



# spontaneously magnetized exciton-polariton condensates: switches and lattices

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South Korea 2017

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# Motivation

- Non-equilibrium system
- Solid state technology, room temperature condensation
- Fast dynamics



Spin lattices



Devices  
(Switches, TRNGs)

# So-called “Simulators”

**nature physics**

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NATURE PHYSICS | REVIEW

## Quantum simulations with ultracold quantum gases

Immanuel Bloch, Jean Dalibard & Sylvain Nascimbène

Affiliations | Corresponding author

*Nature Physics* 8, 267–276 (2012) | doi:10.1038/nphys2259

Received 26 January 2011 | Accepted 13 February 2012 | Published online 02 April 2012

frontiers in  
PHYSICS

## Ising formulations of many NP problems

Andrew Lucas \*

Lyman Laboratory of Physics, Department of Physics, Harvard University, Cambridge, MA, USA

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REVIEW ARTICLE  
published: 12 February 2014  
doi: 10.3389/phy.2014.00005

We provide Ising formulations for many NP-complete and NP-hard problems, including all of Karp’s 21 NP-complete problems. This collects and extends mappings to the Ising model from partitioning, covering, and satisfiability. In each case, the required number of spins is at most cubic in the size of the problem. This work may be useful in designing adiabatic quantum optimization algorithms.

**Keywords:** spin glasses, complexity theory, adiabatic quantum computation, NP, algorithms

**nature photonics**

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NATURE PHOTONICS | LETTER

日本語要約

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## Network of time-multiplexed optical parametric oscillators as a coherent Ising machine

Alireza Marandi, Zhe Wang, Kenta Takata, Robert L. Byer & Yoshihisa Yamamoto

Affiliations | Contributions | Corresponding author

*Nature Photonics* 8, 937–942 (2014) | doi:10.1038/nphoton.2014.249

Received 30 June 2014 | Accepted 19 September 2014 | Published online 26 October 2014

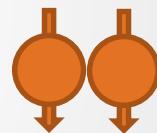
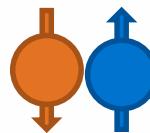


# Key elements of a “simulator” or spin model

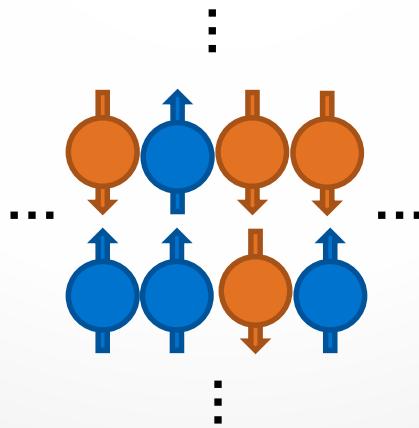
1. Binary state, which can be initialized



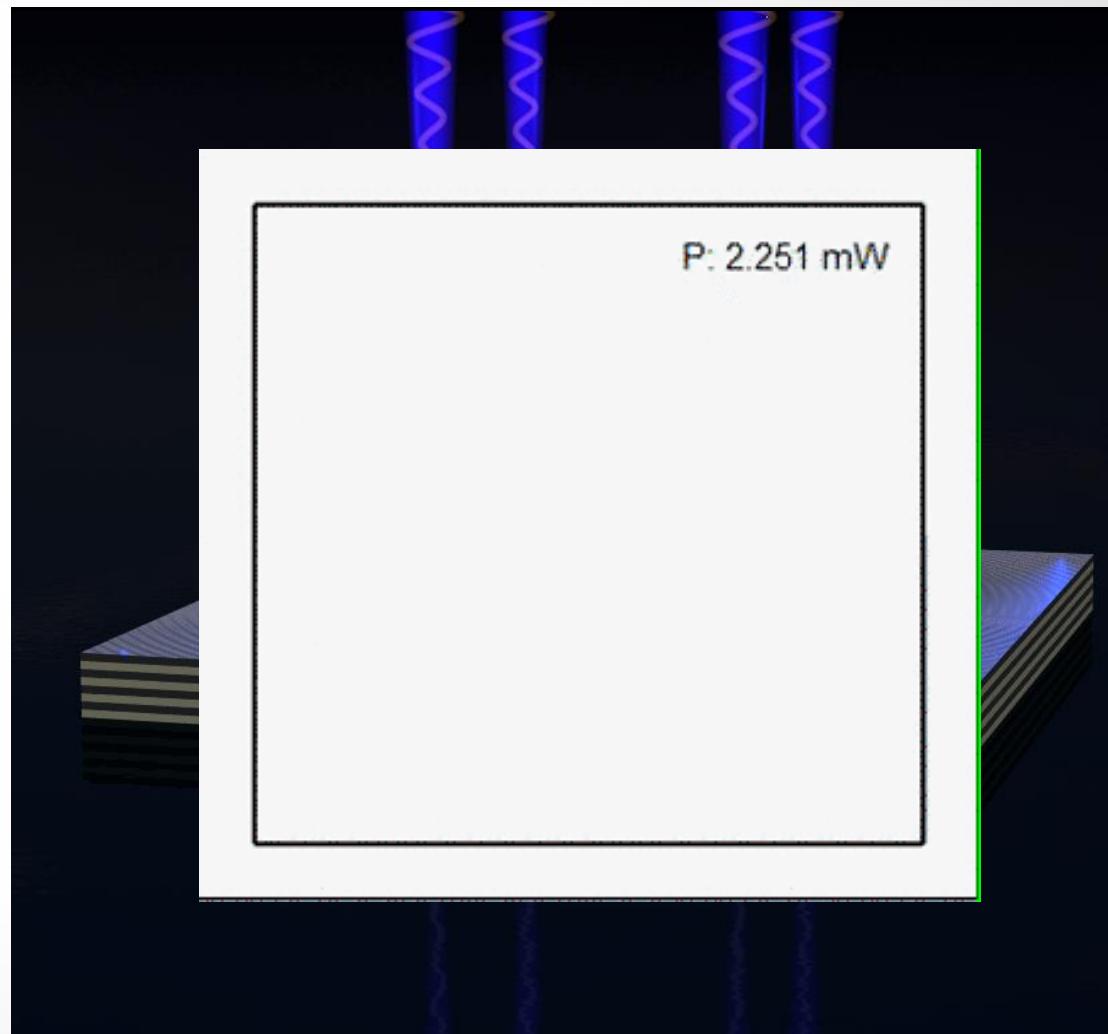
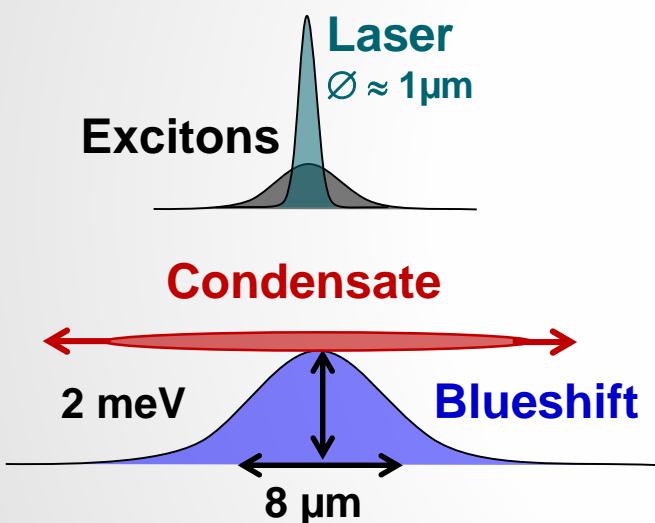
2. Tunable interactions between two



3. Scalable lattices



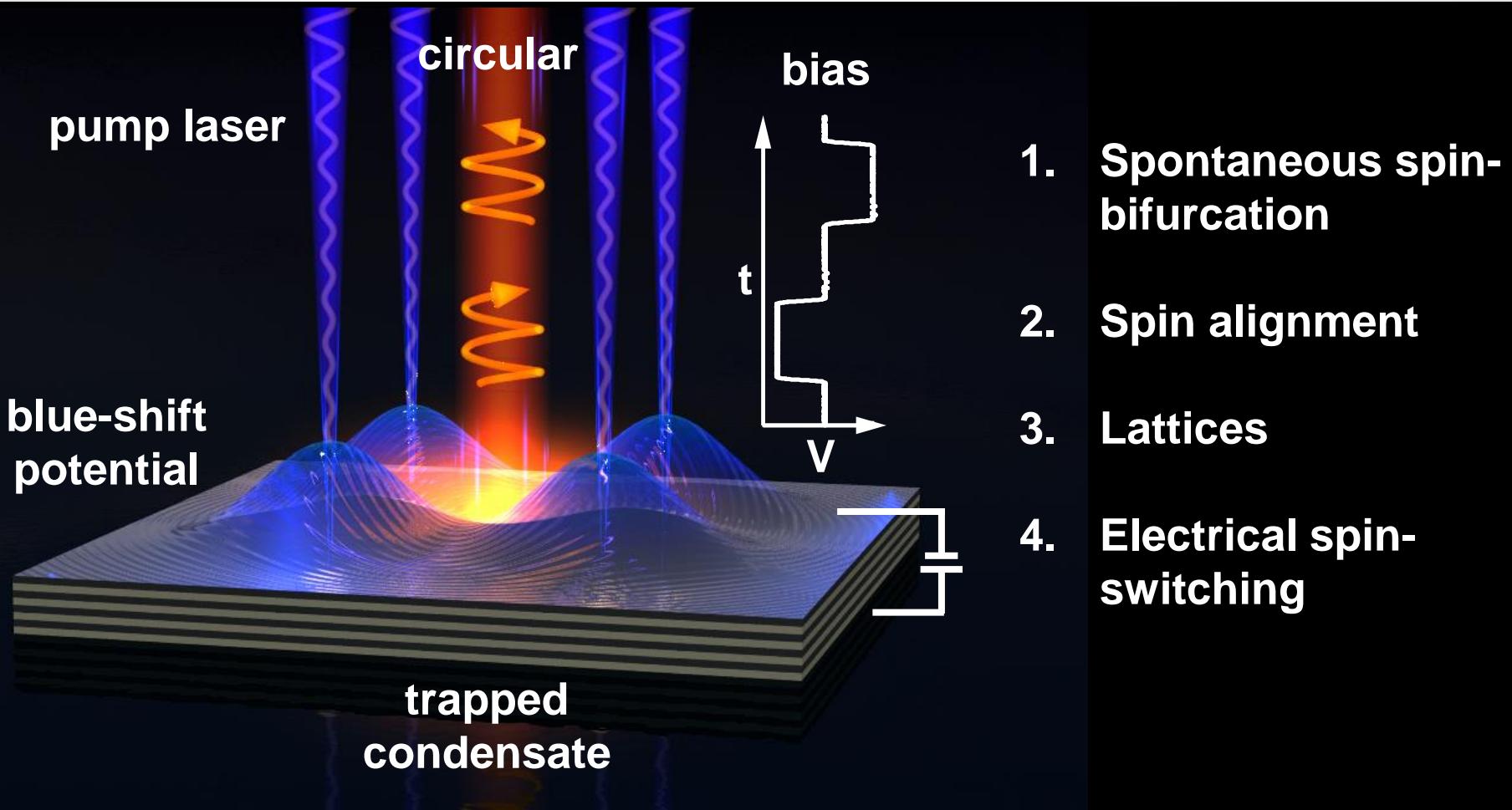
# Polariton condensates in optical traps

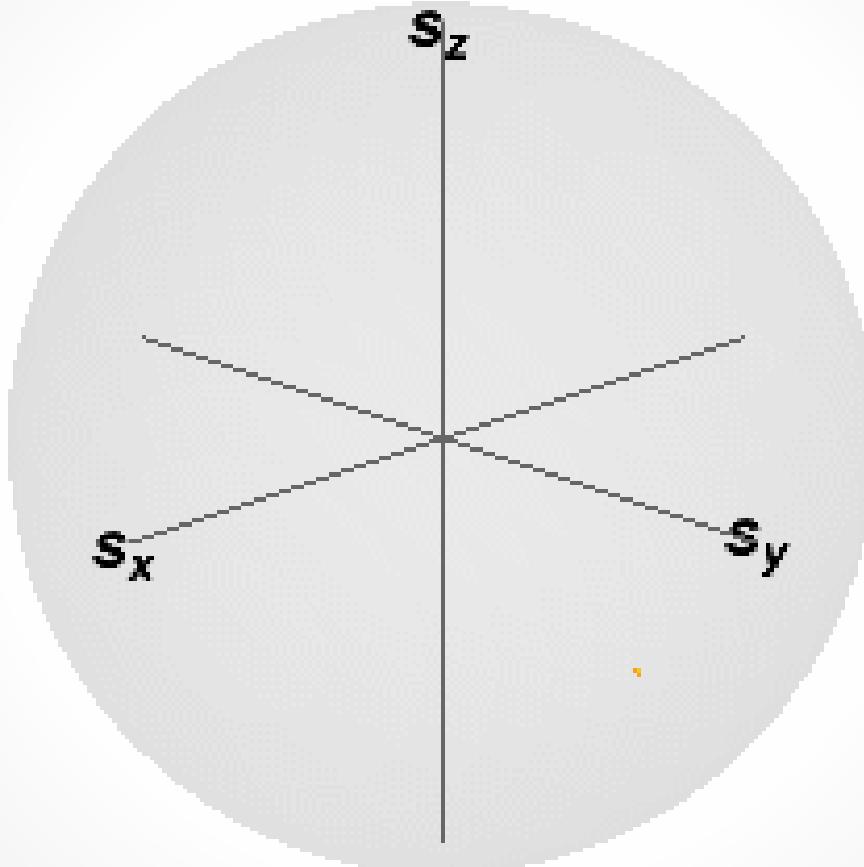


Nat. Phys. 8, 190 (2012), Nat. Comm. 3, 1243 (2012),  
PRL 110, 186403 (2013), PNAS 111, 8770 (2014)



