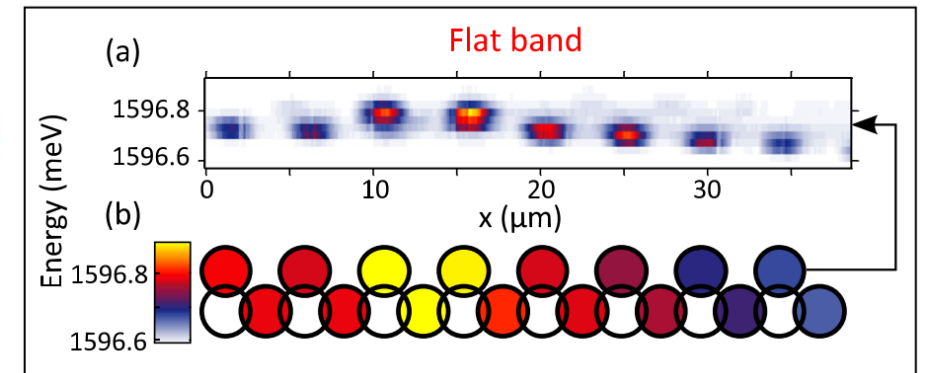
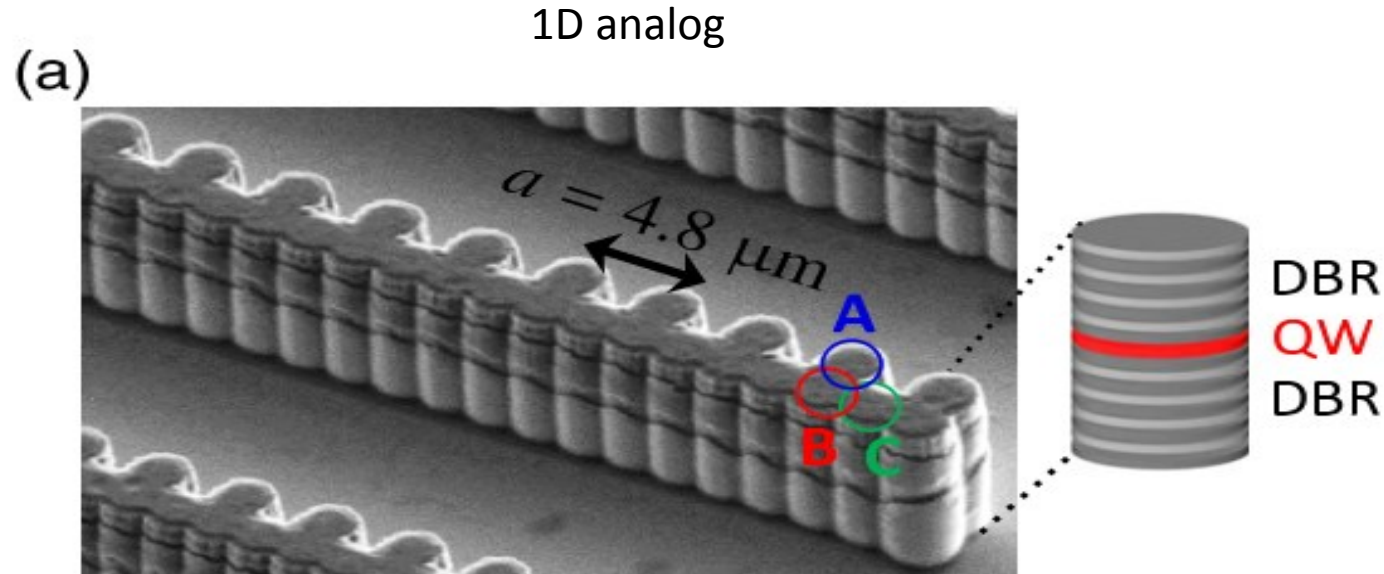
# PSEUDOMAGNETIC FIELDS IN POLARITON SYSTEM

Large spin-orbit interaction  
for photons + real magnetic  
field acting on excitons

*Phys. Rev. Lett. 114, 116401 (2015)*



# 1D Lieb lattice

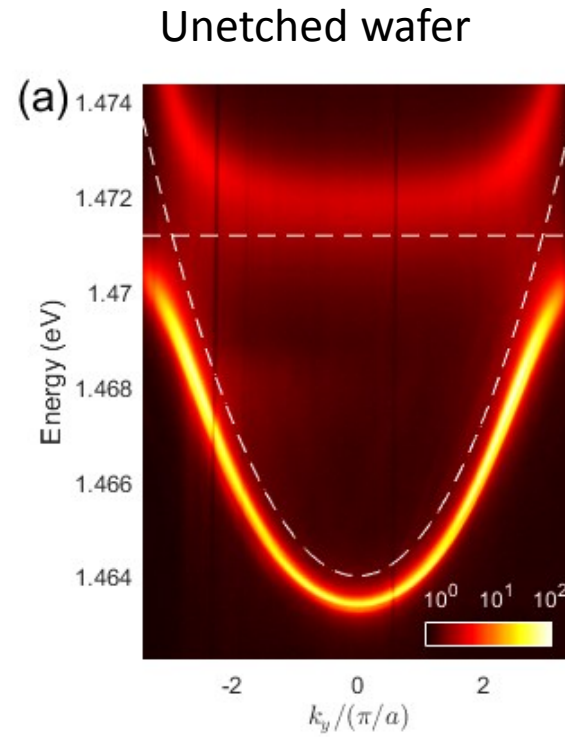


*Phys. Rev. Lett.* **116**, 066402 (2016)

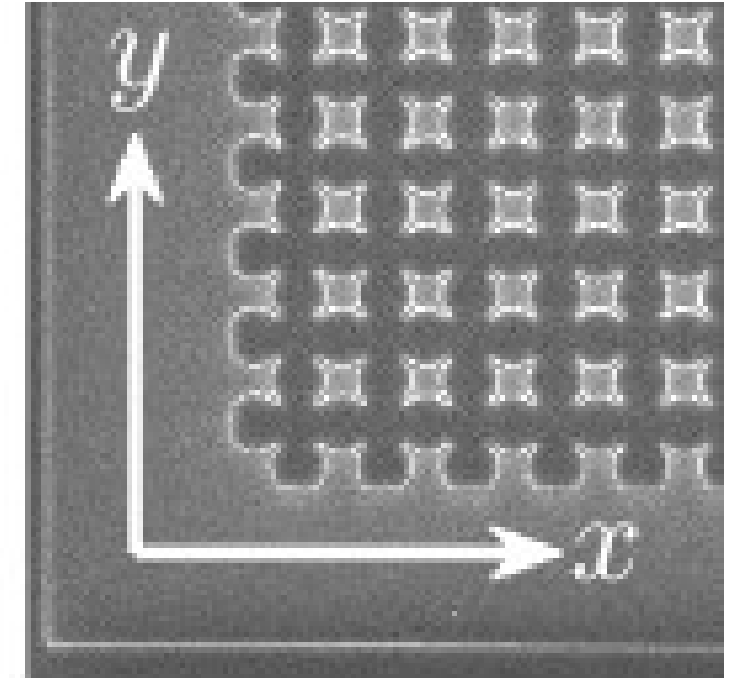
Condensation into S type flat band.

Orbital flat bands and effects of spin orbit coupling unexplored

# Our system



EBL + plasma  
dry etching



- $\lambda/2$  GaAs microcavity with 3x  $\text{In}_{0.4}\text{Ga}_{0.96}\text{As}$  QWs
- Rabi splitting of 4.7 meV
- Linewidth  $\sim 0.1$  meV
- Photon-exciton detuning of -7.2 meV

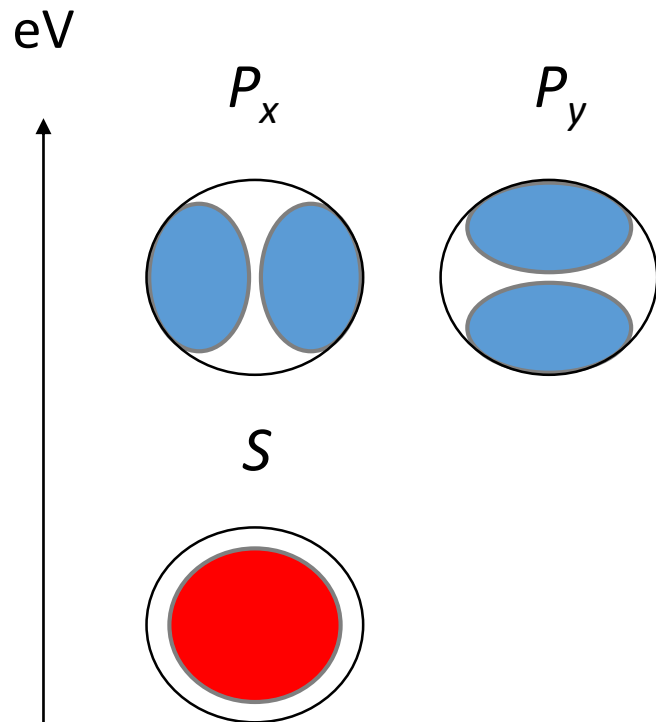
- 14x14 unit cells ( $\sim 100 \mu\text{m}^2$ )
- 3  $\mu\text{m}$  pillar diameter and 2.9  $\mu\text{m}$  separation
- 5.8  $\mu\text{m}$  lattice constant



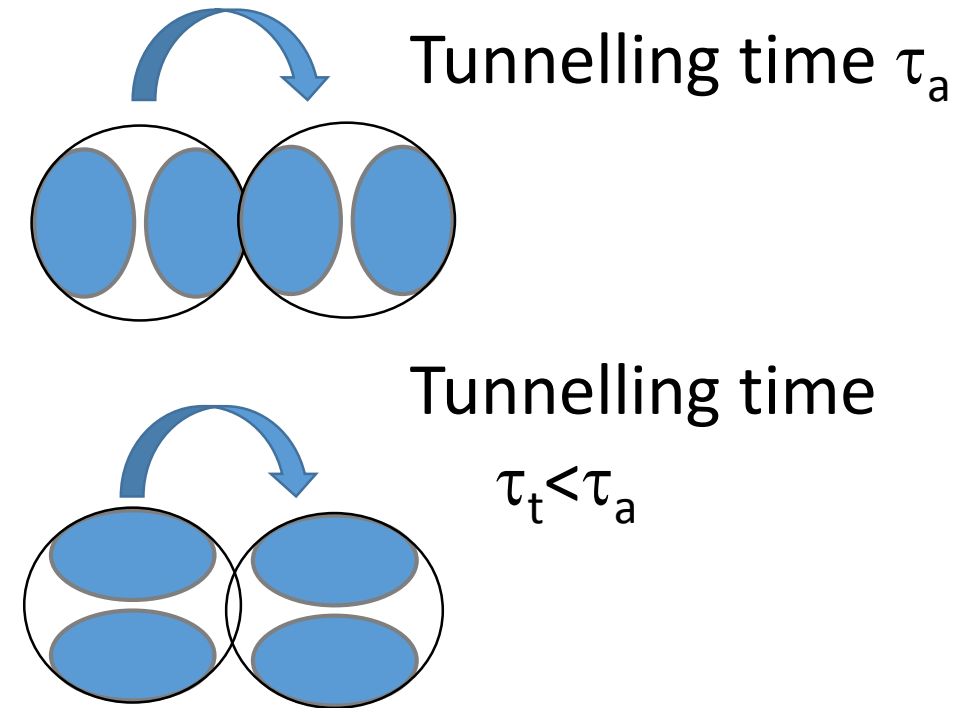
# S and P type orbitals in micropillars

(for now neglect polarisation degree of freedom)