# Outline





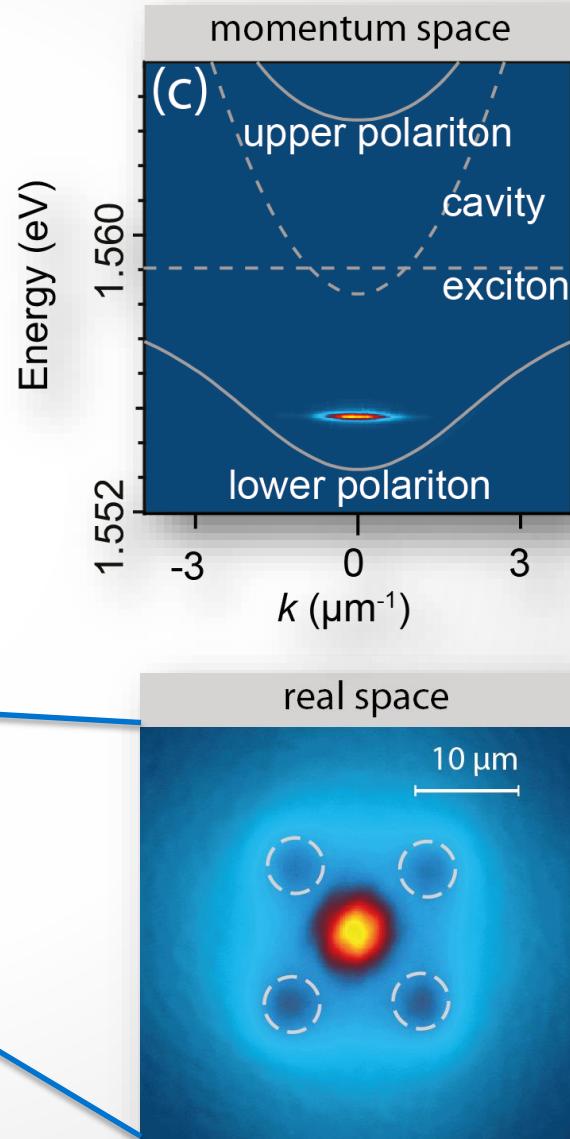
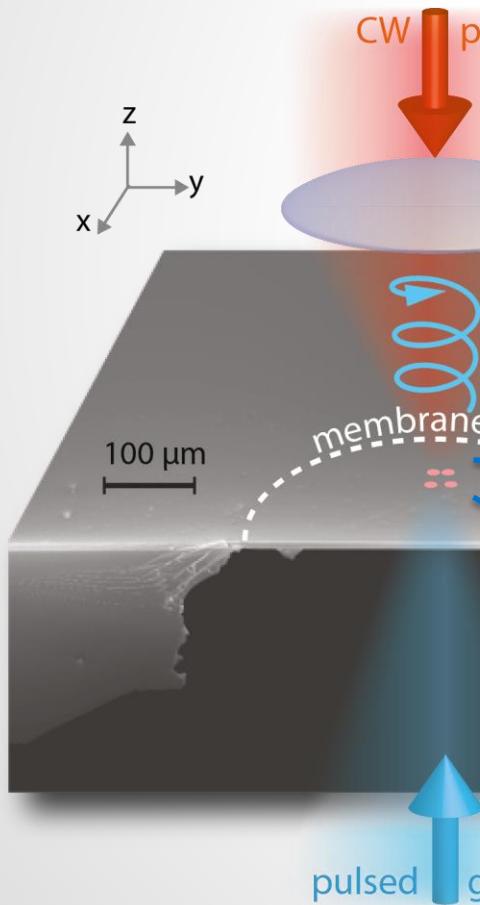
Part 1

## Spin Bifurcation

PRX (2015)

# Membrane microcavity

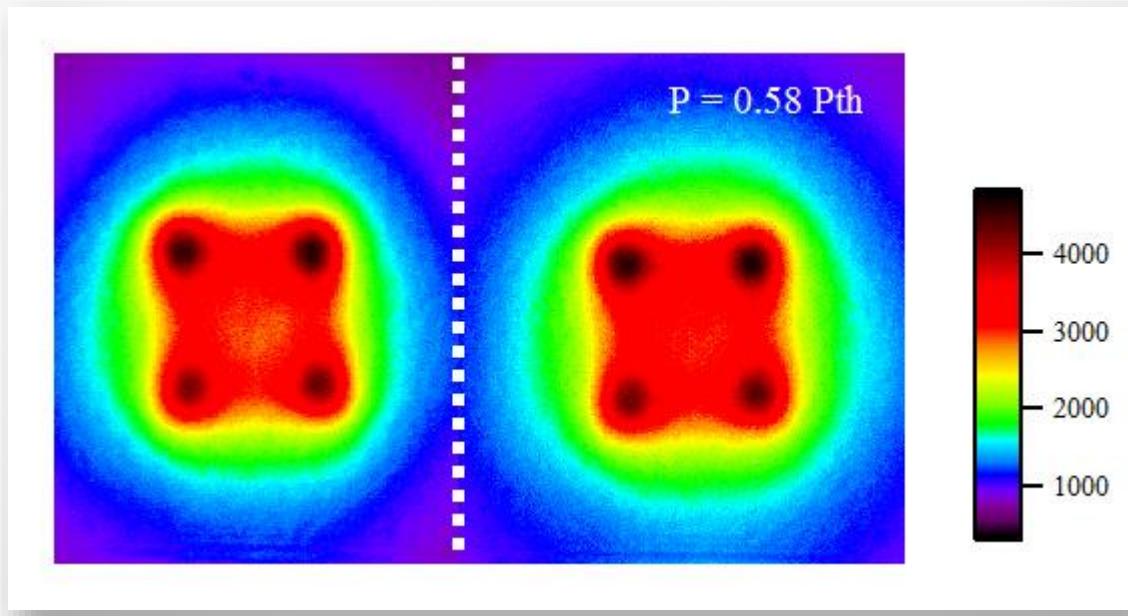
- non-resonant CW pump
- separated reservoirs