Orbitals in single pillar

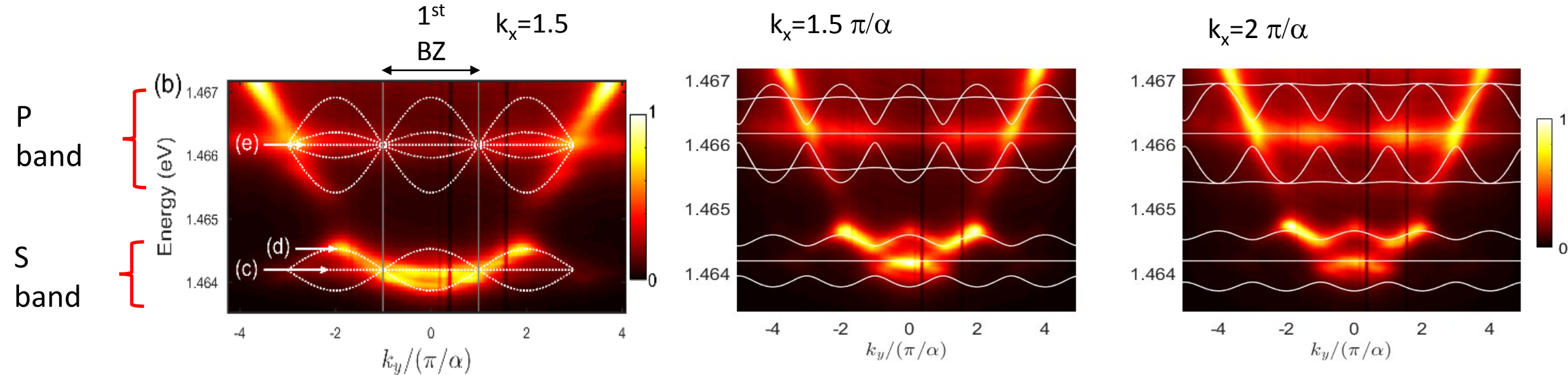


Tunneling of P orbitals between coupled pillars



# Energy-momentum relation

Experimental  $E$ - $k$  relations with tight-binding curves



Emission from Flat S and P type band is pronounced  
 Emission from some dispersive bands is suppressed probably due to far-field destructive interference of different modes

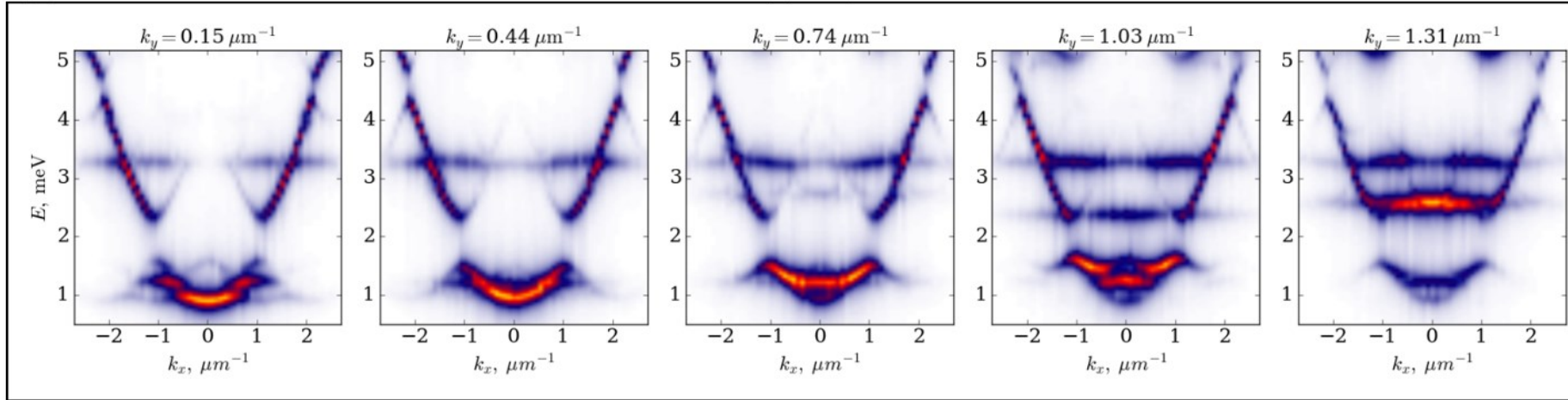
Tight-binding model:

- S band:  $\tau = 0.165$  meV
- P band:  $\tau^a = 0.375$  meV;  $\tau^t = 0.1$  meV



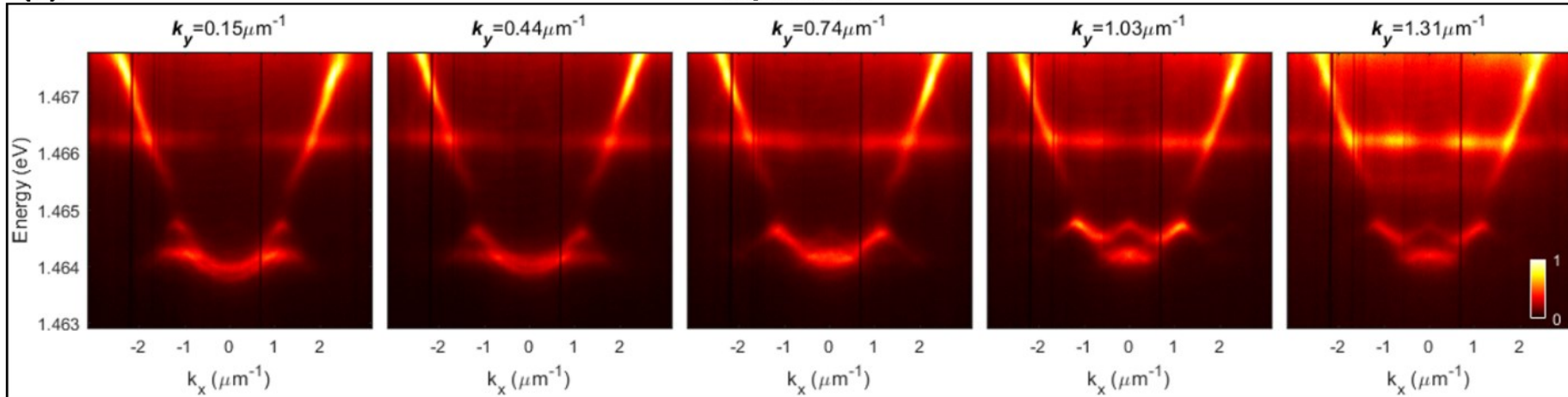
# Schrödinger equation in 2D Lieb potential

(a) Schrödinger equation

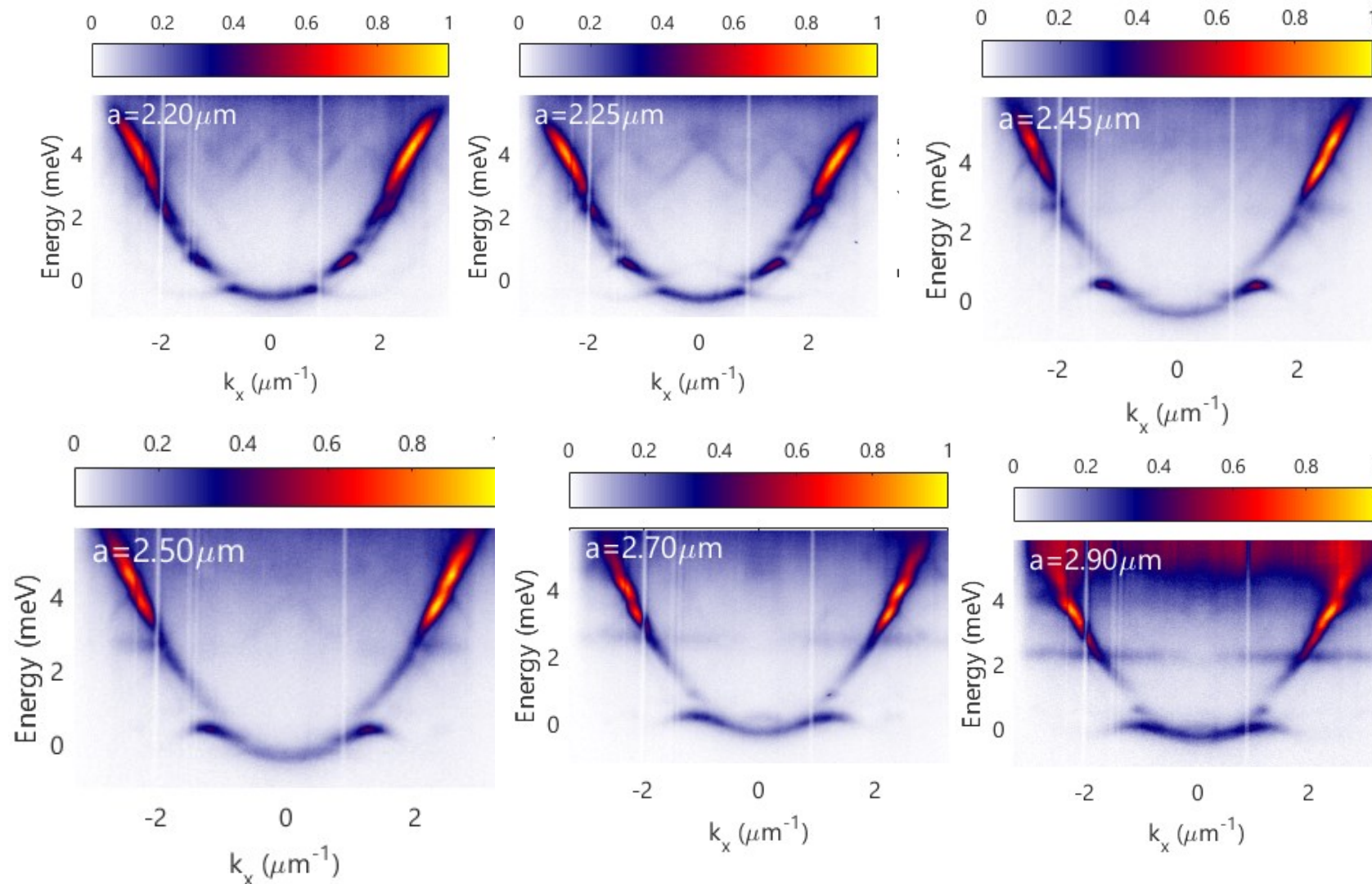


- 10 meV confinement potential
- $m^* = 5 \times 10^{-5} m_0$
- 0.1 meV lifetime

(b) Experiment



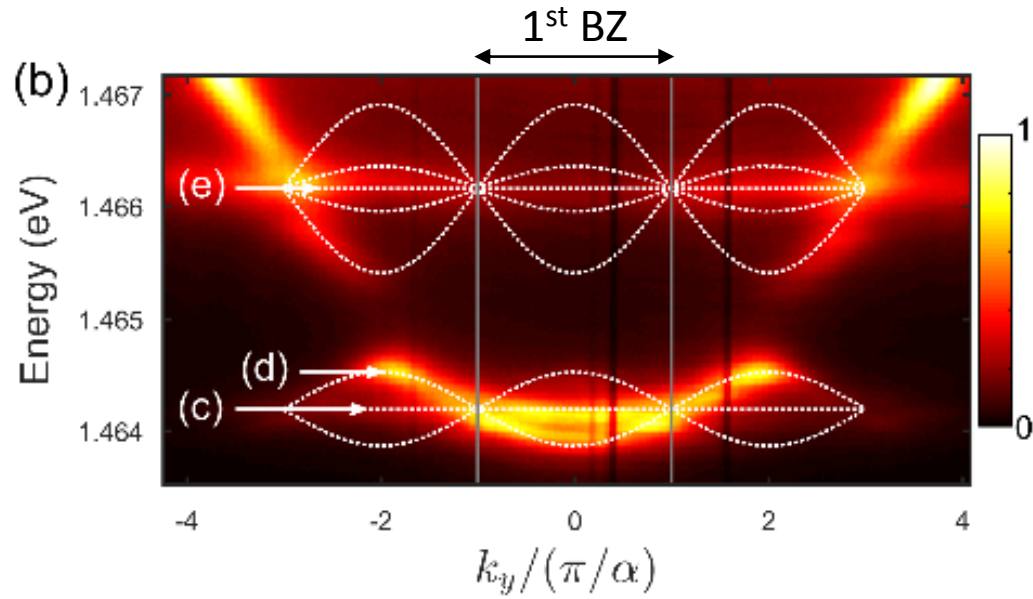
# Band structure for different lattice constants