# Circular polarisation with linearly polarised pump

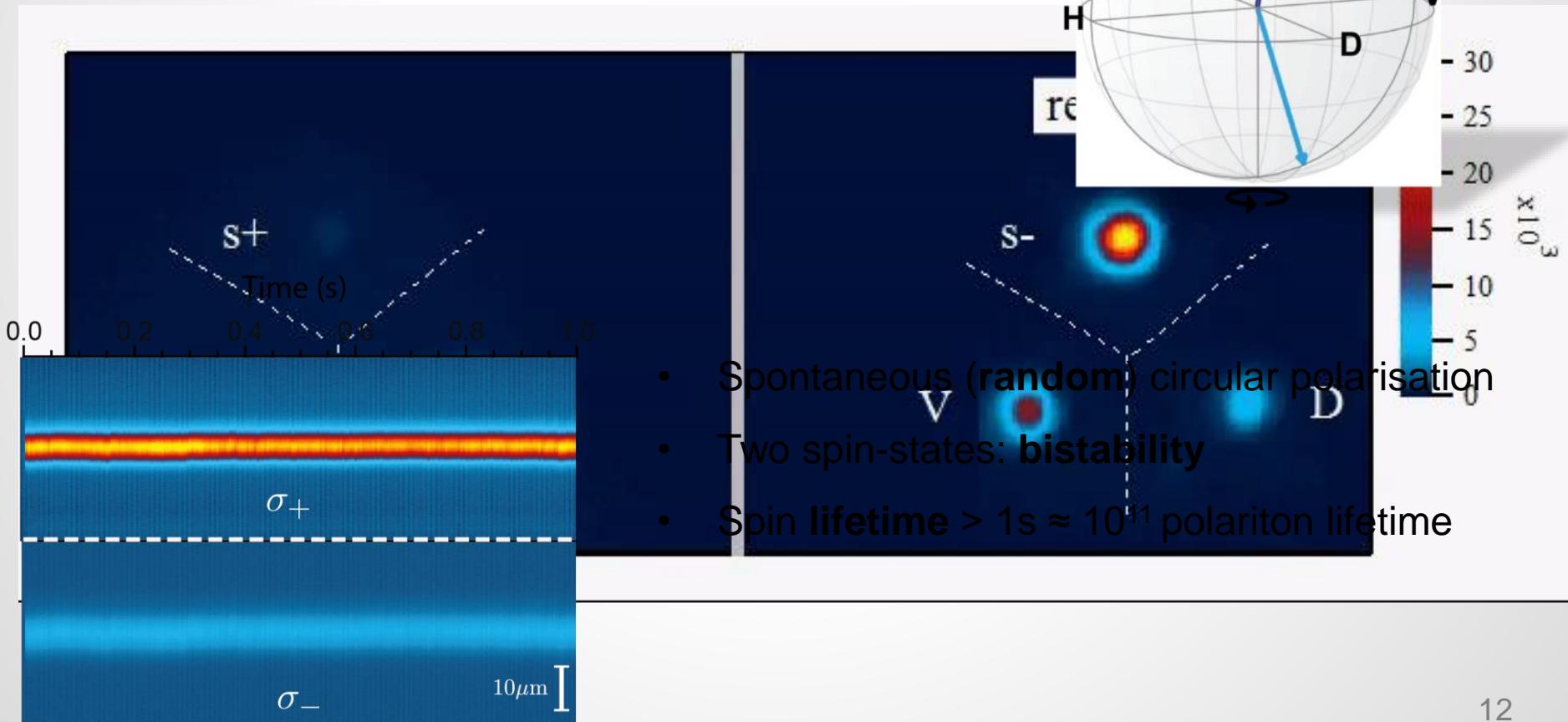
$\sigma_-$

$\sigma_+$

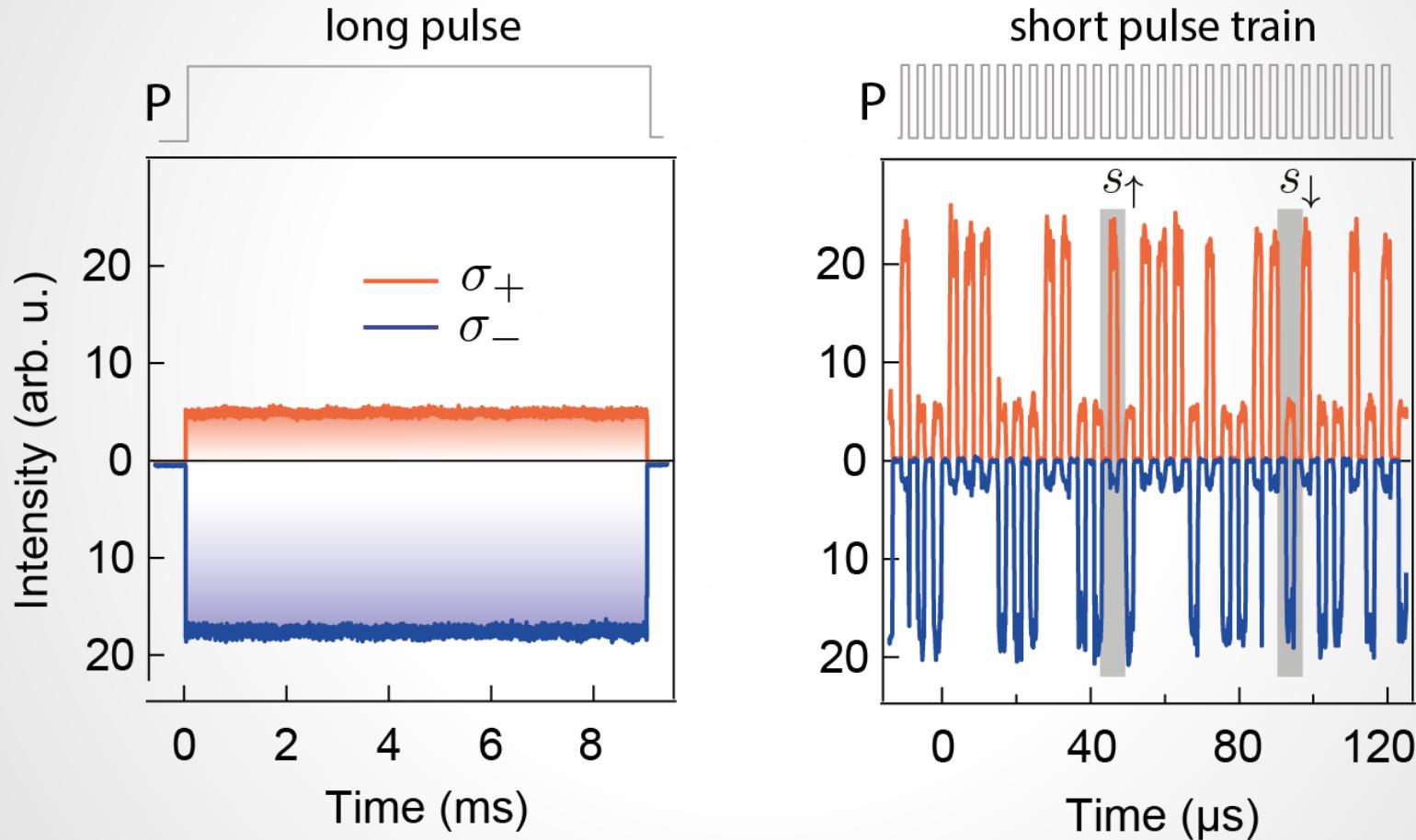


**unusual:** previous works reported **linear** polarisation

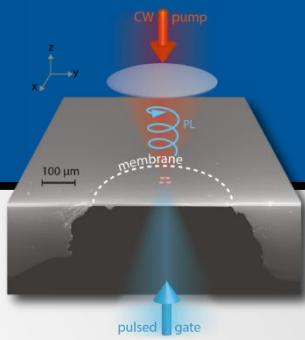
# Spontaneous parity breaking



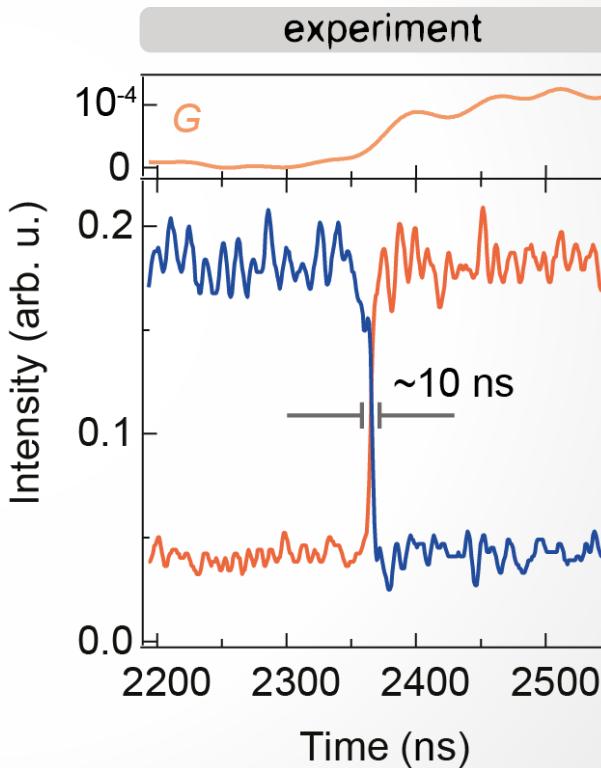
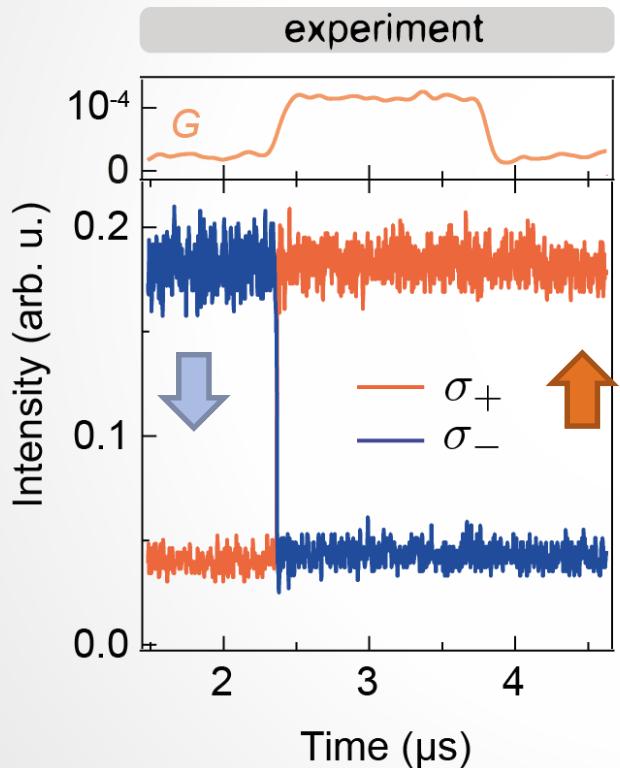
# Stochastic behaviour



# Spin Switching (experiment)



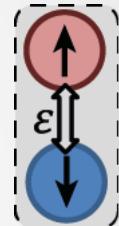
- linear pump: random
- weak  $\sigma_+$  gate:  $10^{-2} N$ , resonant



- switching energy  $\sim 1 \text{ fJ}$
- switches with  $\sim 10$  polaritons

# Key requirements of spin bifurcation

- Nonlinearity  $\frac{d\psi}{dt} = a\psi + \alpha|\psi|^2\psi$
- Linear polarization energy splitting (coupling between spins)
- Lifetime difference between linear polarization modes



# Spontaneous spin bifurcation – theory

$$\Psi = \begin{bmatrix} \psi_+ \\ \psi_- \end{bmatrix}$$

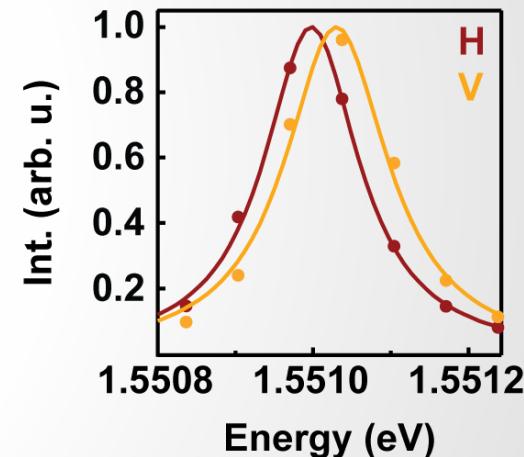
$$i \frac{d\Psi}{dt} = -\frac{i}{2} g(S) \Psi - \frac{i}{2} (\gamma - i\varepsilon) \sigma_x \Psi + \frac{1}{2} [(\alpha_1 + \alpha_2)S + (\alpha_1 - \alpha_2)S_z \sigma_z] \Psi$$

linear polarisation

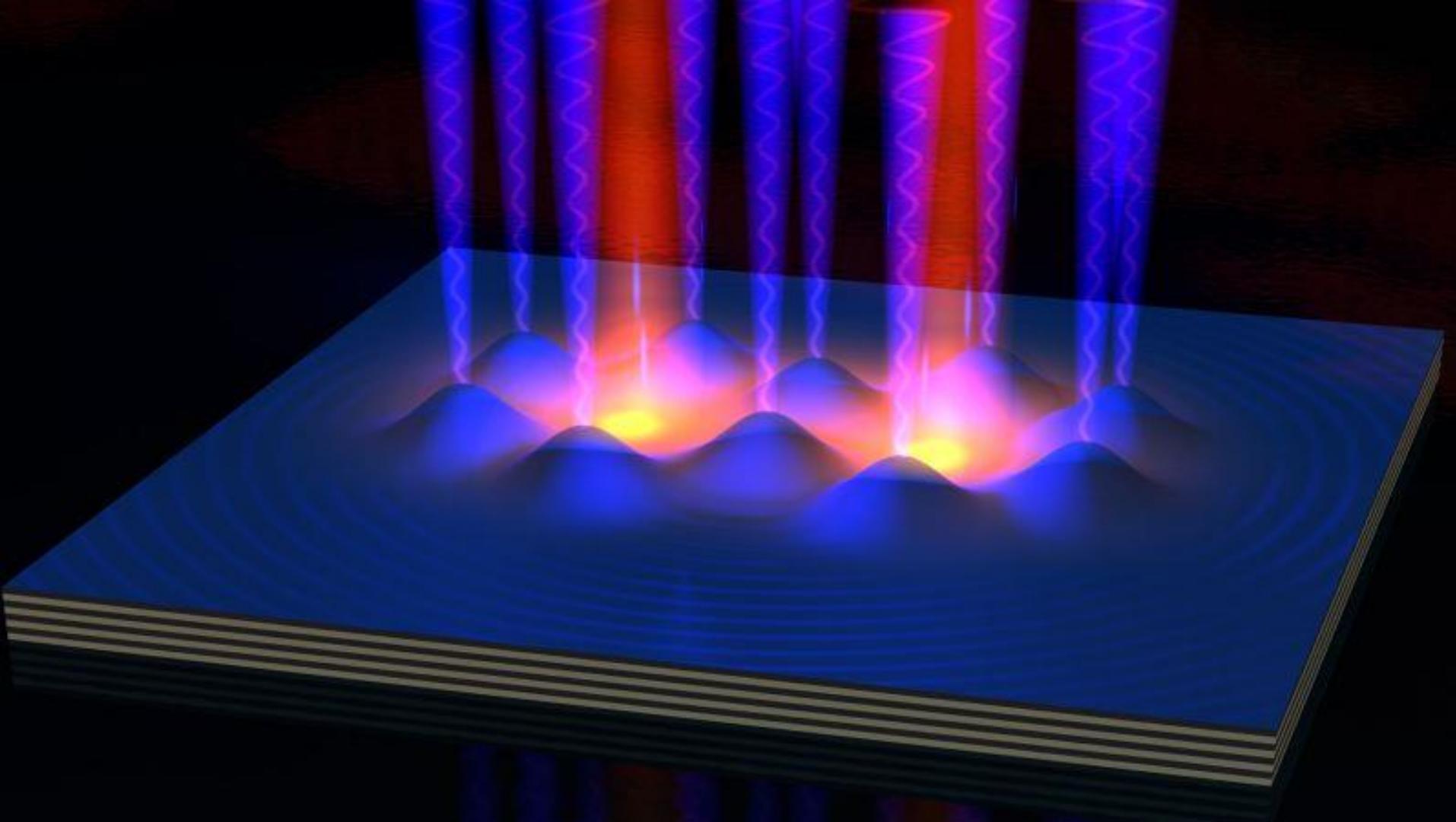
decay rate splitting + energy splitting

pump & decay

polariton-polariton interactions

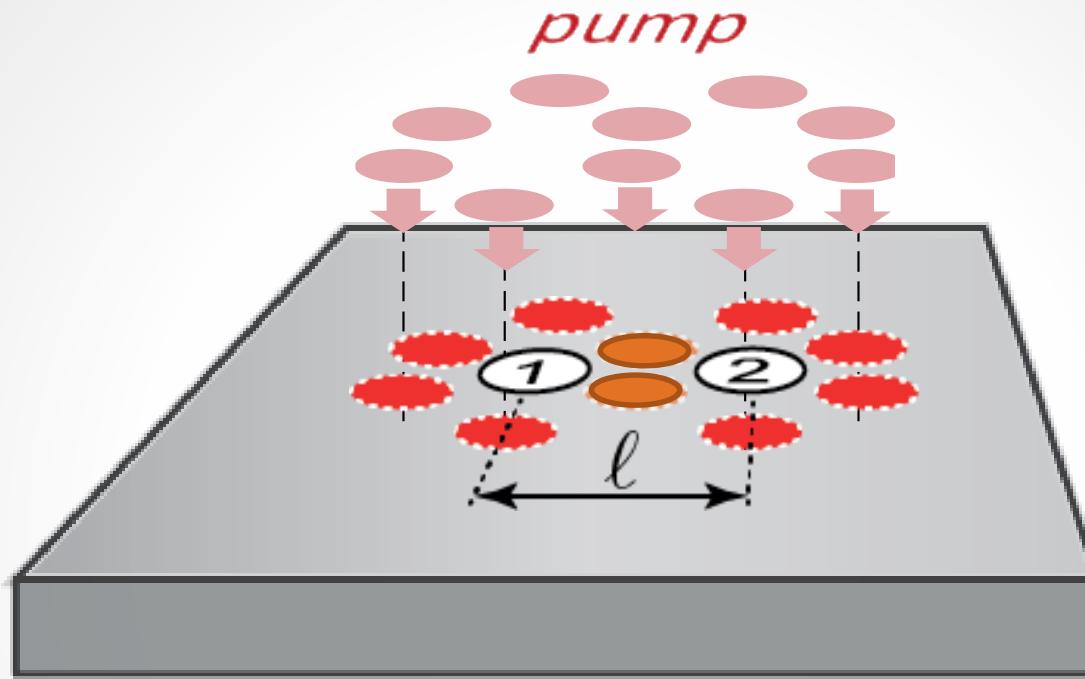


$$\gamma \approx 0.1 \varepsilon$$



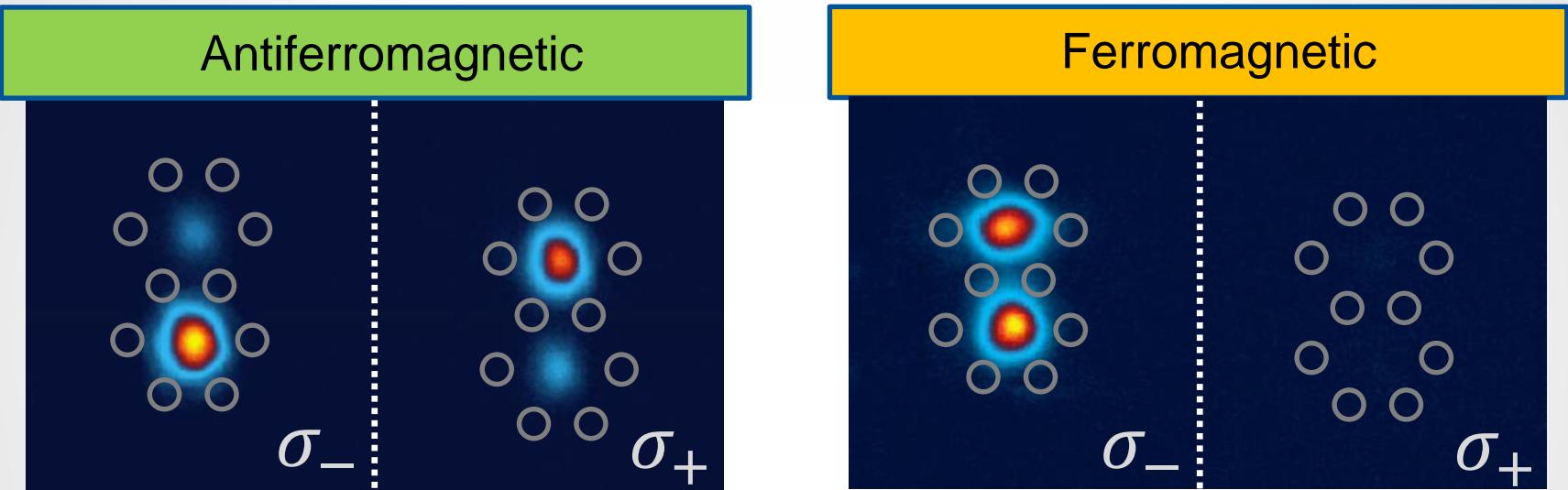
**Part 3**  
**Spin alignment**  
PRL (2016)

# Pumping geometry



- Hexagonal **nonresonant CW pump**
- Playing parameters: **barrier** (continuous) or **separation** (discrete)

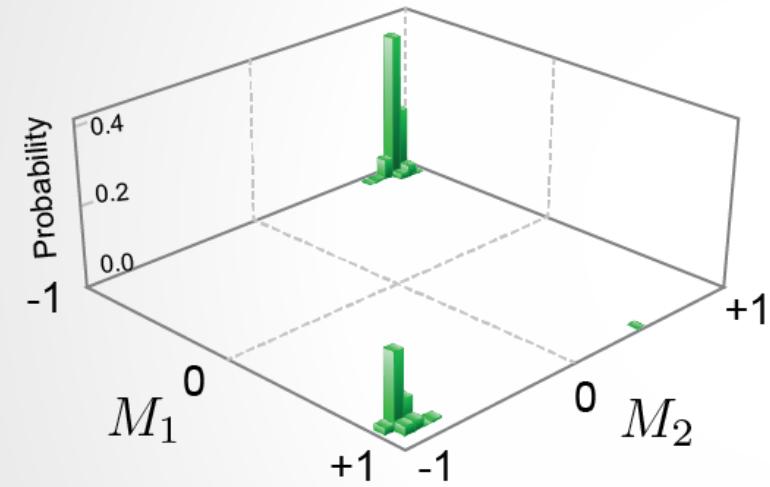
# FM and AFM regimes



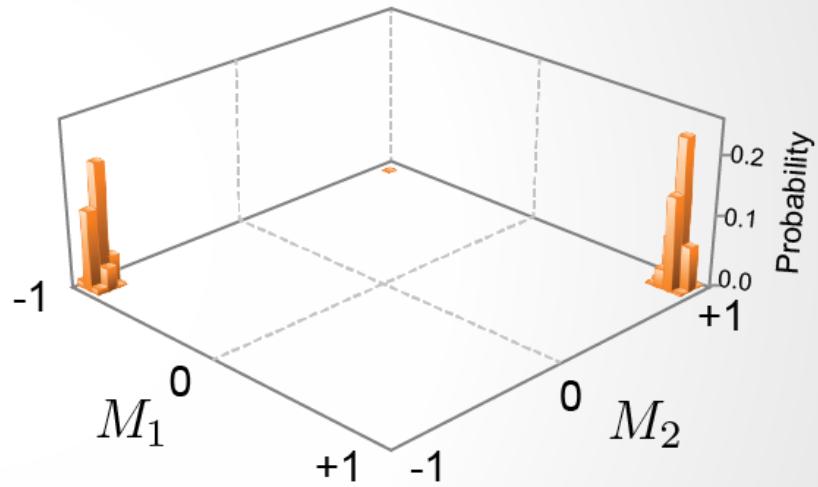
- Two distinct regimes
- sample or position independent

# Correlations

Antiferromagnetic

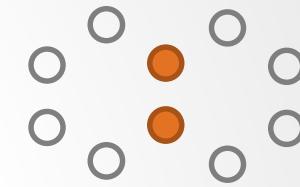
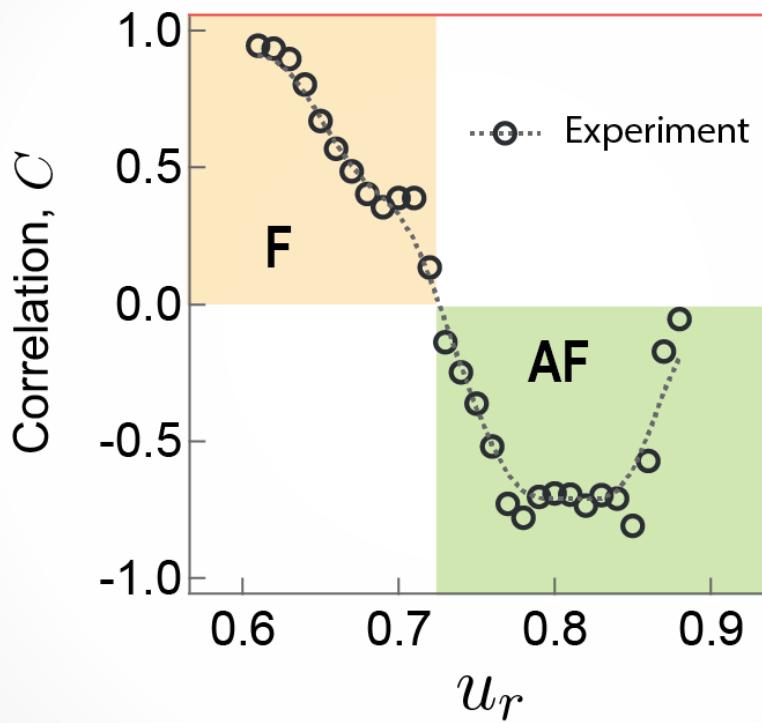


Ferromagnetic



- $M_n$  deg of circ pol of condensate  $n$
- Only two possible states in each regime
- Very robust (>99% coupling efficiency)

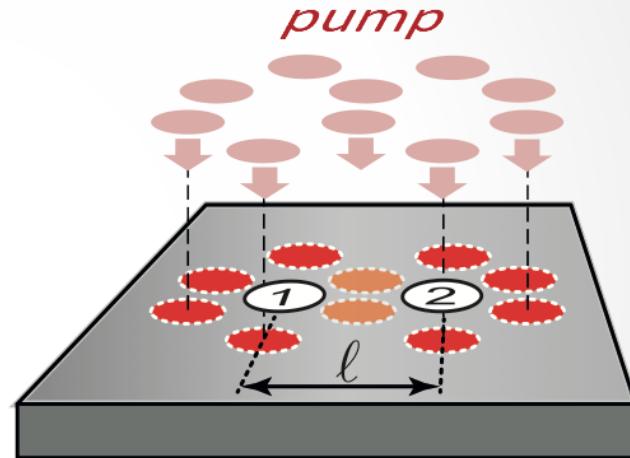
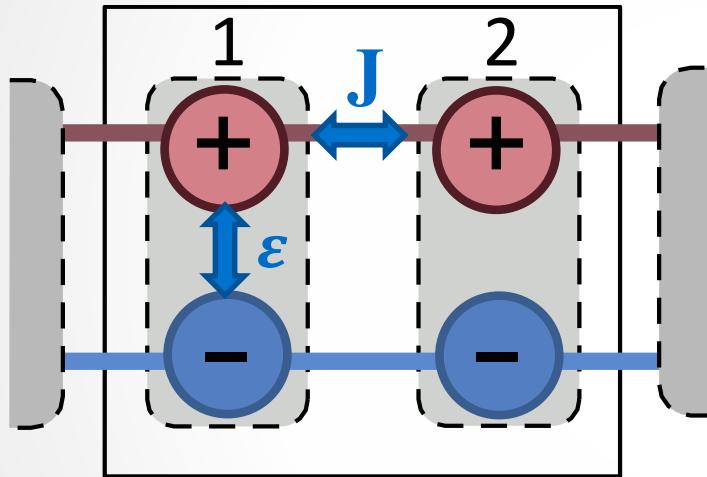
# FM to AFM transition



$$u_r = \frac{I_r}{I_0}$$

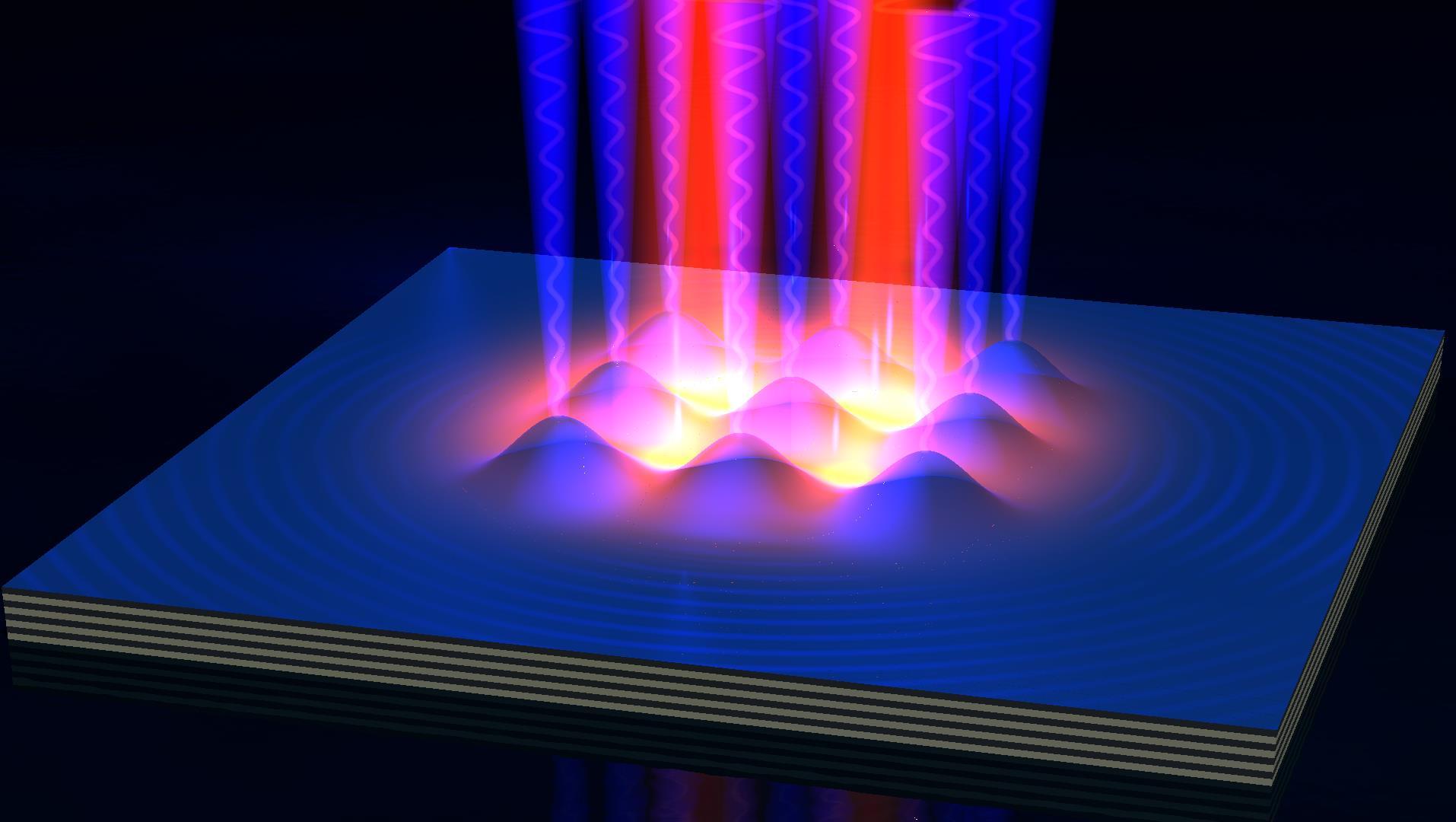
# Bose-Hubbard ladder

- Linear polarization splitting in **spin** space
- Josephson coupling in **real** space