At smaller lattice constants energy gaps become smaller

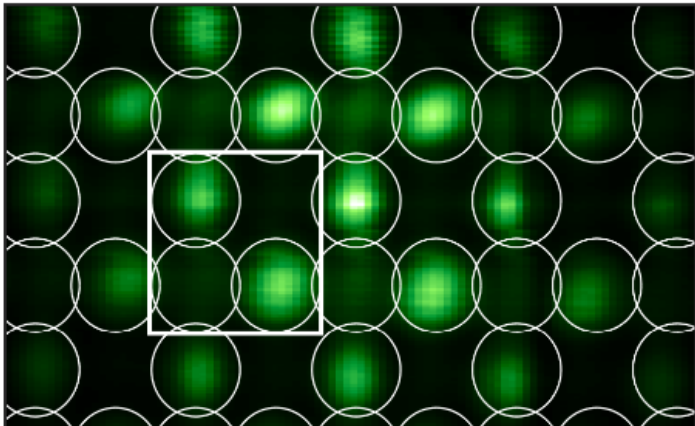
Flat bands disappear

# Real space emission

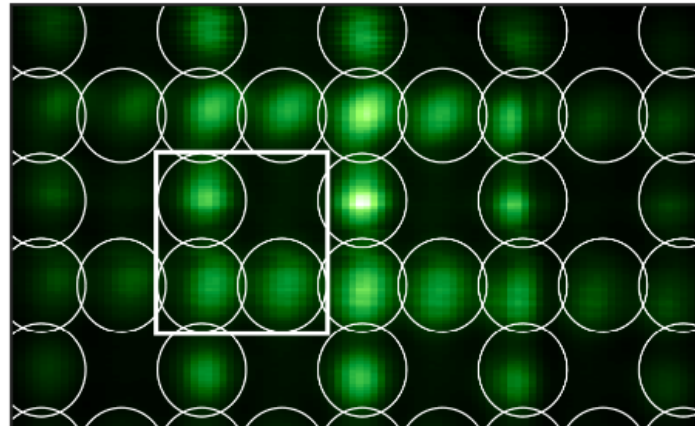


- Flat bands show suppressed emission from *B* sublattices due to destructive wave interference
- AB (dispersive) band eigenmodes are delocalized

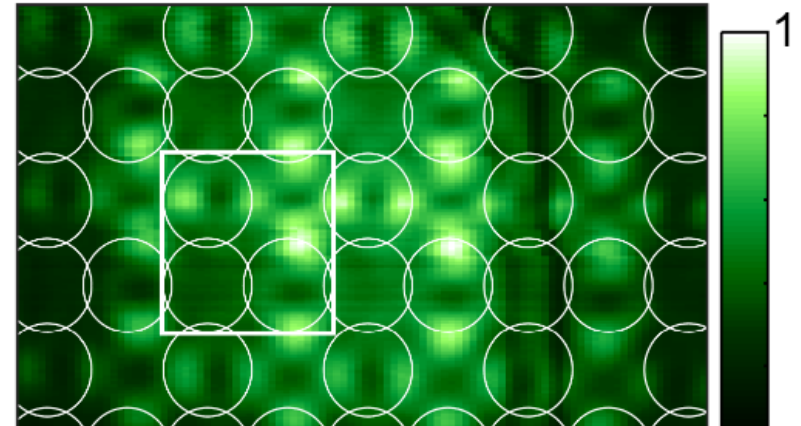
(c) S flat band



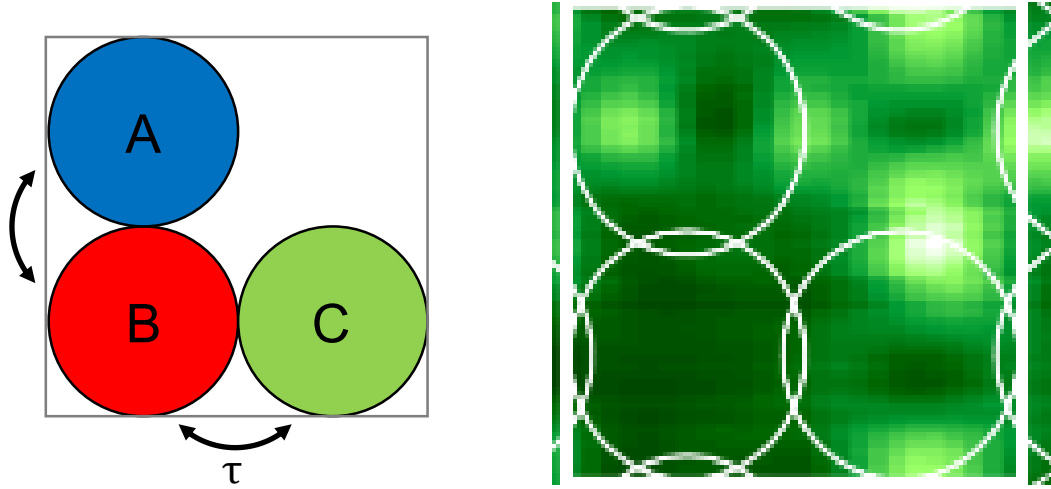
(d) AB band



(e) P flat band



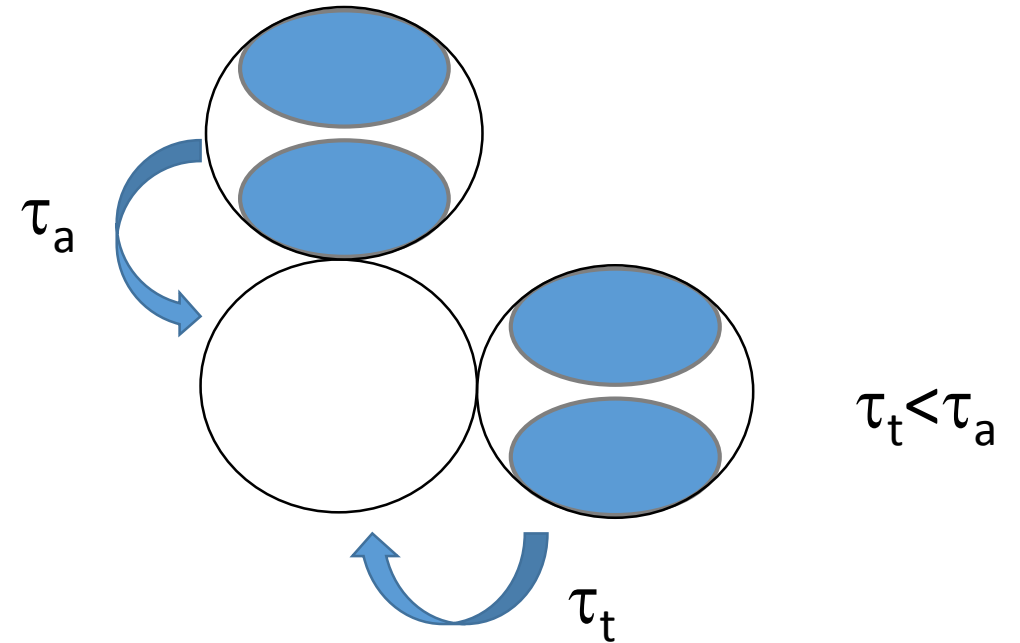
# P-flat band real space pattern



A site has higher proportion of Px orbital  
( $P_x/P_y \sim 6$ )

C site has higher proportion of Py orbital

Population on B site close to zero as expected  
for flat band



$$P_y(A) \tau_a = P_y(C) \tau_t$$



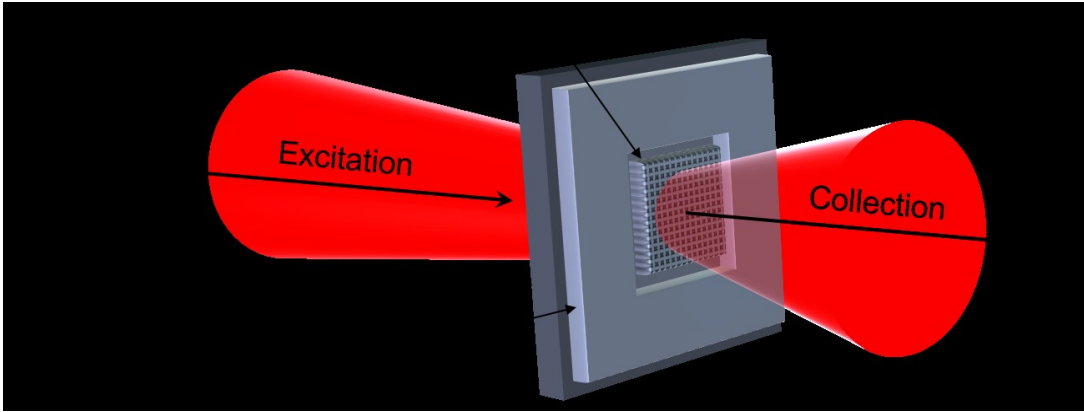
$$P_y(A) < P_y(C)$$



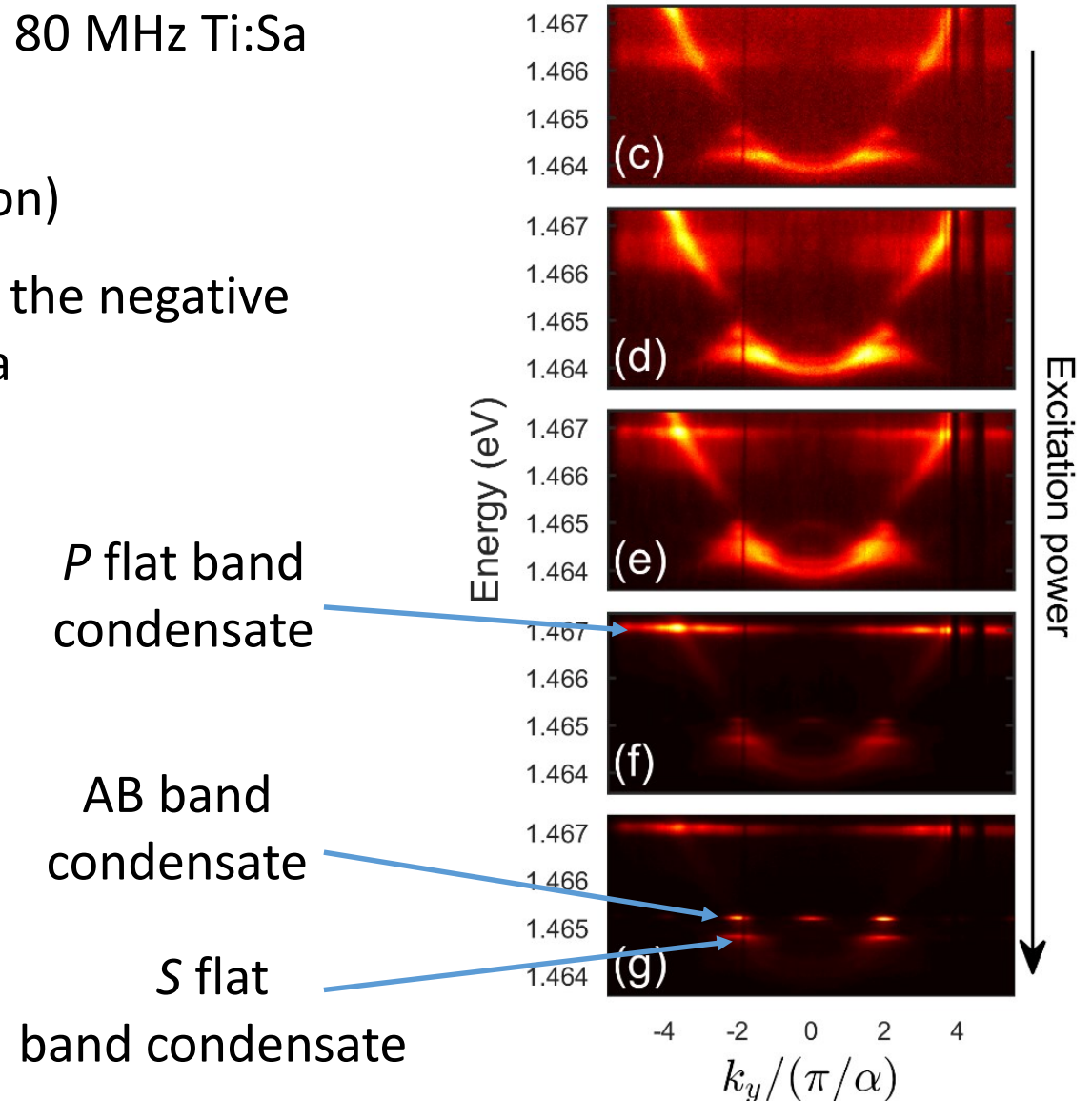
# Polariton condensation

- 100 ps horizontally-polarized pulses from an 80 MHz Ti:Sa laser
- Laser tuned to 843 nm ( $\sim 1$  meV below exciton)
- Polaritons condense into two flat bands and the negative effective mass states at the AB band maxima

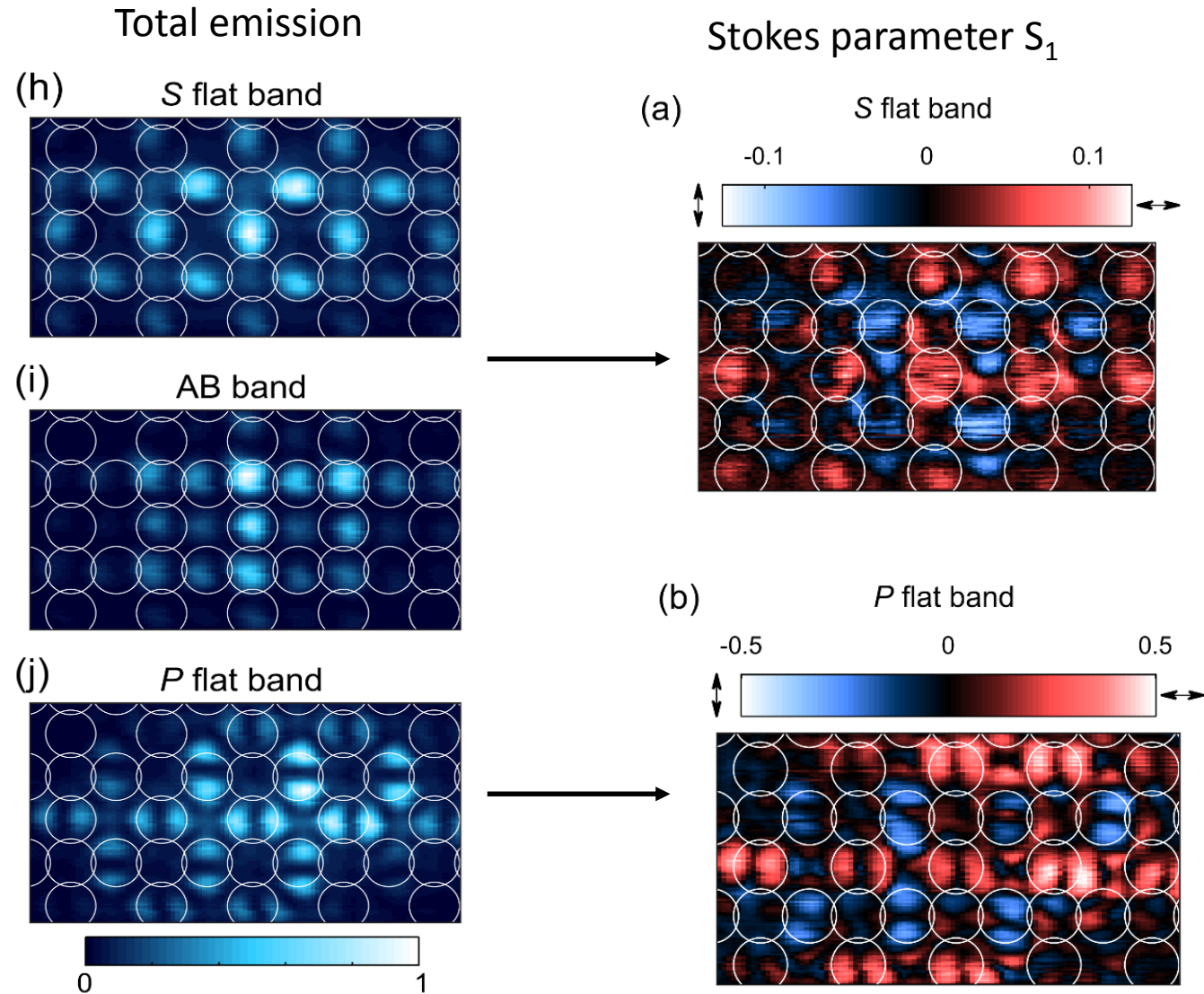
Excitation scheme



Power dependence at  $k = 0$



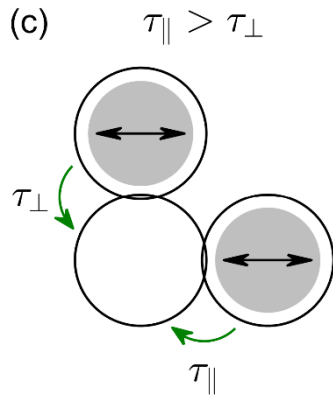
# Real space emission patterns



- Condensates formed on flat bands are localized on *A* and *C* sublattices
- Photonic spin-orbit coupling gives rise to pseudospin texture in flat band condensates

# Polarisation dependent tunnelling

$S$



Tight-binding model:

- $S$  band:

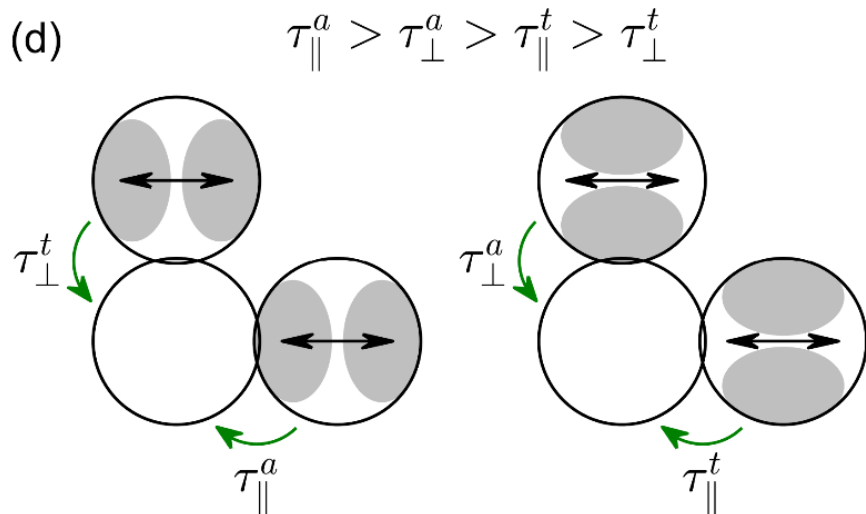
$$\tau_{||} = 0.165 \text{ meV}; \tau_{\perp} = 0.145 \text{ meV}$$

- $P$  band:

$$\tau_{||}^a = 0.375 \text{ meV}; \tau_{||}^t = 0.1 \text{ meV}$$

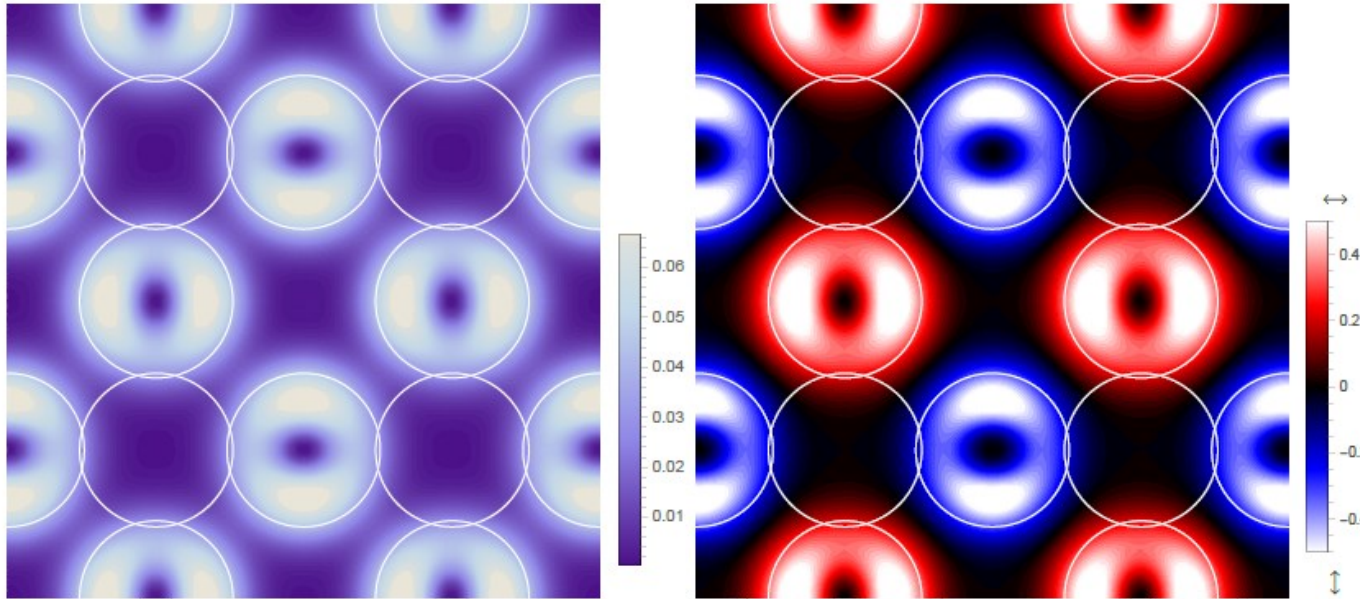
$$\tau_{\perp}^a = 0.125 \text{ meV}; \tau_{\perp}^t = 0.033 \text{ meV}$$