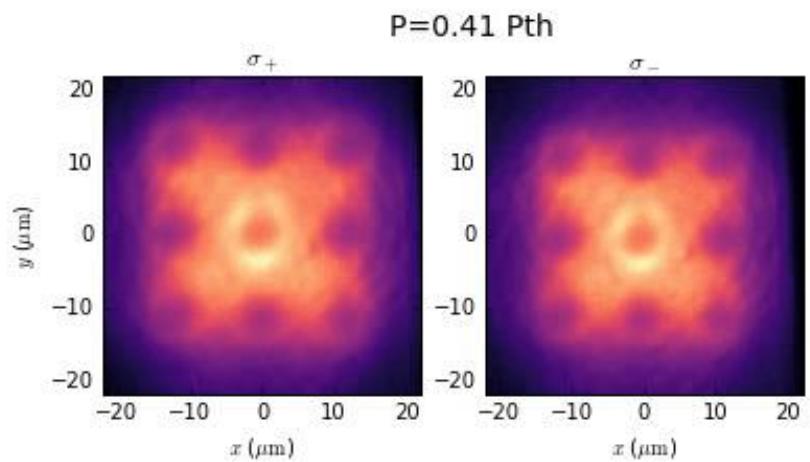
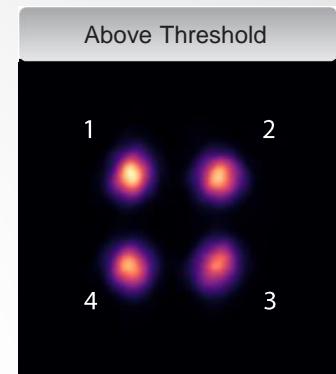
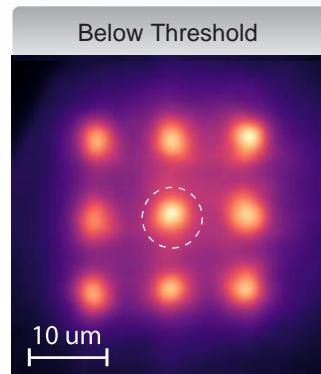
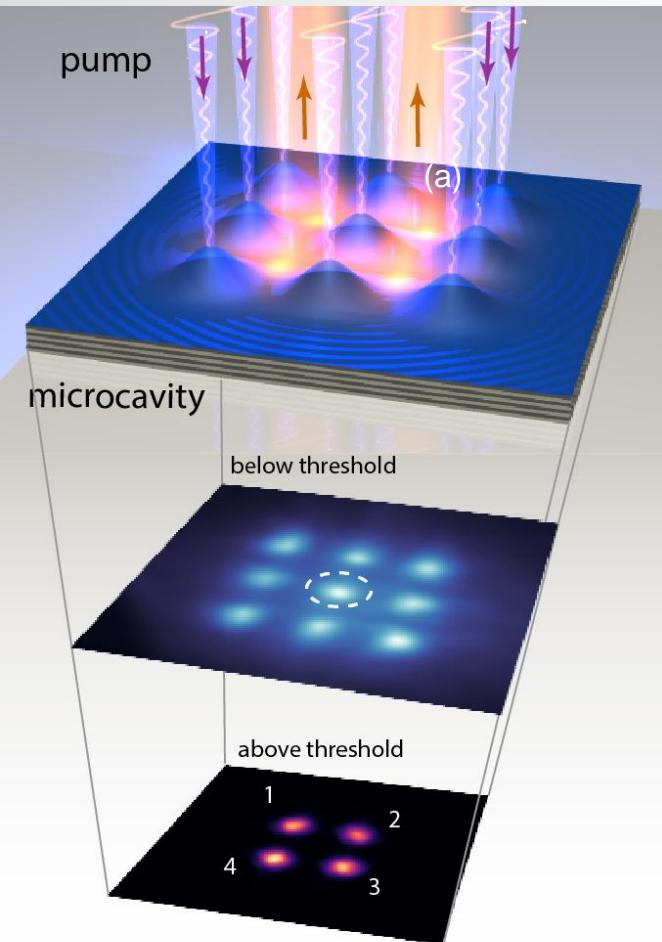
$$J > \epsilon \rightarrow FM$$

$$J < \epsilon \rightarrow AFM$$



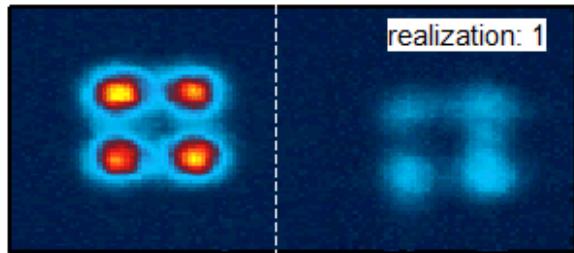
**Part 3**  
**Spin chains**  
Under review in PRL

# Spin chains

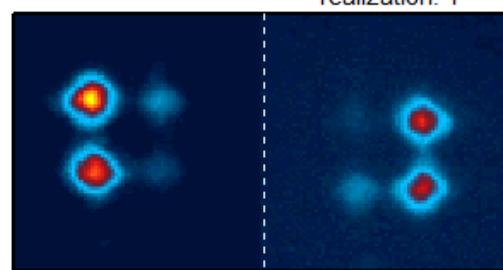


# Spin chains – From FM to AFM phases

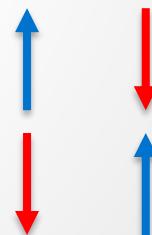
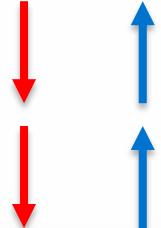
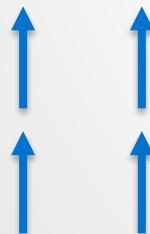
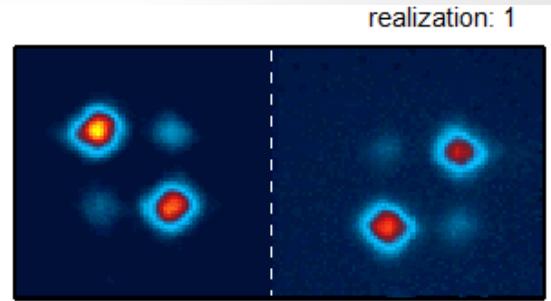
FM



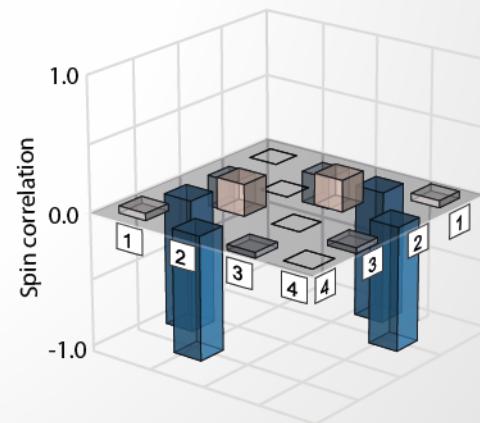
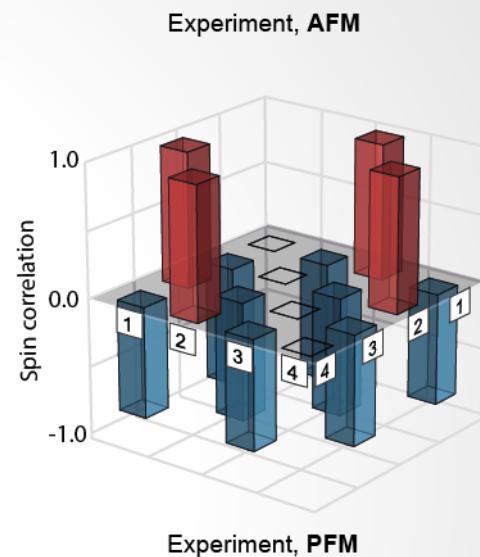
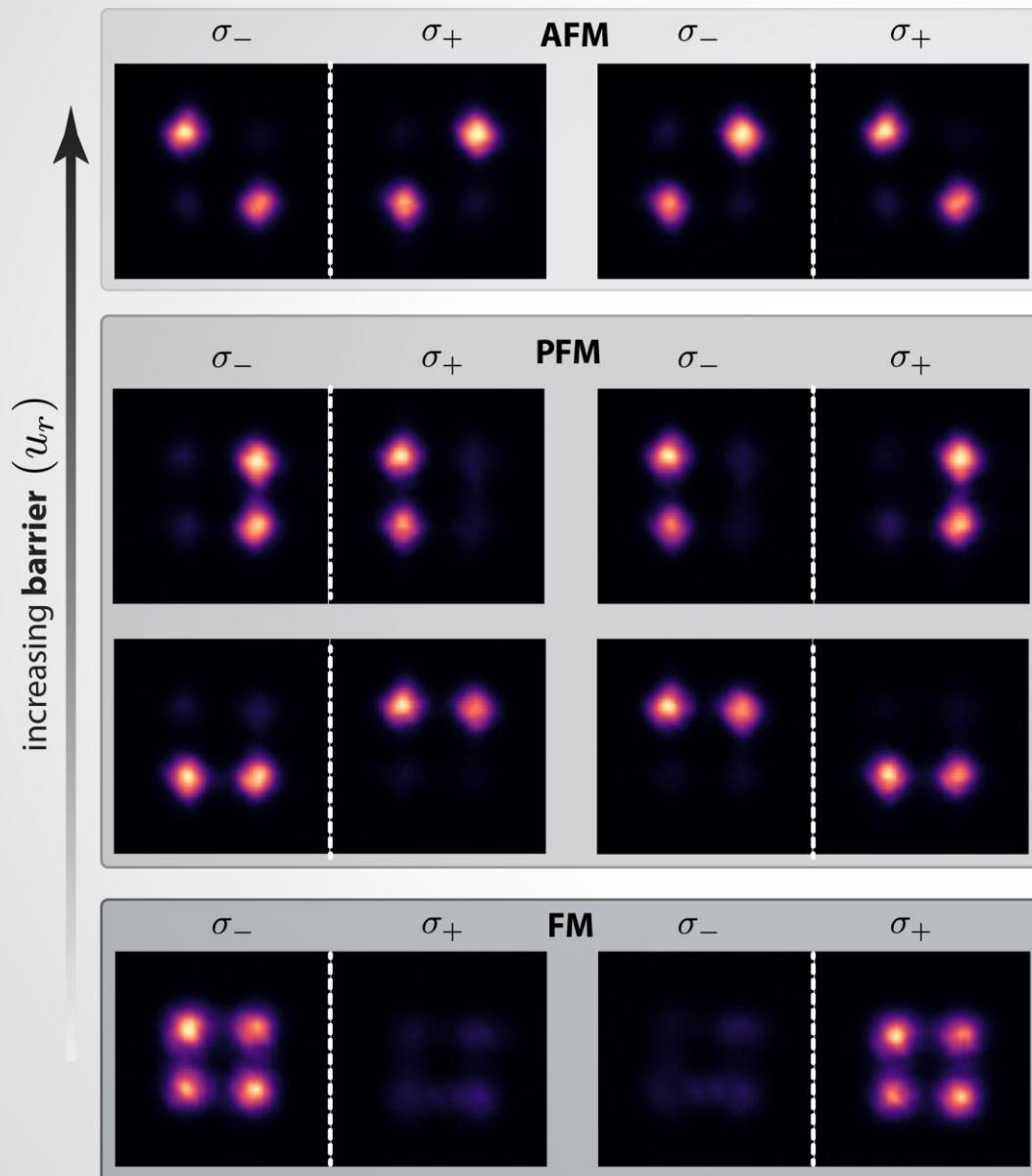
Paired-spin