$P$



# Calculated real space emission patterns with polarisation

Calculated patterns for P flat band



Ratio of orbital populations: 6

$$|\Psi_{P_x}|^2 / |\Psi_{P_y}|^2 \text{ (A sites)}$$

$$|\Psi_{P_y}|^2 / |\Psi_{P_x}|^2 \text{ (C sites)}$$

Linear Polarisation degree

~0.5 for P flat band

~0.13 for S flat band

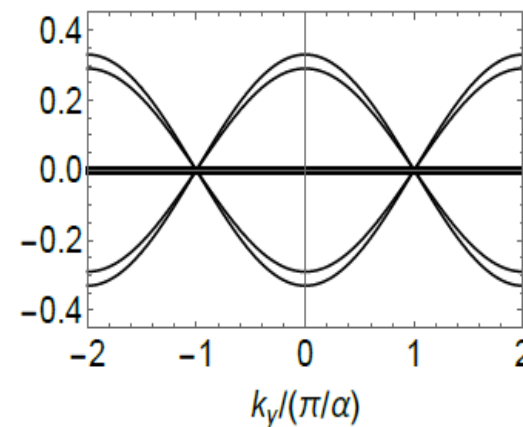
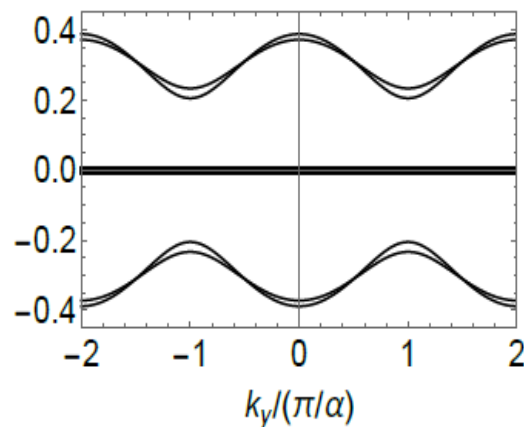
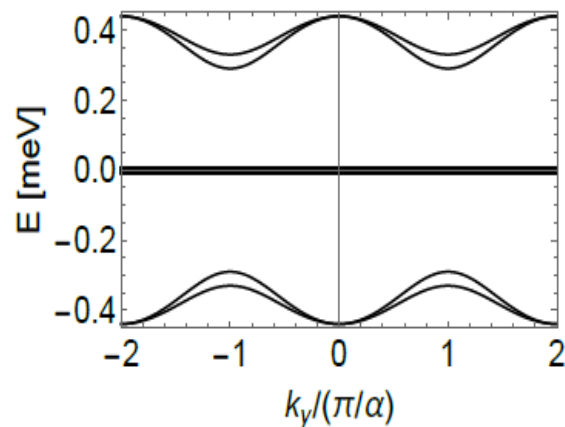
in agreement with the experiment



# Calculated Energy-momentum dispersions

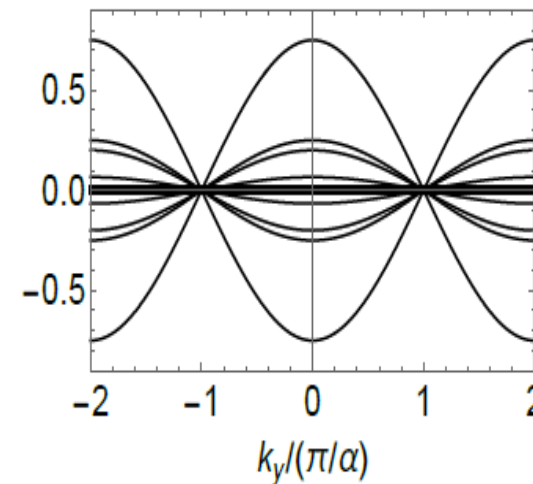
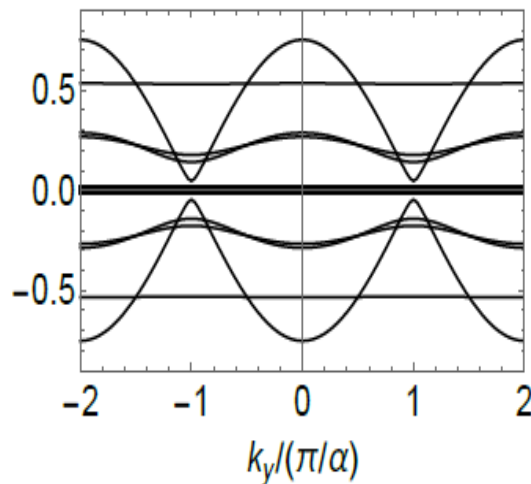
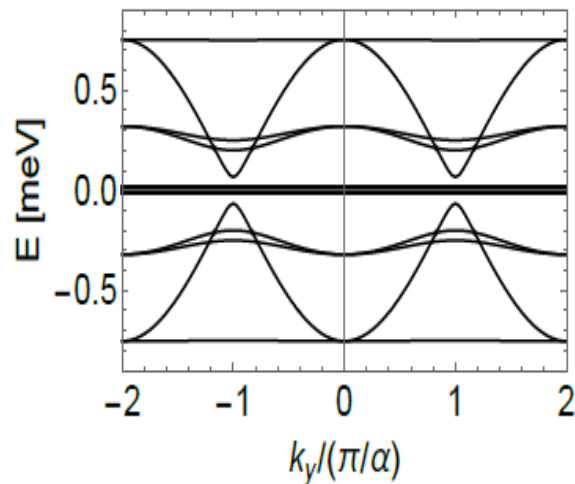
TB model with polarization

$S$



Dispersive bands are polarisation split

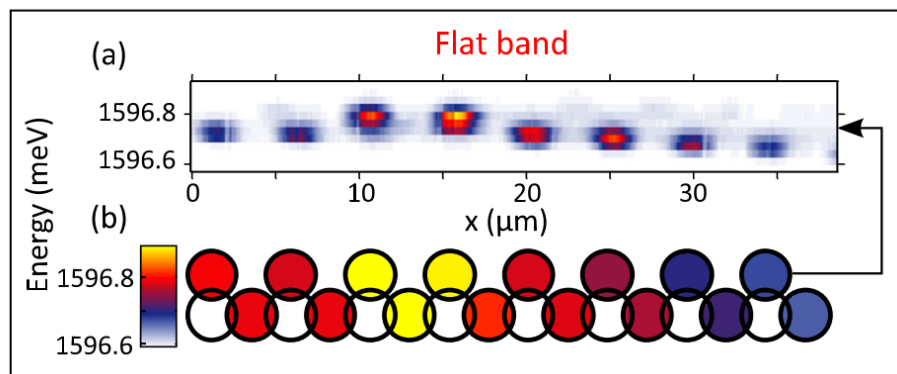
$P$



Flat bands are unaffected by polarisation dependent tunneling

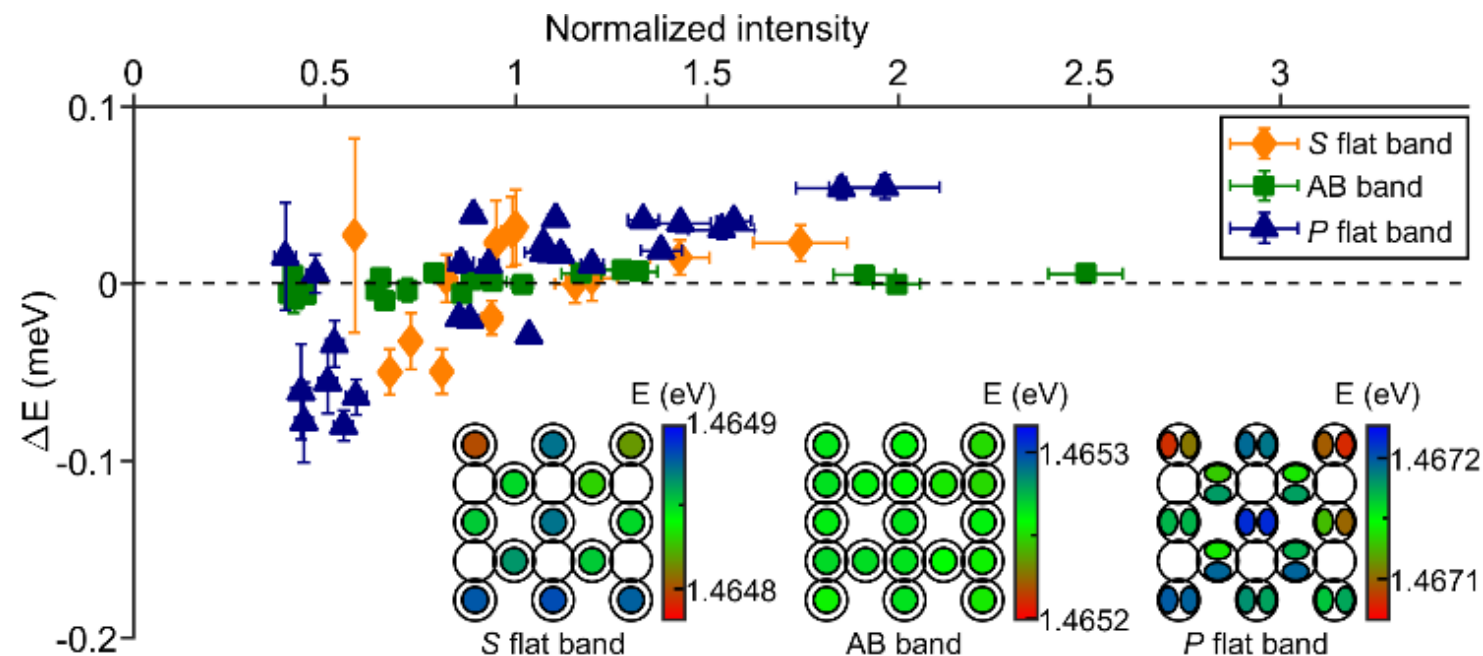
# Condensate fragmentation

1D case



*Phys. Rev. Lett.* **116**, 066402 (2016)

2D case



- Spatially-dependent blueshift of pillar modes seen in flat-band condensates
- Correlation between population and blueshift of orbitals shows role of interactions in spectral fragmentation. Interactions with reservoir are dominant

# Strength of polariton-polariton interaction

Blueshift of polariton energy at given k  $E_{shift} = g_{pol-pol} N_{pol}$  Polariton density

$$E_{shift} = g_{pol-pol} N_{pol} = \underbrace{g_{xx} N_{pol} |X|^4 / N_{QW}}_{\text{Blueshift of exciton resonance}} + \Delta\Omega |C|^2$$