AFM



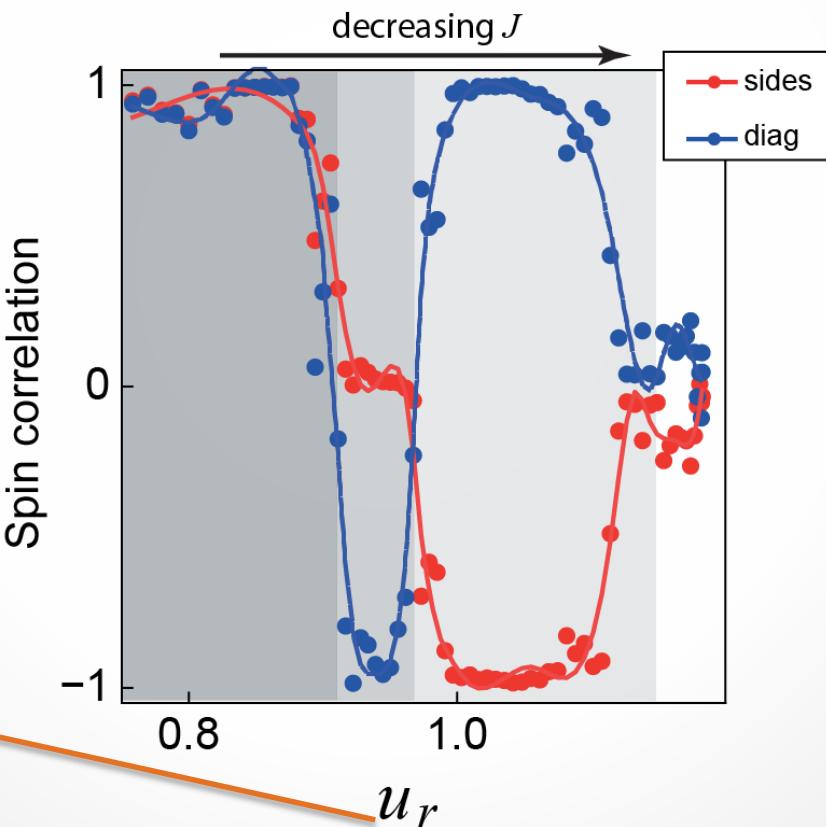
# Spin chain – Possible realizations



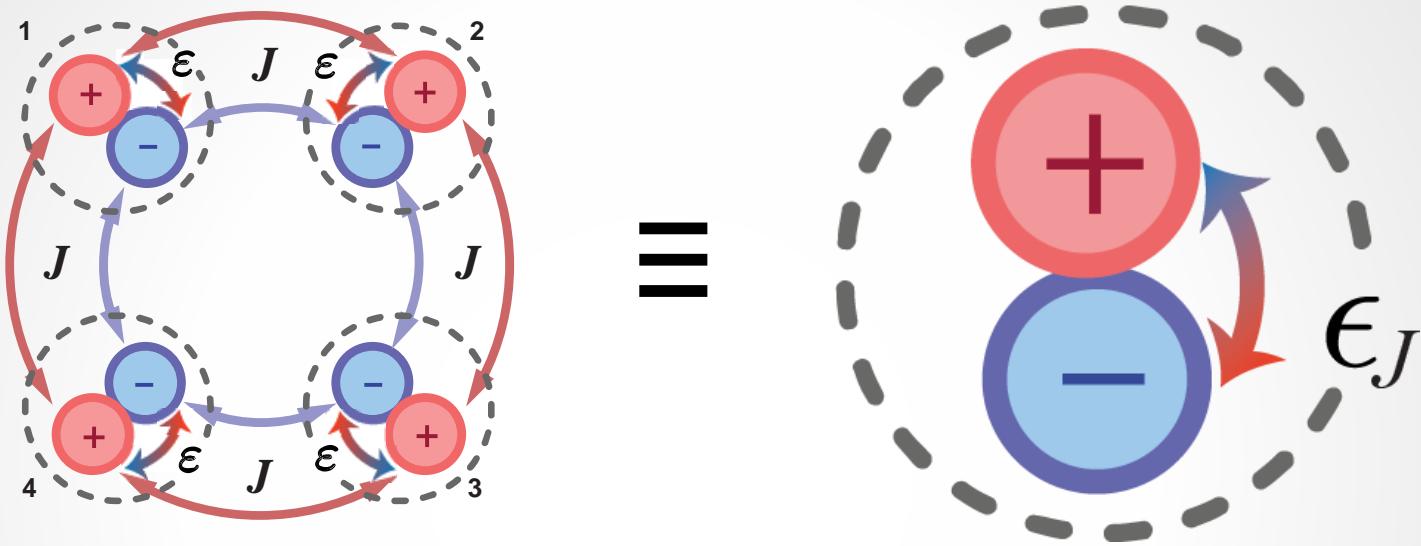
# Spin chain – Phase diagram

FM PFM AFM

Experiment



# Spin chain - Mean-field theory of spin chains



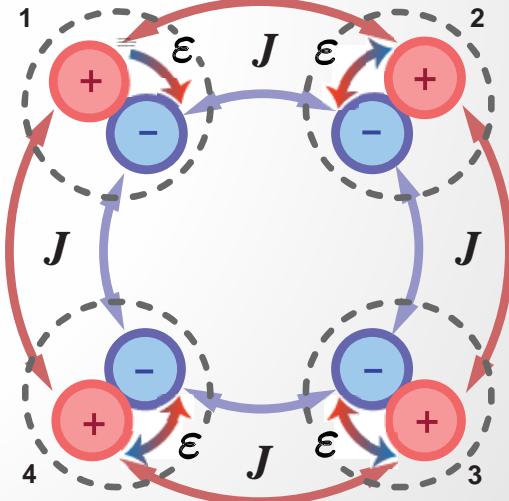
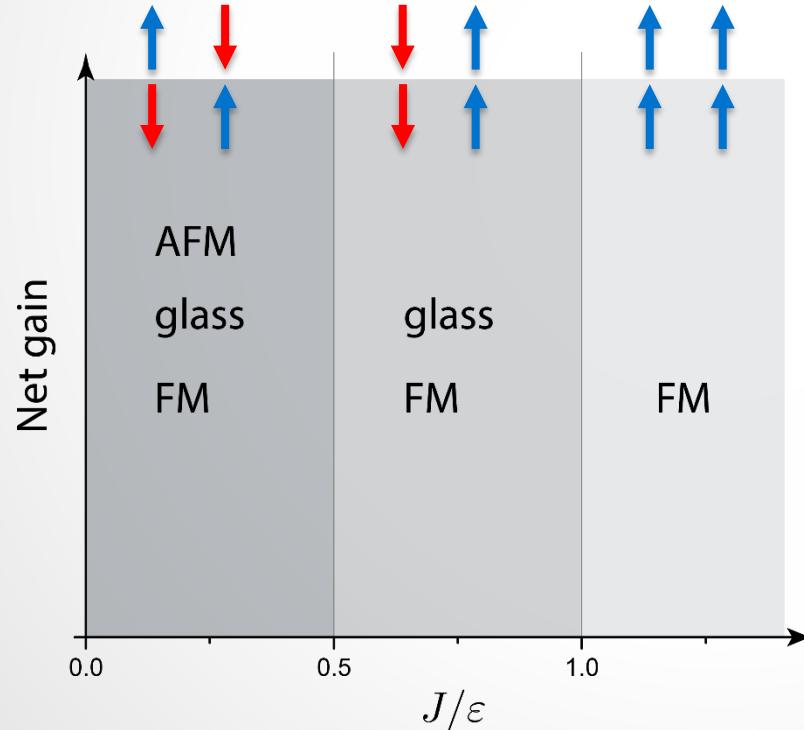
$$\text{renormalized } \epsilon_J = \epsilon + J(a_+ e^{i\phi_+} + a_- e^{i\phi_-}) \quad a = \begin{cases} 0: \text{ FM} \\ 1: \text{ AFM} \end{cases}$$

$$\text{energy shift: } \omega_J = -J((1 - a_+)e^{i\phi_+} + (1 - a_-) e^{i\phi_-})$$

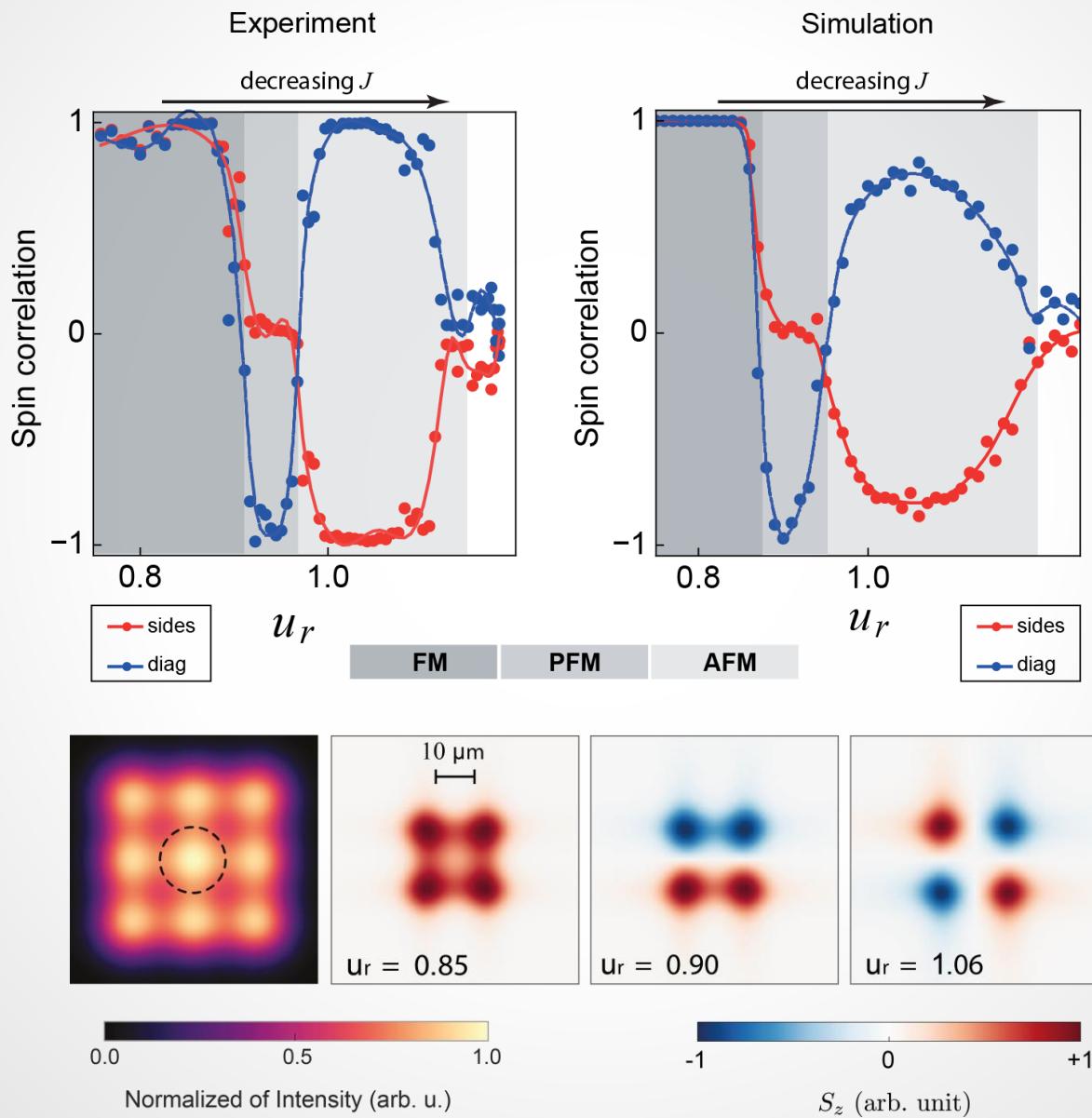
# Three key rules of spin chains

- $\varepsilon_J$  should be real and positive
- $\omega_J$  should be the same for all condensates
- Lowest threshold states win (smallest  $\varepsilon_J$ )