Blueshift of exciton resonance

Exciton fraction      Photon fraction

Strength of exciton-exciton interactions  $g_{xx}$

Number of quantum wells  $N_{QW}$

Reduction of Rabi splitting due to screening of exciton resonance  
by exciton-exciton interactions  $\Delta\Omega = \beta_{xx} N_{pol} |X|^2 / N_{QW}$

# $g_{\text{pol-pol}}$ and $g_{xx}$ from literature

Measuring blueshift of polariton high density phase (condensate) in microcavities pumped resonantly or nonresonantly

*SRK Rodriguez, A Amo et al. arXiv preprint arXiv:1602.07114, Nature Comm (2016)*

$$g_{\text{pol-pol}} = 0.8 \mu\text{eV } \mu\text{m}^2; \text{ } g_{xx} = 30 \mu\text{eV } \mu\text{m}^2.$$

*Lydie Ferrier, et al and Jacqueline Bloch Phys. Rev. Lett. **106**, 126401 (2011)*

$$g_{\text{pol-pol}} = 2 - 10 \mu\text{eV } \mu\text{m}^2; \text{ } g_{xx} > 100 \mu\text{eV } \mu\text{m}^2.$$

*A.S. Brichkin et al PRB, 84, 195301 (2011)*

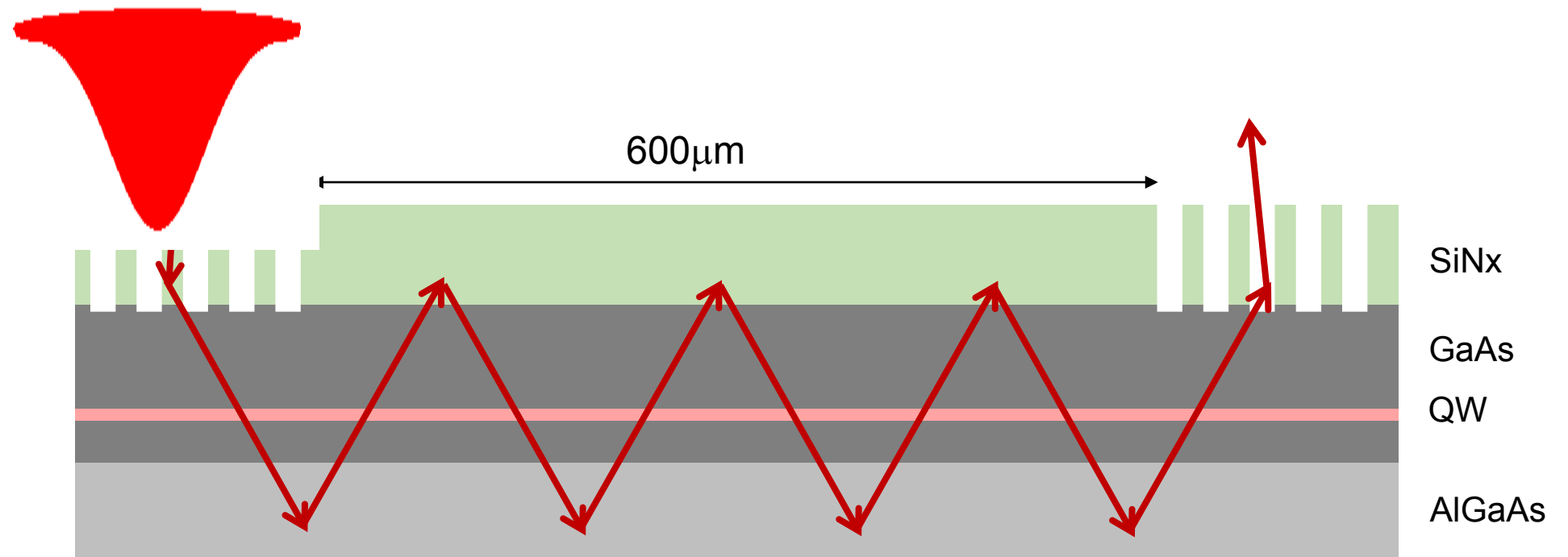
$$g_{\text{pol-pol}} = 0.07 \mu\text{eV } \mu\text{m}^2; \text{ } g_{xx} \sim 2-3 \mu\text{eV } \mu\text{m}^2.$$

consistent with theoretical estimate  $g_{xx} \sim 3a_B^2 E_B$

# Bright Temporal Solitons

<http://arxiv.org/abs/1409.0725> P.Walker et al., *DNK Nature Comm.* 2015

Inject 350fs pulse through a grating. Let it propagate 600  $\mu\text{m}$  and extract it through a second grating.



# Comparison with other photonic systems

From soliton threshold estimate the nonlinear parameter and nonlinear refractive index:

*P.Walker, et al., DN Krizhanovskii Nature Comm. 6, 8317 (2015)*

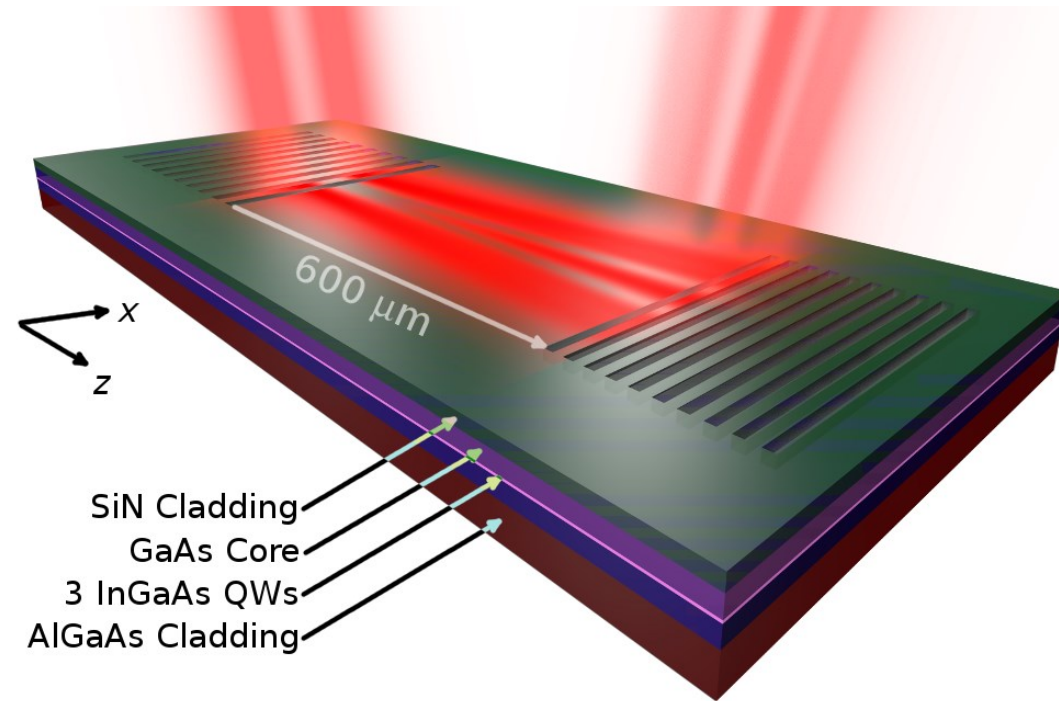
$L_{NL} \approx \frac{1}{\Delta k} = \frac{v_g \hbar}{E_{shift}}$  - the length over which nonlinear phase is 1 rad

$$L_{NL} \approx L_D \approx 40 - 50 \mu\text{m}$$

Excitonic nonlinearity  $g_{xx} = 4\text{-}12 \mu\text{eV} \mu\text{m}^2$

|   | Polariton GaAs system   | AlGaAs waveguides     | Silicon PhC         | InGaP PhC           |
|---|-------------------------|-----------------------|---------------------|---------------------|
| Nonlinear Index $n_2$ ( $\text{W}^{-1}\text{m}^2$ ) | $10^{-14}$ - $10^{-13}$ | $1.8 \times 10^{-17}$ | $6 \times 10^{-18}$ | $6 \times 10^{-18}$ |

# Strength of polariton-polariton interactions for CW pump



- Inject fluids containing amplitude and phase defects.
- Vary the density of the polariton fluid and observe the changes after nonlinear propagation.
- Formation of dark polariton solitons

*P.Walker, et al., DN Krizhanovskii Nature Comm. 6, 8317 (2015)*

*P.Walker et al., DN Krizhanovskii, arXiv preprint arXiv:1703.08351 (2016)*

# Estimation of $g_{pol-pol}$ from CW dark soliton

$$g_{pol-pol} = \frac{\hbar^2}{2M_{x_{eff}}\xi^2 N_{pol}}$$

$M_{x_{eff}}$  - polariton effective mass in transverse direction of waveguide

$\xi$  - dark soliton FWHM or healing length

$N_{pol}$  - polariton density of dark soliton background

$g_{pol-pol} \approx 5 \mu\text{eV} \mu\text{m}^2$       Taking into account  $|X|^2=0.5$  and  $N_{QW}=3$

$g_{xx} \sim 60 \mu\text{eV} \mu\text{m}^2$



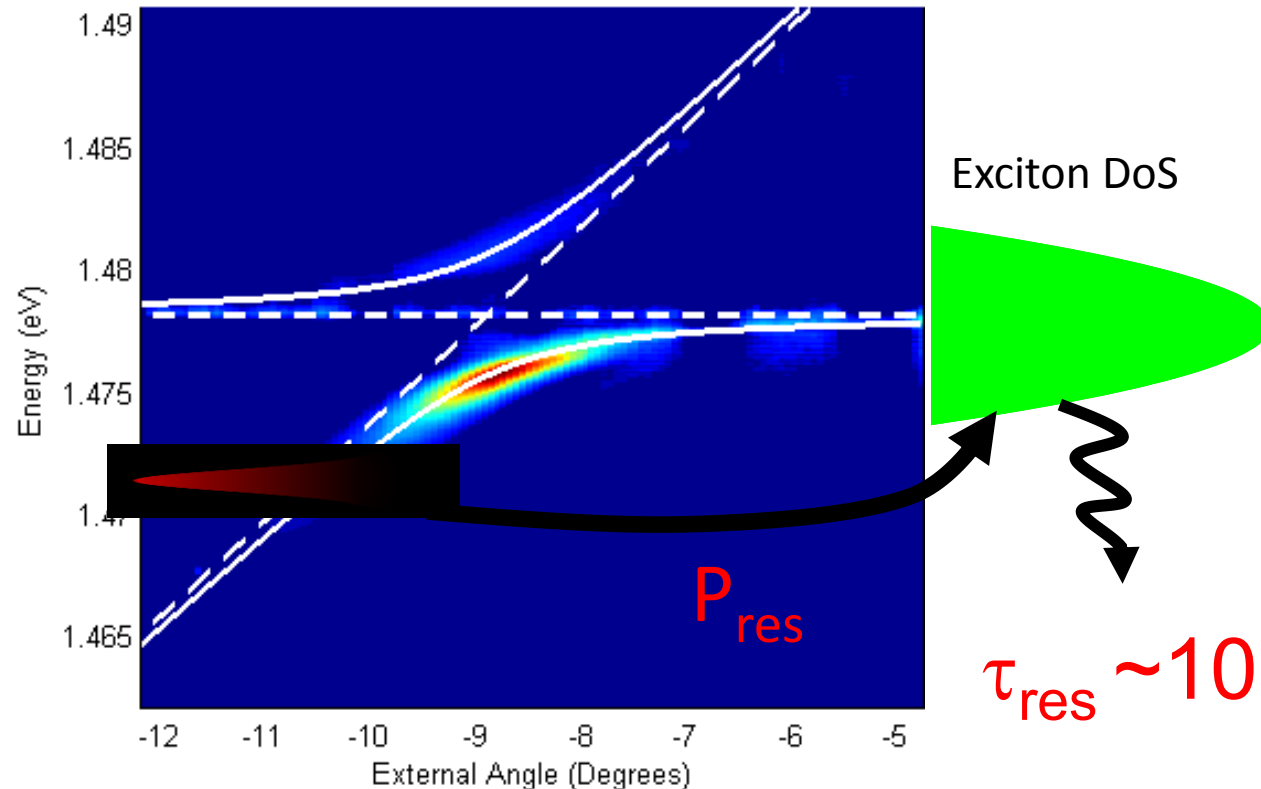
An order of magnitude larger than  
in case of ps pulsed excitation



# Population of exciton reservoir under CW pump

*D Sarkar, SS Gavrilov, Physical review letters 105 (21), 216402 (2010)*

*DN Krizhanovskii, et al Solid state communications 119 (7), 435-439 (2001)*



## Exciton reservoir:

Localised excitons not coupled to cavity mode

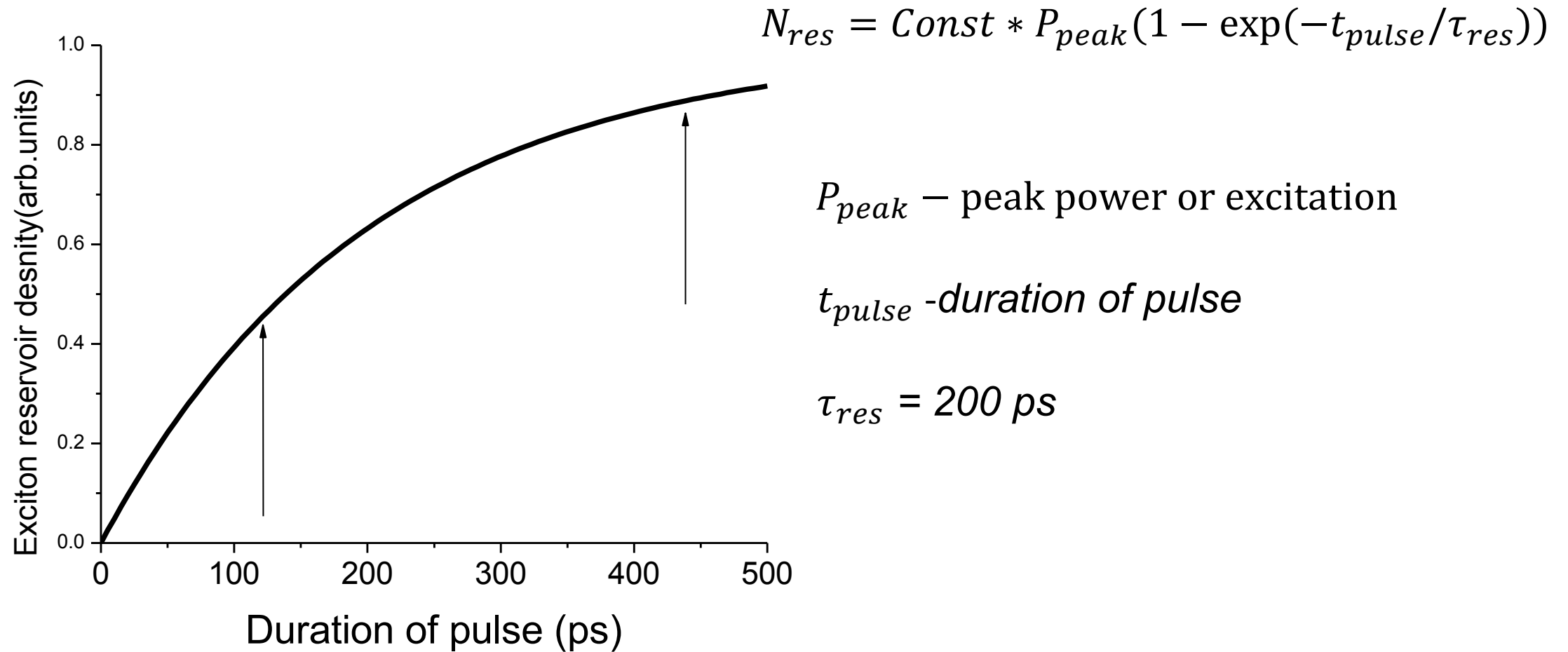
Dark excitons

Excitons with high momenta

Pumping of reservoir directly or via excitation of biexcitons with two linearly polarised polaritons

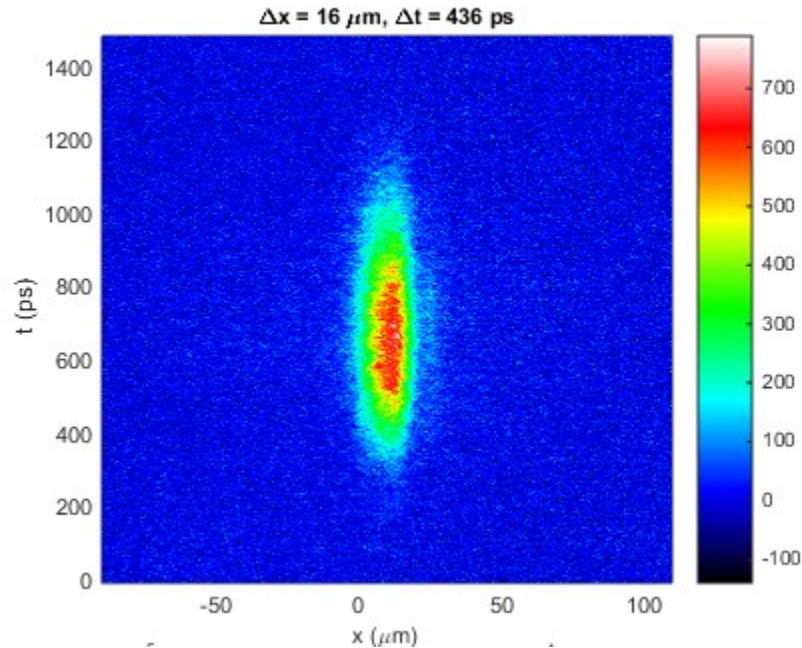
$\tau_{res} \sim 10's-100's \text{ ps}$

# Reservoir density vs duration of excitation

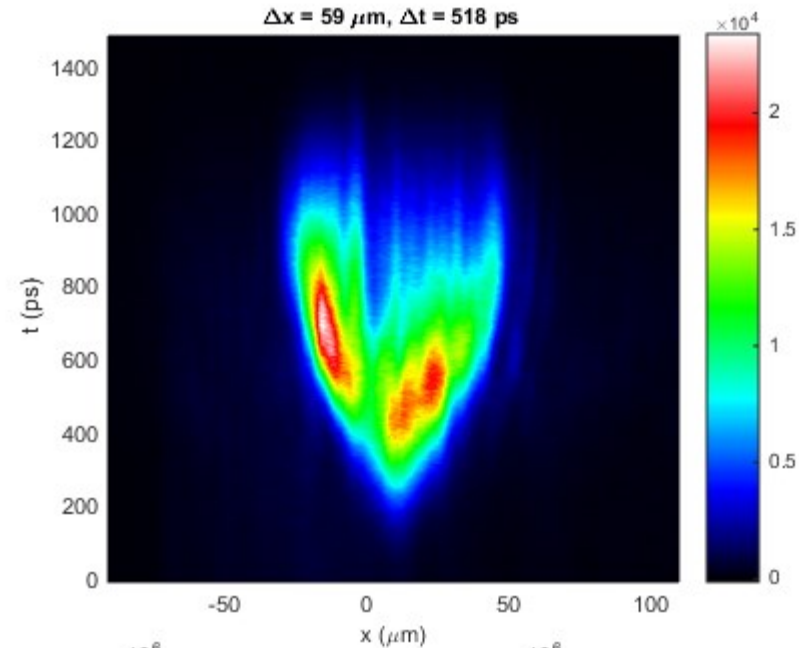


# 450-ps Pulse Spatial Defocussing

13 mW



1.3 W

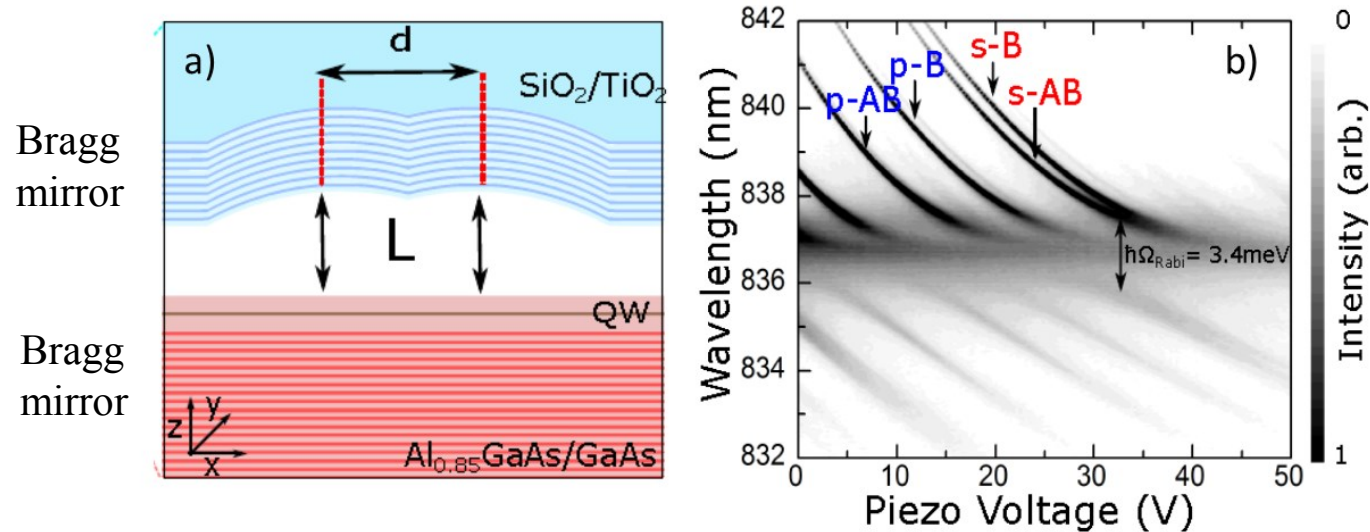


450 ps long pulse      Temporal offset of outer spatial harmonics by 100-200 ps.