$$N_c \simeq \frac{\varepsilon}{\alpha}$$

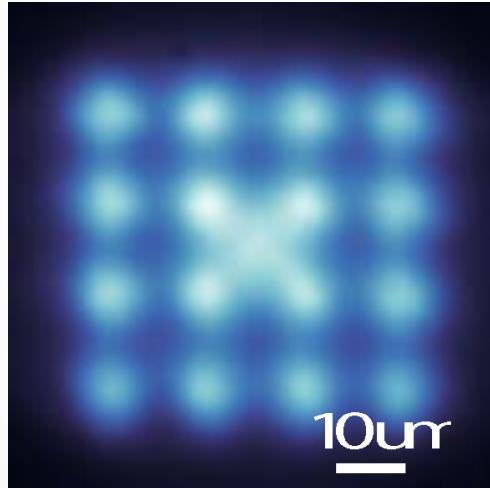


# Spin chain - 2D simulations

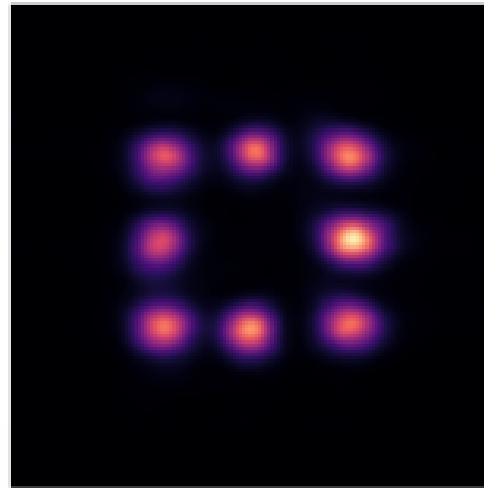


# Large spin rings

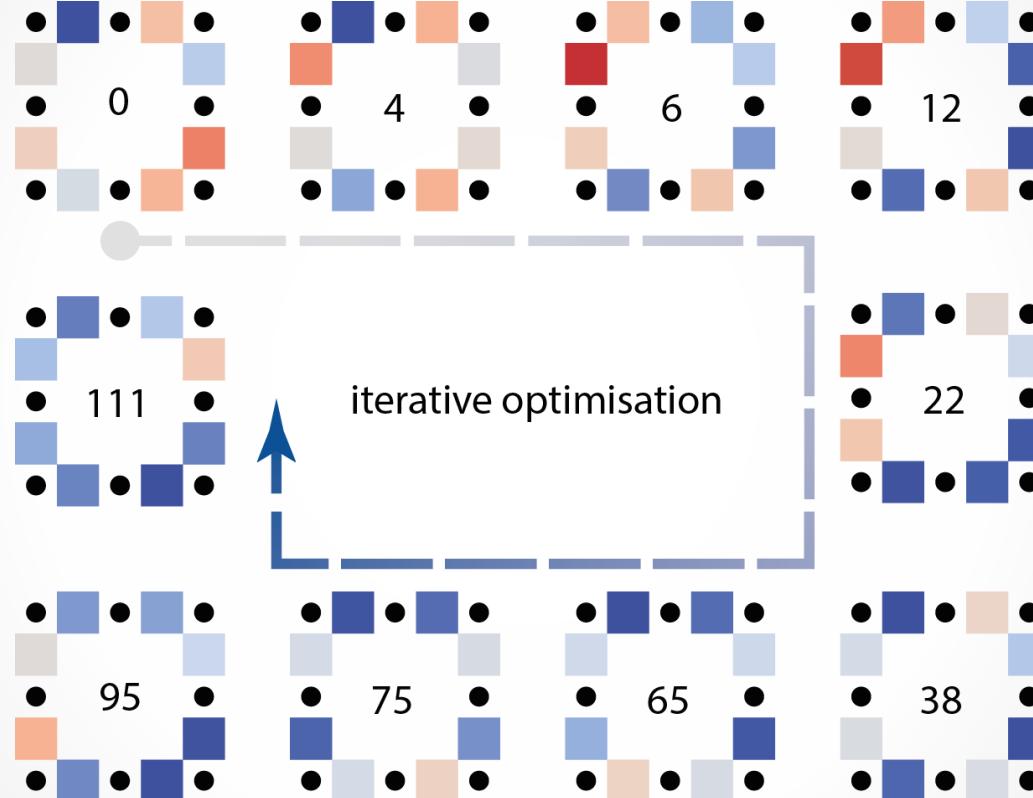
pump



condensate ring

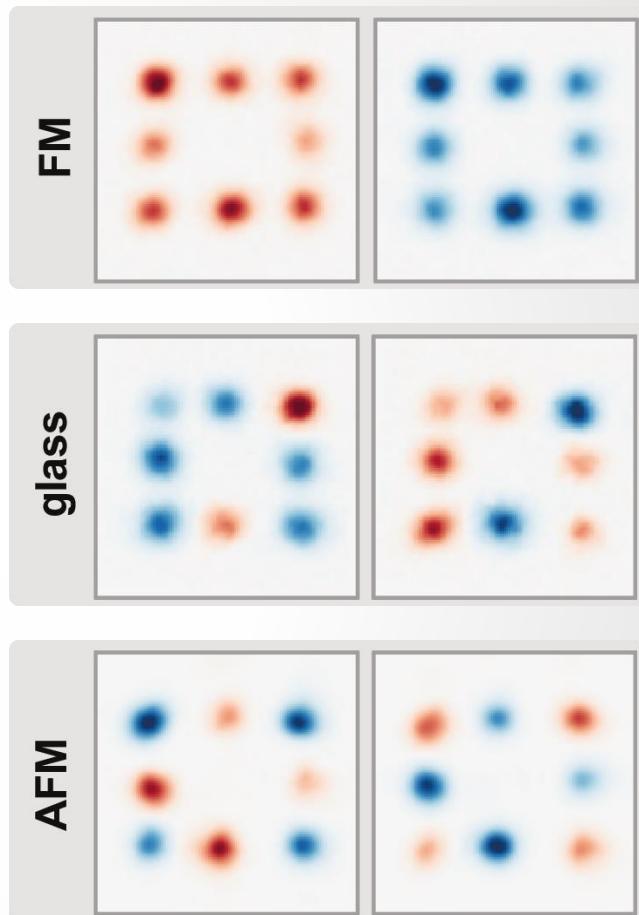
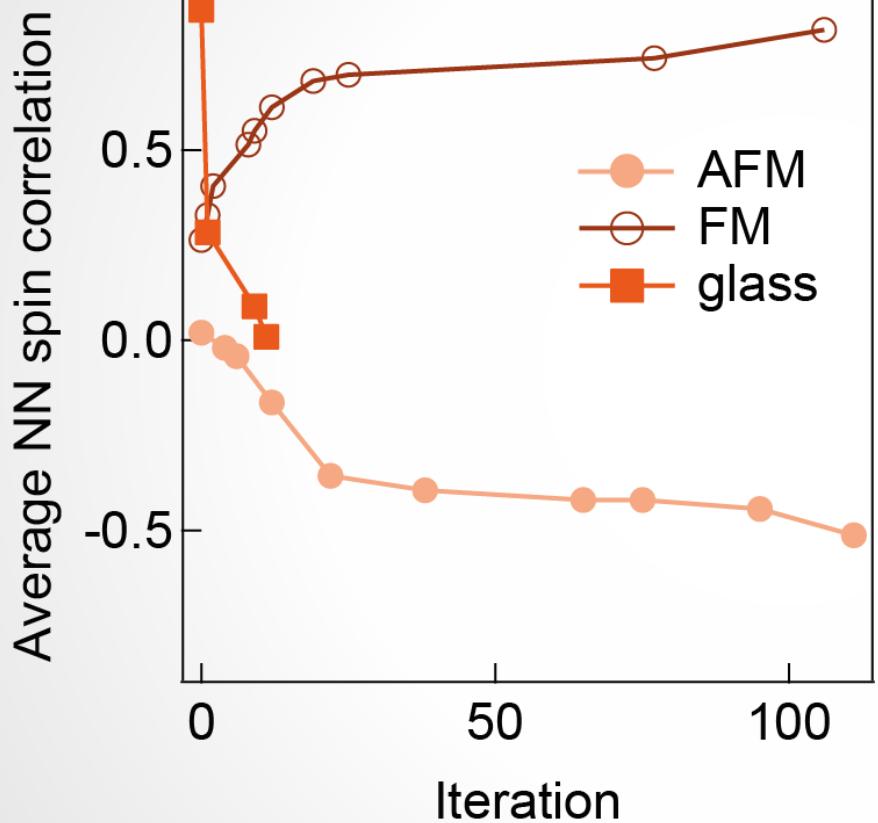