Surprisingly tail of the pulse experiences large defocusing

# TOWARDS QUANTUM POLARITONS IN LATTICES

Active media- GaAs-based quantum well



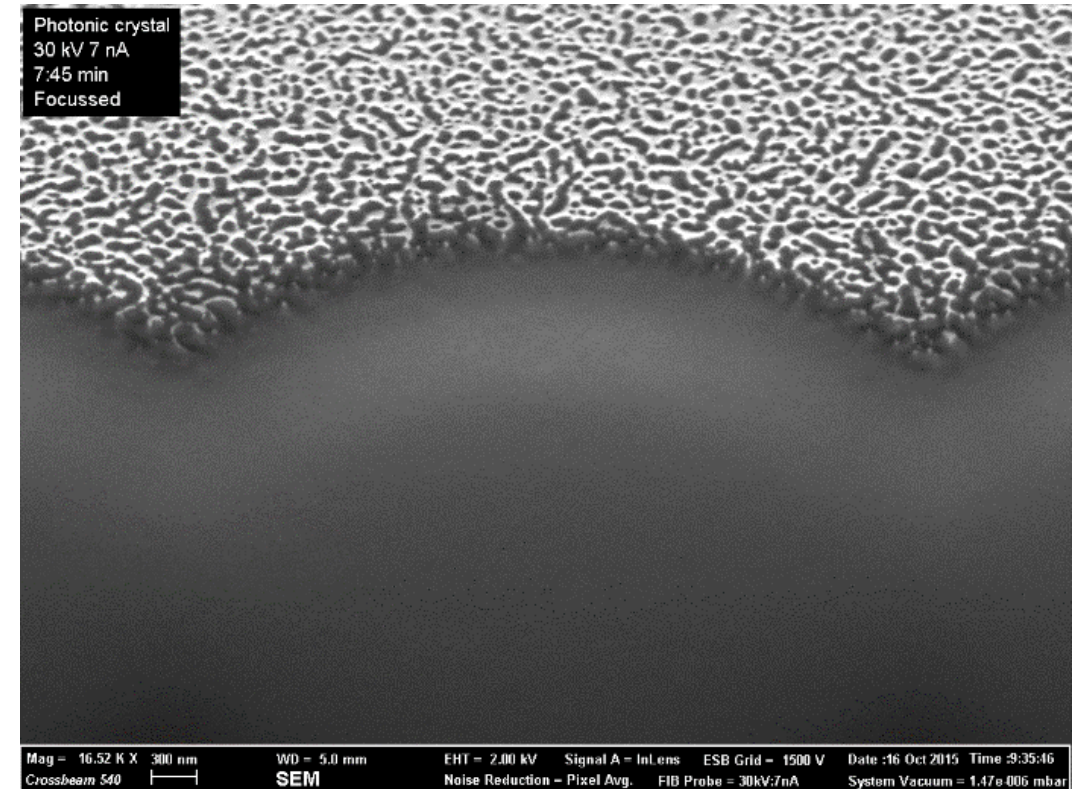
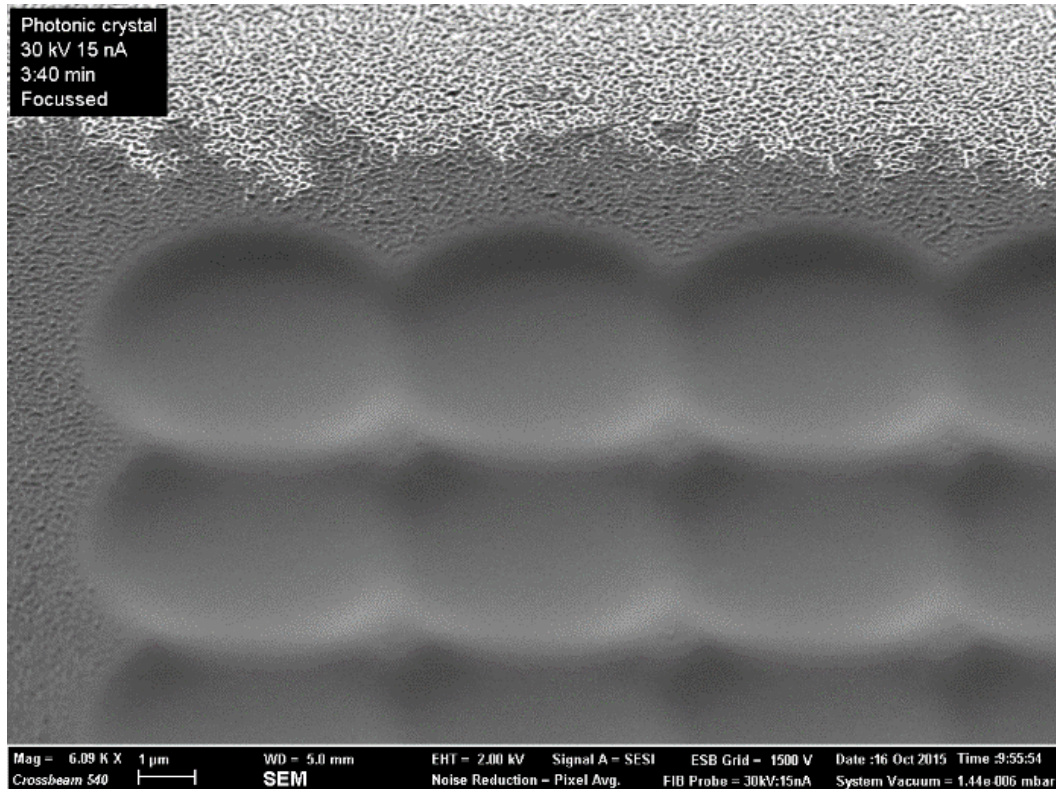
Q-factor  $\sim$  up to 150 000 .

*Dufferwiel, DNK et al Applied Physics Letters 107 (20), 201106 (2015); Phys. Rev. Applied 3, 014008 (2015)*

Strong **lateral** confinement ( $\sim 500 \text{ nm}$ )  $\Rightarrow$  strong polariton-polariton interactions in lattice sites  $U \sim 20 \text{ } \mu\text{eV}$  (maybe further increased up to 100's  $\mu\text{eV}$ )

Scalable system  $\Rightarrow$  My group in collaboration with J Smith (Oxford) demonstrated high-quality photonic molecules, lattices of 3D boxes in progress.

# Fabrication of open MC lattices for topological photonics (Oxford, J Smith's group)





# Summary

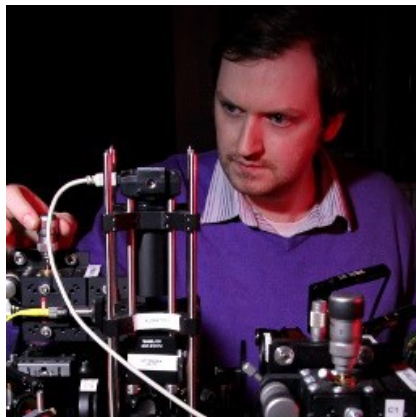
- Full 2D Lieb lattice of etched micropillars
- Flat bands formed by  $S$  and  $P$  orbitals
- Condensation observed in both flat bands and AB band
- Photonic spin-orbit coupling provides pseudospin texture
- Spectral profiles of condensates are spatially-inhomogeneous for flat bands
- Interactions are not very strong and there is effect of reservoir

# Acknowledgements

## Experiment



Charles Whittaker  
(Sheffield)



P. M. Walker (Sheffield)



Prof. M. S. Skolnick (Sheffield)



The  
University  
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## Theory



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Ivan Iorsh

Samples, Sheffield University:  
Ed Clarke  
Ben Royal  
Deivis Vaietikis

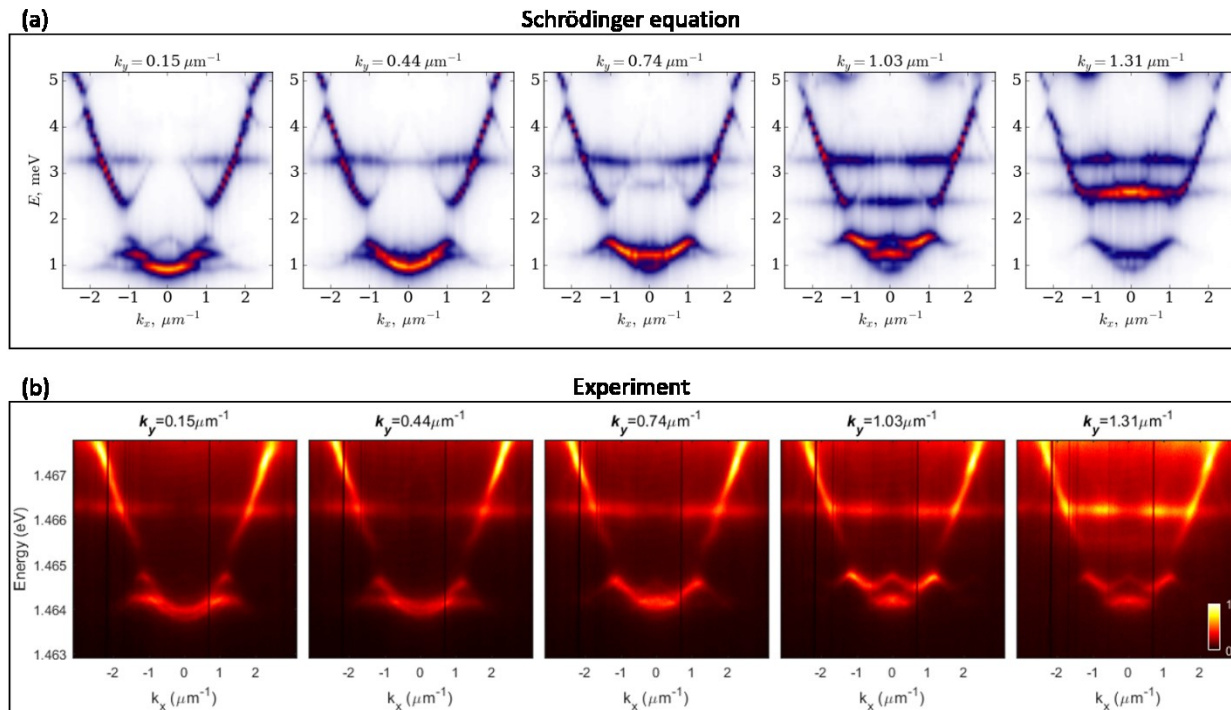
Thanks for listening!



Supplementary material

# Schrödinger equation

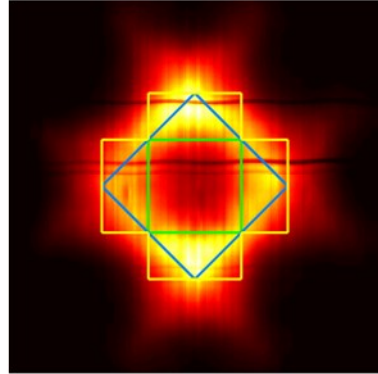
- 10 meV confinement potential
- $m^* = 5 \times 10^{-5} m_0$
- 0.1 meV lifetime



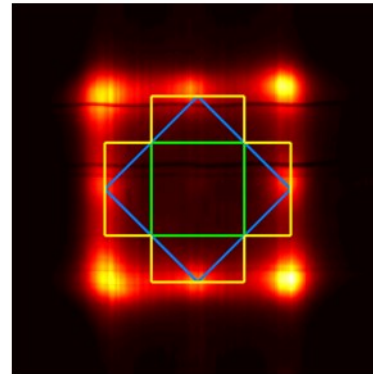
# Fourier space emission

Below  
threshold

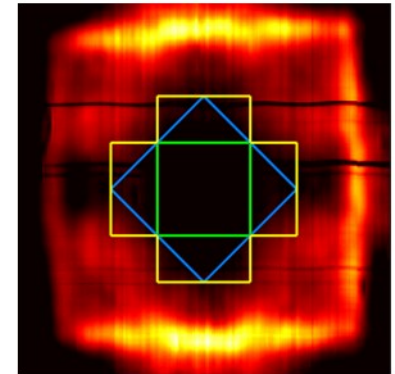
S flat band



AB band



P flat band



Above  
threshold