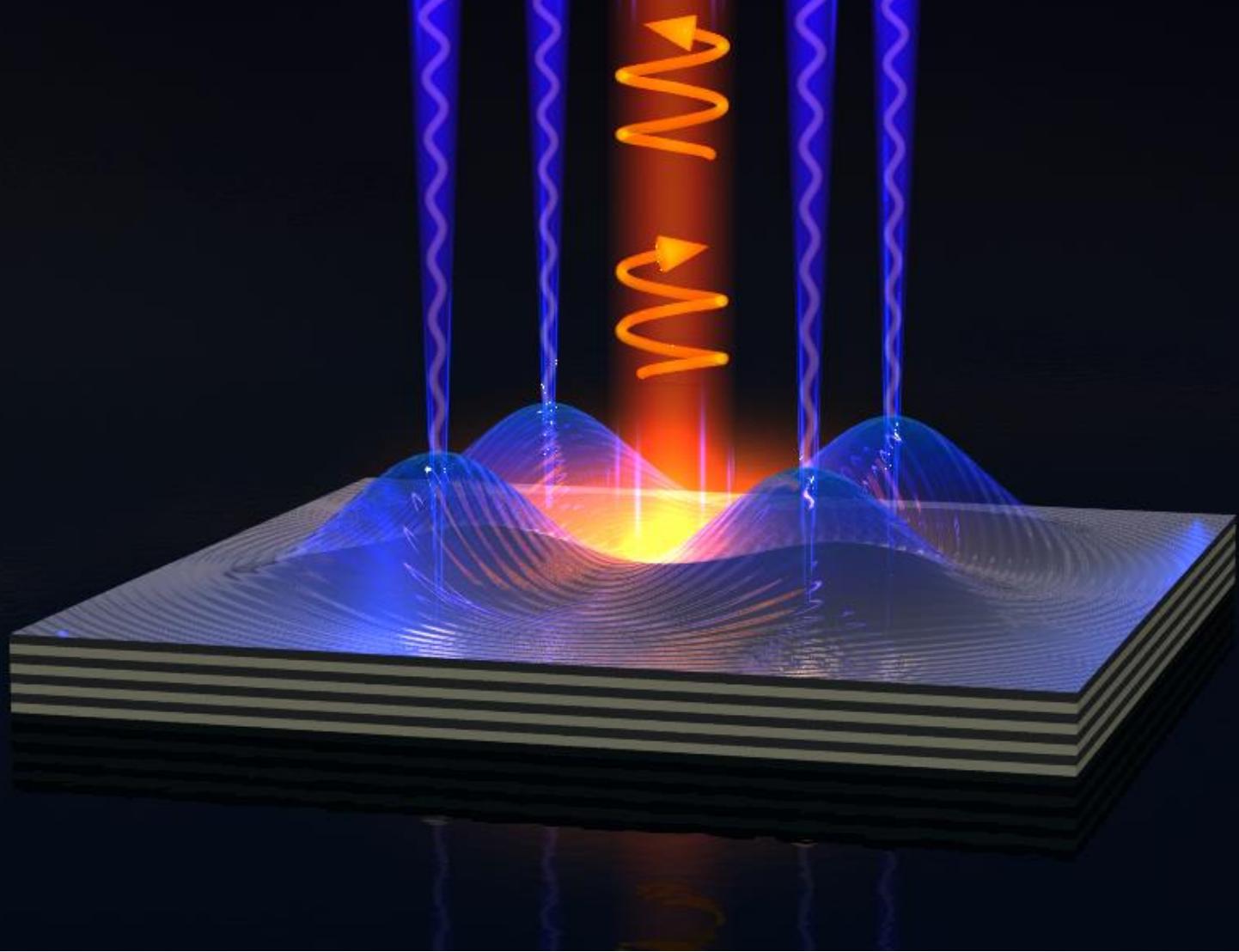
# Engineering spin interactions



blue link: AFM coupling  
red link: FM coupling

# From AFM to glass to FM





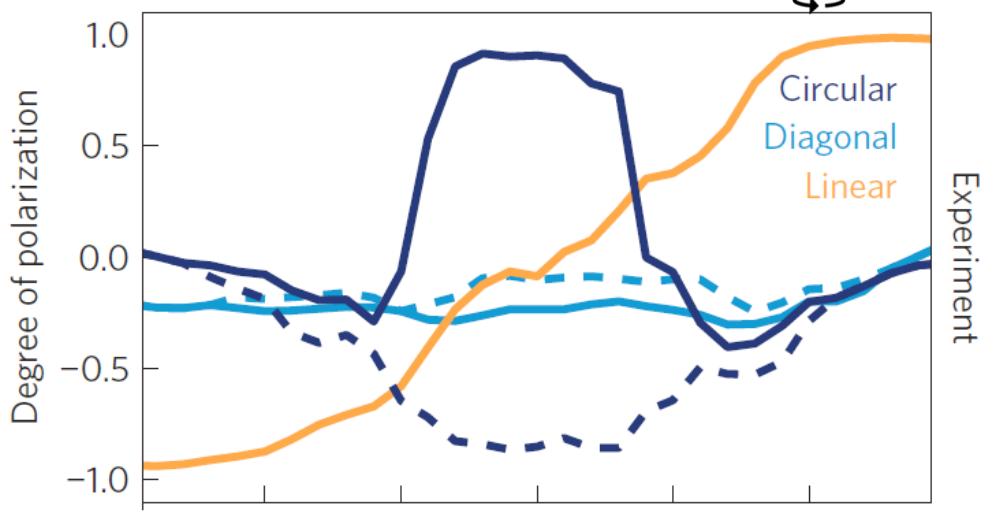
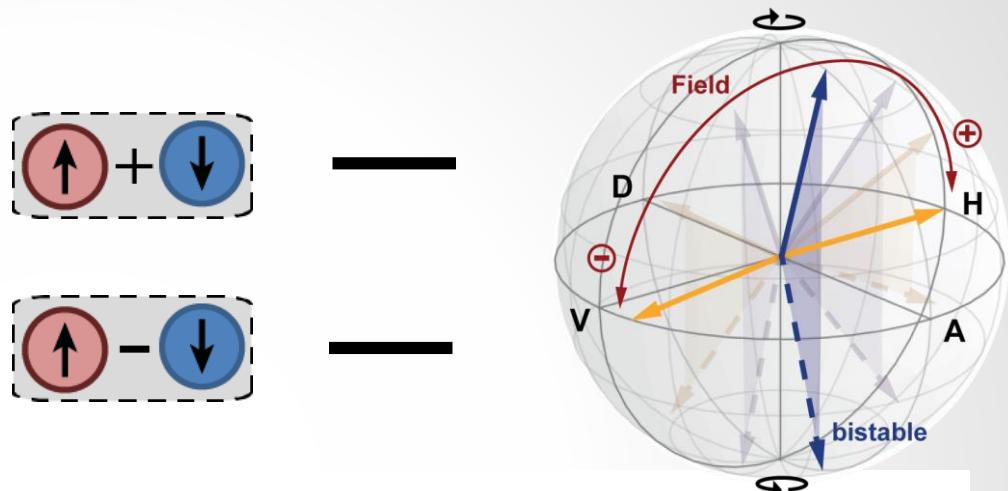
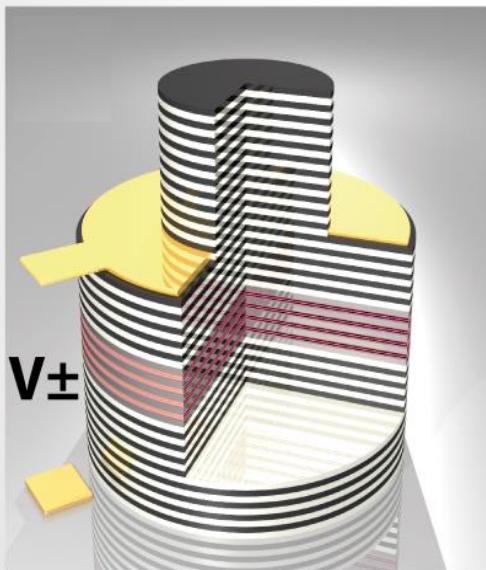
Part 4

## Electrical Spin Switching

Nature Materials (2016)

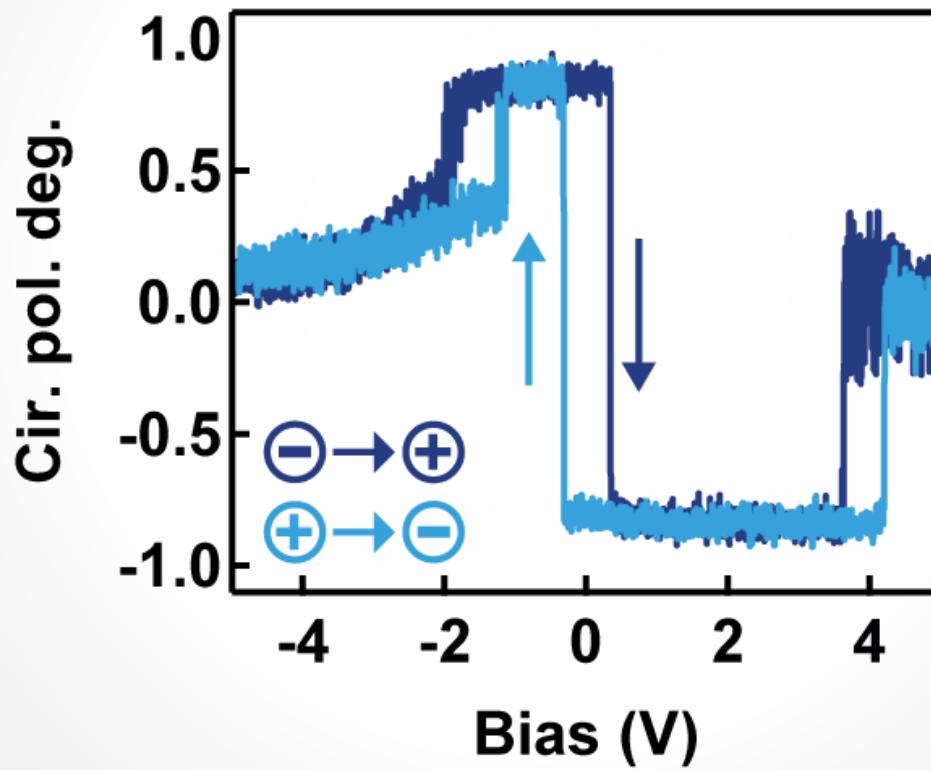
# Applying electric fields

- bias tunes linear polarization energy splitting (Pockel's effect)
- linear splitting controls bifurcation threshold

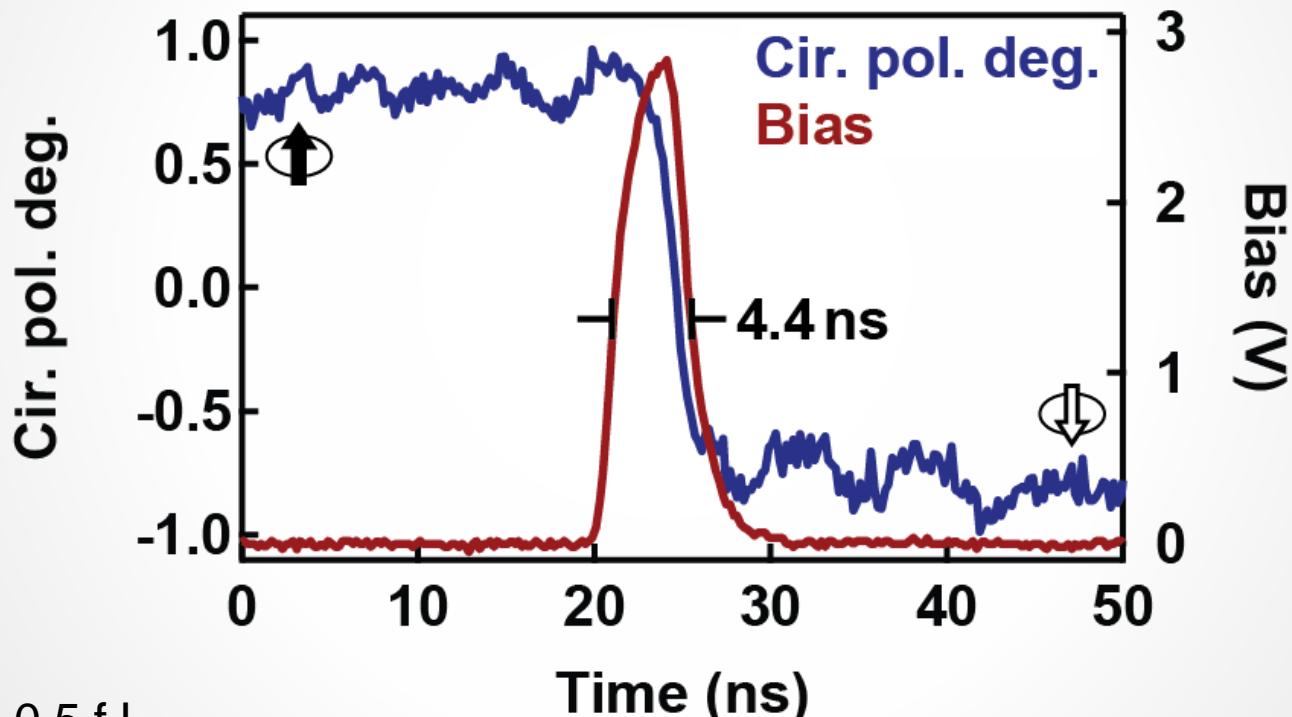


# Hysteresis

Pumping imbalance

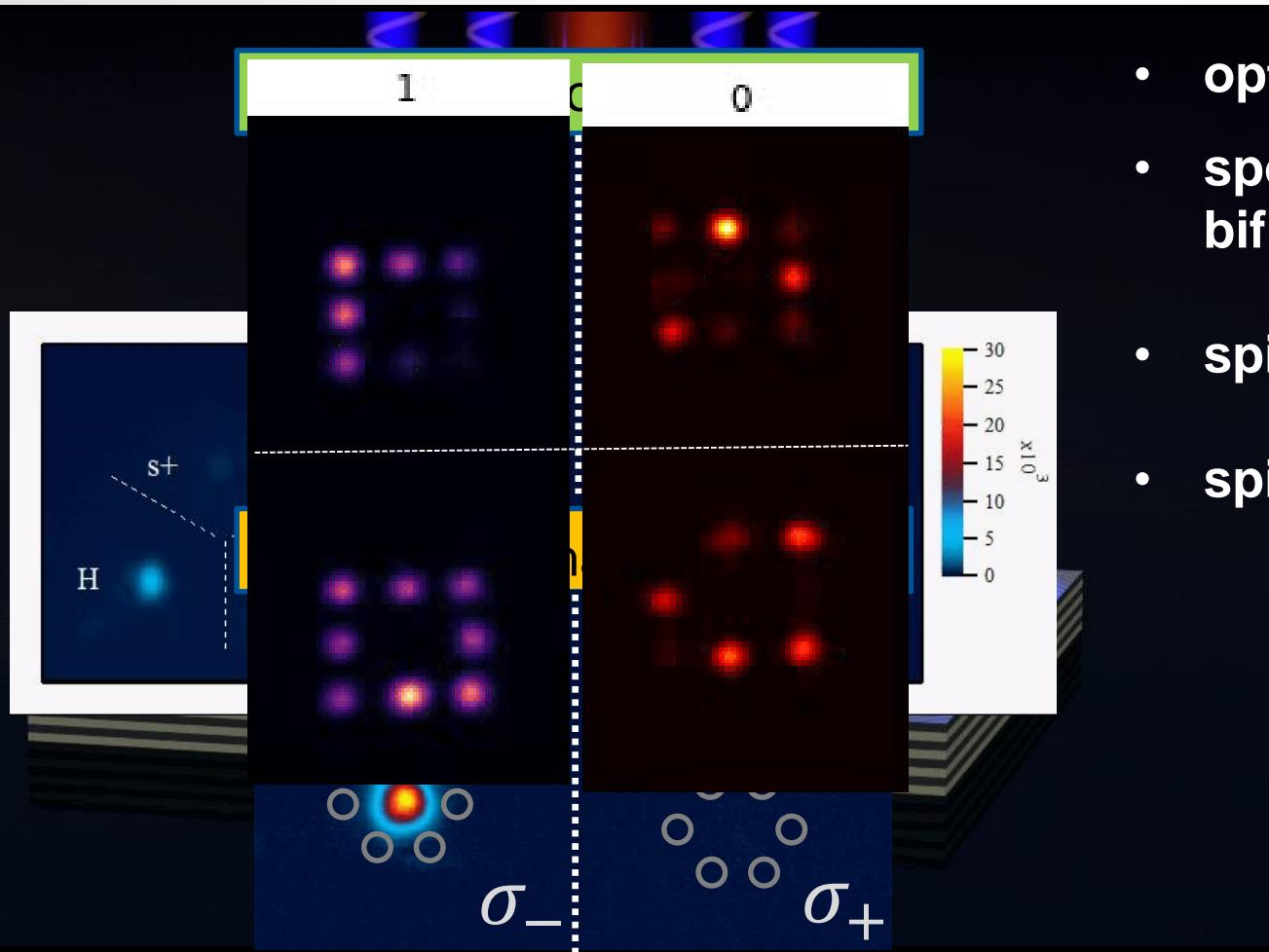


# Electrical spin switching



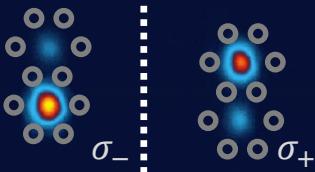
- $E \sim 0.5 \text{ fJ}$
- $t_s \approx 2.5 \text{ ns}$

# Conclusion and outlook

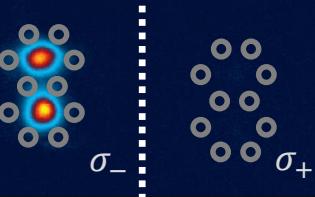


- optically induced traps
- spontaneous spin-bifurcation
- spin coupling
- spin chains

Antiferromagnetic



Ferromagnetic



Thank you!

